

MICROCOPY RESOLUTION TEST CHART



NAVAL POSTGRADUATE SCHOOL Monterey, California





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AN ANALYSIS OF SYMMETRIC REINFORCEMENT OF GRAPHITE/EPOXY HONEYCOMB SANDWICH PANELS WITH A CIRCULAR CUTOUT UNDER UNIAXIAL COMPRESSIVE LOADING

by

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An Analysis of Symmetric Reinforcement of Graphite/Epoxy Honeycomb Sandwich Panels with a Circular Cutout Under Uniaxial Compressive Loading

by

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Submitted in partial fulfillment of the requirements for the degree of

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ABSTRACT

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8.0	Panel RR22:	3-D Sig-Z I	FEA Contours 1	Near the (Cutout	•	311
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0 11	Damal BB22.	2-D Eng 7V	EEN Contours	Manu 444	Contament.		21/

LIST OF SYMBOLS

```
Area (in<sup>2</sup>)
[A]
        Iaminate inplane stiffness matrix (Eqn. 3.11)
        Characteristic length for the average stress failure
a.
           criterion (Eqn. 2.5)
        Radius of cutout (0.500 inch)
        Force resultnat-moment coupling matrix (Eqn. 3.16)
[B]
[C]
        Material elastic constant tensor (Eqn. 3.1)
[D]
        Laminate moment stiffness matrix (Eqn. 3.15)
        Diameter of cutout (1.00 inch)
đ
        Modulus of Elasticity (tension and compression) (psi)
        Strain gage excitation level (volts) (Eqn. 4.1)
E
{F}
        Force vector (lbf) (Eqn. 3.29)
        Thickness of a laminate ply (inch)
h
G
        Shear modulus of elasticity (psi)
        Stress concentration factor
        Finite element stiffness matrix (Eqn. 3.29)
[K]
        Radius of curvature (Eqn. 3.17)
1
        Panel length (in)
        Moment vector (Eqn. 3.13)
{M}
        Stress resultant vector (Eqn. 3.12)
{N}
        Power density (watt/in<sup>2</sup>)
                                  (Eqn. 4.1)
PD
        Resistnace (ohms) (Eqn. 4.1)
R
        Radial distance from the origin (inch)
r
[Q]
        Reduced laminate stiffness matrix (Eqn.
        Reduced transformed laminate stiffness matrix (Eqn. 3.10)
[Q']
        Applied stress (psi)
S
```

- S Compliance (Eqn. 3.23)
- [T] Rotation transorm matrix (Eqn. 3.9)
- w Panel width (in)
- X,Y,Z Rectangular
- | b | Displacement vector (Eqn. 3.27)
- $\overline{\sigma}_n$ Direct stress
- € Direct strain
- σ Applied far-field normal stress
- Poisson's ratio
- $\xi d/[2(d/2 + a.)]$
- $\mu\epsilon$ microstrain (*10⁶)
- Y Shear strain

Average

Subscripts

avg

419	ozago		
С	Compression		
i,j,k	Indices of summation		
1	Lateral direction (parallel to load line)		
max	Maximum		
n	Notched panel		
σ	Stress		
€	Strain		
t	Tension		
t	Transverse direction (prependicular to load line)		
u	Unnotched panel		
ult	Ultimate strength (indicating total failure)		
1,2	Directions parallel and perpendicular to principal fiber direction respectively		
∞	Infinite panel width		

Abbreviations

ASFC Average Stress Failure Criterion

DOF Degrees of freedom (at a node)

Eps-X Strain in the x direction (ϵ_x)

Eps-Y Strain in the y direction (ϵ_{v})

Eps-XY Shear Strain (ϵ_{xy})

FAPF First Audible Ply Failure

FEA Finite Element Analysis

G/Ep Graphite /Epoxy

Ksi Thousand pound force per square inch

LEFEA Linear Elastic Finite Element Analysis

LEFM Linear Elastic Fracture Mechanics

msi Million pound force per square inch

NDI Non-Distructive Inspection

SCF Stress Concentration Factor

ACKNOWLEDGEMENTS

For inspiration and guidance I turn to Lao Tsu. He set these words down during the sixth century B.C. in the province of Honan, China:

Thirty spokes share the wheel's hub; It is the center hole that makes it useful. Shape clay into a vessel; It is the space within that makes it useful. Cut doors and windows for a room; It is the holes which make it useful. Therefore profit comes from what is there; Usefulness from what is not there.

It was upon that passage that this paper was based.

The author owes an incalculable debt of gratitude to the people who made this research possible, for their unflagging patience, if nothing else. The first among these is Professor Milton Bank who was initially drafted to the task of Thesis Advisor but who then adopted my project as his own. His zest and enthusiasm for knowledge changed my life. Professor E.M. Wu entered the project at the last stage and gave it a fine polish.

Robert Besel, Glenn Middleton and Ted Dunton of the Naval Postgraduate School, Department of Aeronautics devoted untold hours to helping me prepare the test apparatus and contributed no end of advice and assistance. Drs. J.A. Bailie, Norman Cyr of Lockheed Missiles and Space Corp, Sunnyvale, CA never tired of my endless questions. The success of this research is due to their most subtle guidance. My debt to both of them goes beyond what can be told. The funds for this research were wholly provided by the U.S. Navy Strategic System Project Office, Washington, DC.

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INTRODUCTION

The ratio of strength to weight is one of the principal means of determining the efficiency of a structure. In aerospace applications this comparison can be the most meaningful measure. The dilemma of designing an airframe for both strength and lightness has been with us since the days of daVinci. The quest for ever higher ratios of strength-to-weight has led to the development and use of high modulus advanced composite materials, principally graphite or carbon fibers bonded together in a polymer matrix, in the place of metal.

Major airframe structural components such as wings or bulkheads require cutouts for bolted or riveted attachment, access to interior space and passage of control and fuel lines. Timoshenko and Goodier [Ref. 1: pp. 78-84], among others, point out that such holes in load-bearing structures act to greatly increase the local stress and to reduce ultimate strength. This characteristic is referred to as the stress (or strain) concentration factor (SCF or K). It seems the SCF may have several definitions, depending on the material and the researcher. In this report it shall be defined as the highest plane strain existing around a cutout divided by the far-field strain; generally called the gross SCF or Kgross. Taking into consideration Saint-Venant's principle, the far-field strain is assumed to be equal to the strain which would exist in an ideal, thin, stressed infinite plate if a cutout was not present. Stress and strain concentrations, while inextricably linked in elastic materials, are not the same. However, since in the application discussed here, there is little appreciable

numerical difference, the term "SCF" will be used to indicate either the stress or strain concentration factor.

When holes or cutouts are necessary in a structural component, airframe designers generally have the choice of accepting either a significantly lower ultimate load or greatly increasing the component's strength, and thus its weight. In either case the ratio of strength-to-weight is reduced in proportion to the highest SCF existing within the member. Properly designed ductile metal structures mitigate the effects of SCF by plastically deforming under high load conditions. This response delays ultimate failure, but can also lead to unacceptable reductions in both stiffness and fatigue life.

The metals used in aircraft construction, principally aluminum and titanium, can almost always be considered isotropic (many manufacturing processes, however, introduce some minor directional properties). The magnitude of the orthogonal strains (X, Y and shear) existing at a point in a plane isotropic panel result from the orthogonal stress resultant at that point and are in proportion determined by the elastic modulus and Poisson's ratio. An applied in-plane stress on an isotropic plate will not induce curvature other than, of course, the possibility of the plate buckling under compression. Composite plates are termed "quasiisotropic" when they are composed of anisotropic or orthotropic laminae stacked with the directional properties arranged in a manner to react identically to a true isotropic material to both moments and inplane loads.

Composite laminates typically lack the ductility of metals. The high-modulus graphite/epoxy (G/Ep) fibers in general use in the aerospace industry allow approximately 1% strain $(10,000\,\mu$)

in tension and compression to complete failure. Depending on the fiber orientation, panels constructed of laminated advanced composites with notches or cutouts can demonstrate from slightly less to much more sensitivity to holes or cutouts than otherwise identical isotropic metal panels. As shown by Rybicki and Hopper [Ref. 2: pp. 15-27], among others, this sensitivity principally depends on the type of weave and the orientation of the plies in the laminate; that is, it depends on the degree of orthotropy.

The inherently brittle nature of advanced composite materials, their characteristically low strain to failure, coupled with manufacturing limitations make their design a far more demanding task than that for metals. Other characteristics, however, including fatigue and corrosion resistance, light weight, and easily tailored directional properties make the design of composite structures very attractive, particularly to the aerospace designer.

A. OBJECTIVES AND SCOPE

This study was designed to investigate the effect of relatively simple co-cured reinforcement of a cutout on the strain field and failure behavior in G/Ep honeycomb sandwich panels subjected to uniaxial compression. Honeycomb construction allows very light yet exceptionally stiff structures. The objective was to determine if a simple and inexpensive reinforcement geometry using small volumes of co-cured G/Ep lamina near the cutout could significantly reduce local stress concentrations and increase the ultimate failure strength in the honeycomb laminate. The idea of local reinforcement around holes is not new; Timoshenko noted [Ref. 1: p. 82] that "reinforcing rings" could decrease the SCF in plates with cutouts. The point was to examine the reaction of an

advanced composite, a material whose characteristics differ markedly from those Timoshenko addressed.

The research was undertaken with the manufacturer principally in mind. Complex or exceptionally thick reinforcement geometries are difficult and expensive to manufacture cost-effectively or with a high degree of quality assurance. This research used only very thin (maximum thickness: 0.028") ply reinforcement in three relatively simple geometries. Since facesheets with reinforcing plies on both sides would require machining a precise shallow depression in both the face of the the honeycomb core and the surface of the layup plate, each difficult and expensive tasks, reinforcement was restricted to the outside surface of each facesheet.

This study was limited to one panel size (10.00" x 8.50"), a single loading condition (uniaxial compression) and three relatively simple reinforcement geometries. The 1.00 inch diameter circular cutout was reinforced with concentric co-cured round and square G/Ep plies around the hole and stiffening strips displaced 0.50 inch (1 hole radius) laterally from the cutout edge. The total amount of reinforcement used varied from 1 to 5 times the G/Ep removed from the cutout. Reinforcement was either one or two plies symmetrically applied to the outside of both facesheets of the panel. A honeycomb core was used, as it would be in an actual application, to increase the panel bending stiffness and thus eliminate the buckling of the whole panel as a mode of failure.

The basic panel facesheets were four layer [0,±45,90] HMF330C/34 G/Ep cured to a thickness of 0.056 inch. Cured sheets were bonded to both sides of a 0.50 inch thick fiberglass/phenolic honeycomb core using 3M, Inc.'s AF-126 (250°F) cured adhesive.

The result was a very light, thin quasi-isotropic laminate: [0,±45,90,core]_s with a great resistance to bending. The HMF330C/34 is a woven, high-temperature epoxy (350°F) G/Ep fabric manufactured by the Fiberite Corporation of Winona, MN. In order to reduce the number of design variables the principal axis of the reinforcement plies was oriented only in the direction of the applied compressive load. This theoretically gives the highest stress concentration and could be considered the worst case.

B. REVIEW OF LITERATURE

1. Background and Historical Research

The subject of notch-induced stress concentrations in plates has been extensively documented. The effects reinforcement have on the SCF in plates have received considerably less attention. Early research concentrated on metals (isotropic materials) and focused on defining the stress and strain fields around circular and elliptic cutouts. Recent research has been primarily in characterizing the response of orthotropic and anisotropic materials.

Kirsch [Ref. 3] is commonly cited as the first to determine exactly the stress concentration factor of a cutout in an isotropic material from the theory of elasticity. Howland [Ref. 4] applied the solution to Airy's equation in polar coordinates to determine the magnitude of the SCF. One of the earliest papers addressing reinforced holes was by Levy, Woolley, and Kroll [Ref. 5]. They investigated the effect of both reinforced and unreinforced holes on the buckling strength of square isotropic plates. They determined that presence of a hole caused only a relatively minor reduction in the buckling (ultimate) load.

A thorough theoretical, closed-form mathematical treatment of anisotropic materials with stress concentrations can be found in the work of two Russian applied mathematicians, S.G. Lekhnitskii and G.N. Savin. Lekhnitskii [Ref. 6] principally addressed the distribution of stress around the edge of variously shaped cutouts in unreinforced anisotropic plates and shells under a variety of loading conditions. He determined that a plate with high anisotropy, as found in strictly unidirectional fiber construction, could produce a stress concentration factor near 9 when the load was parallel (0°) to the principal fiber direction, and slightly more than 2 with the load perpendicular (90°) to it. It must be pointed out that, in composite materials, the SCF may not have a exactly proportional effect on the reduction in the ultimate strength of the plate. Due to the composite's ability to redirect the load path once fibers are broken or lose stiffness through matrix degradation, the ultimate strength is not degraded as much as would be expected by the presence of the stress concentration. This phenomenon is discussed in more detail in section II.D.4.

Savin [Ref. 7] treated the stress and strain fields in a plate resulting from a cutout. He addressed the SCF as a function of a plate's linear material properties, ply orientation and stacking, and its loading. Hole size, reinforcement and geometry were not addressed. A computer program was developed by Garbo and Ogonowski of McDonnell-Douglas [Ref. 8: Vol. 3] which computes the stress and strain field around a cutout based on Lekhnitskii's and Savin's analyses. It was modified by the author for the IBM 370 and is listed in Appendix P.

Substantial research in stress concentrations in composite plates was done by Greszczuk [Ref. 9]. He developed a theoretical solution for failure stress and stress concentrations in both orthotropic and anisotropic material under tension. His method was based on the Hencky-Von Mises distortion energy method, and gave both magnitude and locations of the ultimate stress. Rybicki and Schmueser [Ref. 10] investigated the effects of laminate stacking sequence, lay-up angles, fabrication temperature and thickness on panel stress concentrations using finite element analysis.

There is relatively little research into the effects of reinforcement around holes in composite plates which has been reported in the open literature. Virtually nothing is available on the behavior of notched reinforced plates in compression or on the effect on the type of failure of using honeycomb in such structures.

Kocher and Cross [Ref. 11] demonstrated experimentally that titanium, graphite and steel reinforcement around a circular cutout in a composite plate could reduce the SCF and increase the ultimate failure load in tension. Their results, however, were based on relatively complex, thick reinforcement geometries that have not found acceptance in aeronautical design.

A novel cutout reinforcement method using bonded hoop-wound G/Ep disks was addressed by McKenzie [Ref. 12]. The disks were used to reinforce both aluminum and G/Ep plates under tensile loads. The method proved effective both in reducing the stress around the cutout and increasing the plates' strength.

The team of Daniel, Rowlands and Whiteside [Refs. 13-17] did extensive experimental work in characterizing the effects of

cutouts on a variety of composite materials. They did some limited testing of reinforced specimens in tension and found proportionately reduced SCFs and increased strength. They determined that interlaminar deformations occurred in the boundary region of the cutout, an area they defined as extending about one laminate thickness from the free edge. This deformation was very nonlinear and could cause delamination at relatively low loads. Strain levels next to the cutout, prior to failure, were found to be higher than the ultimate failure strain of panels without cutouts. Based on that, they determined that the SCF did not necessarily produce a proportional reduction in strength. They recommended keeping the reinforcement close to the hole, using stepped diameter plies ("wedding cake") to facilitate the load transfer, and using 45° plies in the reinforcement where possible.

Knauss, Starnes, Henneke [Ref. 18] tested unreinforced 0.15 and 0.24 inch thick T300/5208 panels in compression for unbuckled and postbuckled strength. They found that under high, but less than normally ultimate stress levels, the laminate around the hole could buckle locally, delaminate and initiate total panel failure. A micro-mechanical failure mode was postulated where limited fiber buckling at the point of stress concentration caused by local imperfections such as voids, matrix cracking or poor fiber-matrix bonds led to total failure.

2. Summary of Recent Related Research

This report is the fourth in a series of investigations on the character of stress concentrations in composite plates made of HMF330C/34 G/Ep. This particular material was chosen because of its current use in both the Trident submarine launched ballistic

missile (SLBM) and the prototype Lear Fan propjet aircraft and the fact that it has a relatively small data base compared to other G/Ep prepreg material currently in aerospace use. This research was funded by the Strategic Systems Project Office of the Naval Sea Systems Command and greatly assisted by Lockheed Missiles and Space Co. (LMSC), Sunnyvale, CA.

The initial project was undertaken by Herman [Ref. 19] who investigated the pre- and postbuckled strength of HMF330C/34 panels loaded strictly in shear. He used a molded-in 45° flange around the cutout to add strength to the shear web. He determined that this reinforcement method was well-suited to adding stiffness to panels that were not buckled but that the panels did not see a significant increase in ultimate strength once buckling had occurred.

O'Neill [Ref. 20] demonstrated that reinforcement of only one face of a notched panel under tensile loading provided limited additional strength. Initially, the reinforcement of only one side of a cutout was considered attractive since only a small additional manufacturing effort was required. Asymmetric reinforcement, however, displaces the midplane of the laminate (under the reinforced area) toward the reinforced side. Uniaxial tension tends to pull this local midplane toward the load line, causing out-of-plane bending at the hole, which results in high shear stress between plies, delamination and premature failure. The delamination counteracts most of the decrease in stress concentration provided by the reinforcement.

Pickett and Sullivan [Ref. 21] and Bank, et al. [Ref. 22] continued O'Neill's research examining tension panels with symmetric reinforcement. They showed that suitably designed

reinforcement which was symmetric along the axis extending through the panel's thickness could both reduce strain concentrations and proportionately increase the ultimate strength. No delamination was noted in their test panels.

The work reported here extends the idea of symmetric hole reinforcement to compression specimens with a honeycomb core.

II. APPROACH TO THE PROBLEM

A thorough investigation into the effect of reinforcement around stress concentrations in composite plates must examine various materials, hole sizes, panel and reinforcement layups and geometries as well as the means and directions of load application. This research addressed only a small portion of the total problem. The material, hole and panel size, layup and loading method remained constant—only the amount and the shape of the reinforcement was varied. Reducing the number of design variables to only two allowed an analysis of the sensitivity of the SCF to certain thin reinforcement geometries.

A. METHOD OF INVESTIGATION

To investigate the effects of co-cured reinforcement around cutouts, linear elastic finite element analysis (LEFEA) was employed to determine the strain field in each panel configuration. Plots were drawn of the strains existing on a line from the point of highest stress concentration at the cutout across the middle of the panel (the X axis) and around the cutout and contours of the three inplane strain fields (Y, X, and shear). These are included as figures in the appendices for each geometry. Specimens of each configuration were manufactured, instrumented with strain gages and finally loaded in compression to failure. The analytical and experimental results were compared and the failure mode of each panel evaluated.

Total failure, in this report, is assumed to be facesheet delamination, separation and buckling with massive fiber failure

such that the panel could not withstand a full reversal of the load. Partial failure was facesheet delamination and separation without the massive fiber failure and infers that there could be significant tensile strength remaining.

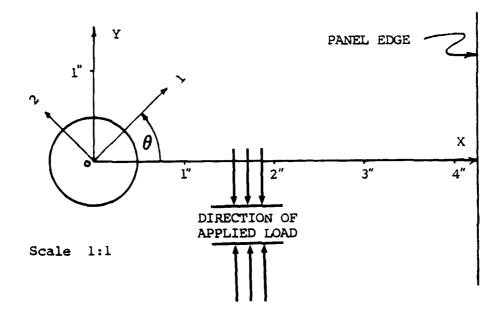
B. COORDINATE SYSTEM

There are several different right-hand coordinate systems that have been used in the analysis of laminated materials. Analysis is, of course, independent of the the system used, but more than one student has lost his way attempting to compare methods or results expressed in different systems by various recognized authorities in the field.

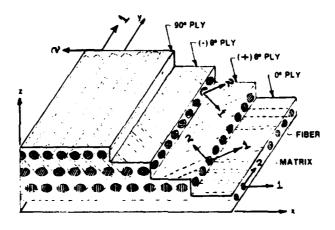
The data presented in this report is based in a cartesian system with the plane of the laminated panel aligned in the X-Y plane. Individual ply orientations are considered to be rotated counter-clockwise from the X axis an angle of theta (θ) degrees. These plies in the layup are assigned a local orthogonal coordinate system designated the 1-2 axes. The laxis, also referred to as the principal axis, is considered to be in the fiber direction with the highest elastic modulus (E_1).

Figure 2.1 shows the upper right quadrant of a typical panel in the X-Y (global) coordinate system as well as the ply 1-2 (local) coordinates. This coordinate system was used by R.M. Jones in Mechanics of Composite Materials and Ashton, Halpin, and Petit [Ref. 23]. Tsai and Hahn [Ref. 24] chose instead to fix the X-Y axes to the ply and the 1-2 axes to the panel. The principal researchers in the field do not use the same system.

The panel is oriented so that the area of greatest interest, a horizontal plane bisecting the circular cutout, is aligned with the X axis, where $y \approx 0.0$ ". The origin is assigned to the center



Panel Coordinate System (X-Y)



Ply Coordinate System (1-2)

Figure 2.1 Panel and Ply Coordinate Systems.

of the circular cutout. The compressive load is applied to the panel 90° to this plane, parallel to the Y axis, and referred to as $\overline{\sigma}_n$. The 2 axis is centered at the midplane of the panel and extends through the thickness toward the viewer, completing a right-hand coordinate system.

C. SELECTION OF TEST SPECIMEN CONFIGURATION

The dimensions of the test specimens were chosen to approximate, at least in order of magnitude, a typical honeycomb panel with a cutout found in many aerospace applications. The overall size was limited by the size of the test machine and compression test frame.

Hong and Crews [Ref. 25], among others, demonstrated that the stress concentration in orthotropic composites under uniaxial loading was dependent on the ratio of hole diameter to panel width (d/w). Whitney and Nuismer [Refs. 26 & 27] pointed out that the absolute hole size had a significant effect on the stress gradient and ultimate strength when the hole diameter (d) was less than 1.0 inch.

The cutout's 1.00 inch diameter was chosen, therefore, to limit, as much as possible, hole-size effects. The panel was then designed as large as practical to reduce the effect of finite panel dimensions and still fit into the test frame and machine. Hole-size and finite-width effects are addressed in more detail in Section II.D.3. The specimen size, 10.00" x 8.50", gave a diameter-to-width ratio (d/w) of 0.118 and a diameter-to-length ratio (d/l) of 0.100. A comparison is made in Section III.C.3 between the solutions for finite and infinite plates of otherwise equal thickness and material constants.

A fabric G/Ep prepreg material was chosen because it has been somewhat less studied than tape and because it is finding increased use in airframe construction. The cured fabric laminate has slightly less in-plane stiffness and strength per unit thickness than uniaxial tape made from identical fibers. This is due to the nature of the weave, where the fibers (or tows) are cured with "crimps" rather than straight. Fabric has, however, demonstrated significant advantages over tape in its damage tolerance [Ref. 28] and ease of manufacture [Ref. 29].

Graphite/epoxy unidirectional tape can be most effectively applied in flat or slightly curved structures such as wings and access panels. Fabric, on the other hand, lends itself to applications requiring high curvature or complex shapes. Tape cannot be used in small inside or outside radius applications without fiber separation, inducing matrix-rich/fiber-poor areas and suffering severe loss of strength.

HMF330C/34 fabric G/Ep manufactured by Fiberite Inc. was chosen because it is a high modulus fabric, using Thornel T300 graphite fibers, found in many aerospace applications. It is an eight harness satin (8HS) weave cloth which minimizes the number of fiber crimps while maintaining many of the desirable characteristics of cloth. Figure 2.2 illustrates some details of its weave.

1. Panel Reinforcement Configuration

Reinforcement of the panel cutout was of three general types: round, square, and strip. The round and square were concentric with the hole, the "stiffening" strips were centered 0.750 incn away from the hole edge, parallel to the applied load. Table I lists the panel designations, reinforcement geometries and amounts; Figure 2.3 shows representative configurations.

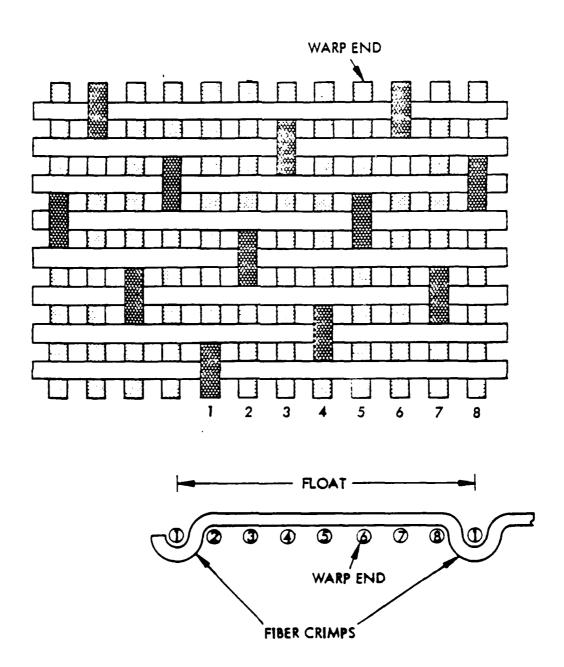


Figure 2.2 8 Harness Satin (8HS) Weave Cloth.

The basic panel was a quasi-isotropic eight ply (nine separate layers including the core) G/Ep panel. For more simple comparison, the amount of reinforcement was normalized by the amount of G/Ep removed from the 1.00 inch diameter cutout in the facesheets of the unreinforced panel. The relative volume of the reinforcement ply(s) was determined from this volume (0.088 in³) of G/Ep. The round and strip reinforced panels had 5 increments of 100% of the removed reinforcement volume and the square reinforcement had increments of 100, 300 and 500%. The 200% and 400% reinforcements were each two plies thick.

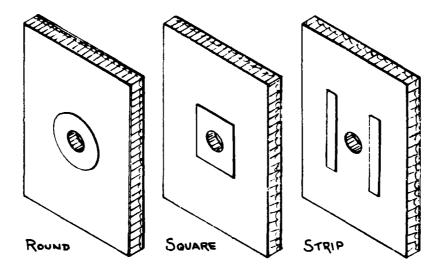


Figure 2.3 Panel Reinforcement Configurations.

The panel designation was devised to be somewhat descriptive of the test specimen. The first letter, P or R, refers to either a plain (unreinforced) or reinforced configuration, respectively. The second letter indicates the type of reinforcement: none (O), round (R), square (S) or strip (H); X indicates no hole was present. The first numeral represents the normalized percent

of reinforcement, 1 to 5 for 100% to 500% (Ø indicates no reinforcement). The second numeral is the number of reinforcing plies on each facesheet. For example, RH42 is a reinforced panel with four times the removed hole volume (0.352 in³) arranged in a strip configuration, 2 plies thick on each facesheet.

TABLE I
TEST SPECIMEN MATRIX

		=========					
	Reinforcement						
Panel	Туре	Normalized	Ply(s) per				
Designation		Volume (%)	Facesheet				
PXØØ	No cuto	out or reinf	orcement				
POØØ	None	0	0				
RR11	Round	100	1				
RR22	Round	200	2				
RR31	Round	300	1				
RR42	Round	400	2				
RR51	Round	500	1				
RS11	Square	100	1				
RS31	Square	300	1				
RS51	Square	500	1				
RH11	Strip	100	1				
RH22	Strip	200	2				
RH31	Strip	300	1				
RH42	Strip	400	2				
RH51	Strip	500	1				

Figure 2.4 shows a typical laminate cross-section from the midplane. Each panel was symmetric about all three axes. Exceptional care was required and taken during the manufacturing process to ensure that the reinforcement plies were placed directly opposite each other on the opposing facesheets. When

measured, no reinforcement was more than 0.05" off center; the average was less than 0.02".

D. SOME CHARACTERISTICS OF NOTCHED GRAPHITE/EPOXY PLATES

The characteristics of composite materials differ radically from those of the metals they replace. As previously noted, composite fibers, particularly G/Ep, are by nature very brittle. Tensile failures in composite plates with cutouts are, almost without exception, load dependent. [Refs. 20-22]

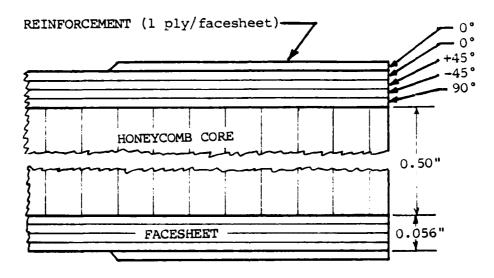


Figure 2.4 Typical Laminate Cross-Section.

Compressive failure, the type dealt with here, is more dependent on the type and thickness of the laminate, the use of honeycomb to overcome the tendency to buckle, the size of cutouts and the presence of imperfections. The compressive failure modes tend to be complex, composed of one or more types of failure: stability, ply delamination, matrix cracking, etc. Stability failure is principally the buckling of either fibers within the matrix (micro-mechanical) or the structure itself (macro-mechanical). These test specimens and the frame were designed to

preclude macro-mechanical buckling (in the Euler column mode) since little would be learned about the reinforcement effects and this type of failure has been well documented beginning with Levy, Woolley and Kroll [Ref. 5].

1. Stress Concentration due to Notch Effects

It is well known that notches and cutouts in plates act as stress risers. For circular holes in plane elastic isotropic infinite plates under uniaxial tension or compression, the stress at the hole edge 90° to the applied load will be exactly three times the far-field stress. The distribution of stress around the hole edge and the stress field around it can be predicted using Airy's stress function. Dally and Riley [Ref. 30: pp. 67-83] give a clear and concise derivation of the stress field equations which will not be repeated here.

2. Orthotropic Effects on Stress Distribution

When an orthotropic plate with a stress riser is loaded, the SCF depends on the degree of orthotropy, that is, how much the elastic modulii change with radial direction. This is sometimes referred to, not always correctly, as the ratio of E_1/E_t . The subscripts "1" and "t" refer to the effective lateral and transverse modulii where the lateral direction is parallel to the applied load and transverse is 90° to it. In the coordinate system used in this report, the load is applied parallel to the Y axis and the ratio is expressed as: E_y/E_x . Note that a ratio of 1.0 does not ensure isotropy; it must be accompanied by the appropriate shear modulus (G_{xy}) and Poisson's ratio (v_{xy}) . For a circular hole in an infinite-width plane orthotropic plate, the stress concentration K_∞ on the cutout edge 90° to the applied load was given by Nuismer and Whitney [Ref. 27: Eqn. 3] as:

$$K = 1 + \sqrt{2(\sqrt{E_1/E_t} - \nu_{1t}) + E_1/G_{1t}}. \qquad (2.1)$$

In an idealized infinite laminated plate, this equation must be equally valid in both tension and compression. This stress concentration factor (K) may be considered a far better indication of the orthotropy of a material than the ratio E_1/E_+ .

The distribution of stress in the Y direction along the X axis ($\sigma_{Y}(x,0)$) due to an applied (far-field) normal stress ($\overline{\sigma}_{n}$) may be approximated using the following equation:

$$\sigma_{Y}(x,0) = [(\overline{\sigma}_{n}/2)(2+b^{2}+3b^{4}-(K-3)(5b^{5}-7b^{8})],$$
 (2.2a)

where:

$$b = a/(x-d/2)$$
 and $x > d/2$. (2.2b)

The variable "d" is the diameter of the circular cutout and "x" is a location along the X axis (y = 0.0") when the coordinate system is concentric with the hole. This relationship is a quite accurate polynomial approximation developed by Konish and Whitney [Ref. 31].

3. Effects of Finite Plate Width and Hole Size on SCF
Compared to infinite plate width under uniaxial stress,
finite plate width acts to increase the SCF. This fact becomes
obvious in plates with a high d/w ratio. The applied stress must
be carried by a greatly reduced net cross-section. The increase
in SCF is due more to the net section effect than the presence of
the cutout. Peterson [Ref. 32: pp. 110-111] gives the following
equation to approximate the SCF at the edge of an unreinforced
circular cutout in a finite-width isotropic plate:

$$K_f = [2 + (1-(d/w)^3)]/[1-(d/w)]$$
 (2.3a)

This can be extended to an orthotropic plate where K_{∞} does not equal exactly three using:

$$K_f = (K_m/3) 2 + [1 - (d/w)^3] / [1 - (d/w)]$$
 (2.3b)

The test specimens used in this report had a d/w ratio of 0.118; K_f was then calculated to be 3.045 for the unreinforced, quasi-isotropic panel POØØ. At $\overline{\sigma}_n = -10.0$ ksi this would theoretically make the maximum stress -30,450 psi at the $\theta = 0^\circ$ position on the cutout (90° to the applied load) compared with 30,000 psi predicted for an infinitely wide plate. This is an increase of 1.5%. Thus panel width has little more than a negligible effect on the SCF of the test specimens in this report.

Further data that relate a plate's dimensions to its SCF are given by Hong and Crews [Ref. 25: pp. 8-10]. They calculated stress concentration factors in finite-width orthotropic plates under uniaxial loads using finite element analysis. They used a different definition of SCF, one based on the net cross-sectional area stress concentration ($K_{\rm net}$). This report uses the SCF based on far-field stress or the gross SCF ($K_{\rm gross}$). The two are related by the equation:

$$K_{gross} = K_{net}/[1-(d/w)].$$
 (2.4)

To make valid comparisons with SCF data presented in this report selected results of Hong and Crews' analysis, converted from K_{net} to K_{gross} , are listed in Table II.

Their results show that quasi-isotropic layups ([0,±45,90]_s) give results very close to the theoretical isotropic values. Greater orthotropy in the load direction results in a correspondingly greater SCF. It is interesting to note that the

ratio of length to width (1/w) has an increasing effect on the SCF as the ratio d/w increases.

Nuismer and Whitney [Ref. 27: p. 118] point out the effect of absolute hole size on panel failure: ". . attention was called to a phenomenon that since became known as the 'hole size effect,' that is, for tension specimens containing various sized circular cutouts, larger holes cause greater strength reductions than do smaller holes." They state that the classical stress concentration approach does not explain such an effect and they go on to propose that while the stress concentration factor is the same, the distribution and gradient near the hole is different. Figure 2.5 reproduced from Ref. 27 illustrates this point.

4. Failure Stress Criteria

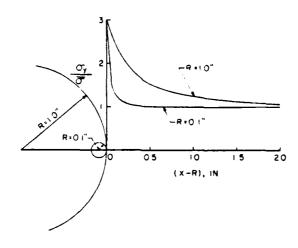
As previously noted, the SCF does not explain the "hole size effect" on failure. Nuismer and Whitney rejected linear elastic fracture mechanics (LEFM) to explain the inverse relationship between hole size and strength. They noted that while all circular holes in infinite width plates should have the same theoretical SCF, the distribution in fact changes with hole radius. The smaller the hole the more concentrated the stress near the edge appears [Ref. 27: p. 118]. Nuismer and Whitney proposed that when the notched stress (\mathbf{C}_N) reached an average value of $\mathbf{C}_{U,ult}$, the unnotched ultimate stress over some characteristic distance as, that the panel's ultimate strength had been reached and failure resulted. This characteristic distance as must be arrived at by testing a statistically significant number of panels. This distance as is defined:

$$\frac{1}{a_{\bullet}} \int_{0}^{a_{\bullet}} \boldsymbol{\sigma}_{y}(x,0) dx = \boldsymbol{\sigma}_{U}, \text{ult}$$
 (2.5)

TABLE II $\mbox{STRESS CONCENTRATION FACTORS-} \mbox{K}_{\mbox{gross}} \mbox{ (HONG & CREWS)}$

		======	===	=======	======	======	======	=====
				Diameter-to-Width			Ratio:	d/w
Layup	$\mathrm{E_{l}/E_{t}}$	K L	/w	0.05	0.10	0.33	0.50	0.67
[0,±45,90] _s	1.00	3.00	1	3.00	2.74	3.33	4.02	5.76
[0,±45,90] _s	1.00	3.00	2	3.01	3.03	3.49	4.36	6.36
[90]	0.07	2.48	1	2.48	2.51	2.97	3.78	5.61
[90]	0.07	2.48	2	2.48	2.51	2.97	3.78	5.88
[±45] _s *	1.00	2.06	1	2.88	2.93	3.38	3.84	5.16
[±45] _s *	1.00	2.06	2	2.88	2.92	3.36	3.80	5.28
[0,90] _s *	1.00	3.78	1	4.78	4.69	5.61	5.08	6 . 93
[0,90] _s *	1.00	3.78	2	4.82	4.84	5.22	6.06	8.16
Eo:	13.49	5.43	1	6.36	6.07	5.24	5.82	8.01
[0]	13.49	5.43	2	6.44	6.44	6.54	7.30	9.54

Indicates an E_1/E_t ratio of 1.00, but not a quasi-isotropic laminate.



(Reproduced from Reference 27)

Figure 2.5 Hole Size Effect on Normal Stress Distribution

The ratio of notched to unnotched ultimate strength $(\boldsymbol{\sigma}_n/\boldsymbol{\sigma}_u)_{ult}$ for infinite plates is:

$$\sigma_n/\sigma_u = 2(1-\xi)/[2-\xi^2-\xi^4+(K_\infty-3)(\xi^6-\xi^8)]$$
 (2.6a) where:

$$\xi = d/(d/2 + a_0)$$
 and $x > a_0$. (2.6b)

Nuismer and Labor [Ref. 33: p. 55] determined that for AS/3501-5 G/Ep (tape) in compression this characteristic length was 6.2 mm (0.24"). They also note that the characteristic length for tape in tension was only 2.3 mm (0.091"). Test data provided by LMSC indicates that for HMF330C/34 fabric G/Ep this characteristic length is close to 7.3 mm (0.33") in compression.

Isotropic materials may be modeled using classical plate theory neglecting out-of-plane stresses (±z in this coordinate system). Orthotropic materials, however, develop complex interlaminar stress fields near the edge of a cutout. The subject has received much theoretical attention [Refs. 34 through 36]. Tang [Ref. 34: p. 1631] states that "... radial and shear stresses of each layer along the contour of the hole are in general not zero because there exists a three-dimensional state of stress at the free edge of each layer which the plane stress solution cannot predict." Greszczuk [Ref. 9: p. 372] pointed out that "In orthotropic and anisotropic plates containing openings, the failure will take place not as a result of stress concentration, but rather as a result of interaction of various stress components."

Under uniaxial compressive loading the laminate will have a Poisson expansion induced out-of-plane tensile stress (σ_z) which is highest at the hole's edge at point of the greatest

stress concentration. This stress is added to any local stress due to machining and imperfections and combined tend to hasten delamination and the ultimate failure. In the experimental results reported here it was not possible to effectively quantify the effect on failure of this out-of-plane stress.

III. COMPUTATIONAL ANALYSIS

Before an experimental program could be developed, it was necessary to understand and be able to analyze the strain field resulting from a cutout in a representative panel and to be able to predict the reaction of test specimens to an applied compressive load. Three analysis methods were used: classical laminate theory, the linear elastic stress function and linear elastic finite element analysis (LEFEA).

Laminate analysis provides the basic stress-strain relation at a point, once the material properties of each constituent ply are specified. The stress function was used to predict the theoretical stress-strain fields in an infinite unreinforced orthotropic elastic plate with a circular cutout. These two can be solved in closed-form and require relatively little computation time using modern computers. The finite element method allows detailed analysis of reinforced finite-width reinforced panels, but requires a significant allocation of computer resources for an accurate representation of the strain field.

There are several coordinate systems and notations in general use in laminate analysis. The following section presents the method used in this report, explicitly defines the notation and gives justification for some of the assumptions that were made.

A. LAMINATE THEORY AND ANALYSIS

Laminate theory seeks to predict the properties of a multidirectional composite laminate based on the properties and orientation of its constituent lamina. Individual laminae are usually either unidirectional (tape) or woven (cloth) fibers embedded in a polymer matrix (generally a thermoset resin whose molecules are linked in three dimensions and which exhibits elastic properties in normal use) and tend to have strongly directional properties. The theory assumes that the state of stress is plane, displacements are small compared to laminate thickness and that strain is much smaller than unity.

Pipes [Ref. 37: pp. 4-1, 5-1] presented the micro- and macro-mechanical models that are the basis of the theory. An anisotro-pic material's elastic response at a point to applied stresses may be defined using generalized Hooke's Law. The constitutive relation is Equation 3.1, where σ_{ij} and ε_{kl} are the components of the stress and strain tensors and c_{ijkl} is the tensor of elastic constants. Using this most general of equations there are 3^4 or 81 material constants.

$$\sigma_{ij} = \sum_{k=1}^{3} \sum_{l=1}^{3} c_{ijkl} \epsilon_{kl}$$
 (3.1)

This equation may be greatly simplified using the symmetry of stress and strain and the requirement that the strain energy density function be positive definite [Love, Ref. 38: pp. 97-111 and Feynman, Ref. 39: v. 2, ch. 31-7] reducing the independent elastic constants from 81 to 21. Symmetry reduces both σ_{ij} and ϵ_{kl} from nine to six different values. Feynman explains that the elastic response of a crystal with no symmetry in the three axes can be completely defined using 21 independent coefficients. The notation can be contracted using the following convention where the index: i = 1, 2, 3:

$$\sigma_{ii} = \sigma_{i}$$
 $\sigma_{23} = \sigma_{4}$ $\sigma_{13} = \sigma_{5}$ $\sigma_{12} = \sigma_{6}$ $\varepsilon_{1i} = \varepsilon_{i}$ $\varepsilon_{23} = \varepsilon_{4}$ $\varepsilon_{13} = \varepsilon_{5}$ $\varepsilon_{12} = \varepsilon_{6}$ (3.2)

The constitutive relation can now be expressed as:

$$\sigma_{i} = \sum_{j=1}^{6} c_{ij} \epsilon_{j}. \qquad (3.3)$$

This is a sixth-order symmetric matrix (where $C_{ij} = C_{ji}$).

Idealized thin laminate theory neglects stress and strain in the ±z direction; the equations are reduced to plane strain and stress, further contracting the elastic constant tensor to a third-order symmetric matrix. In orthotropic systems (axes at right angles to each other) the "l" direction is the principal fiber direction (or the direction with the highest elastic modulus), "2" is 90° to it and "6" is the shear in the 1-2 plane.

$$\sigma_{i} = \sum_{j=1,2,6} Q_{ij} \boldsymbol{\epsilon}_{j}. \tag{3.4}$$

The matrix [Q] is termed the reduced laminate stiffness matrix, is symmetric and is related to [C] by:

$$Q_{ij} = C_{ij} - \frac{C_{i3} C_{j3}}{C_{33}}$$
 (i, j = 1,2,6) (3.5)

The matrix [Q] may be expressed explicitly in terms of modulii and Poisson's ratios:

$$Q_{11} = \frac{E_1}{1 - \nu_{12} \nu_{21}} \qquad Q_{12} = \frac{\nu_{12} E_2}{1 - \nu_{12} \nu_{21}} \qquad (3.6)$$

$$Q_{22} = \frac{E_2}{1 - \nu_{12} \nu_{21}} \qquad Q_{21} = Q_{12} = 0 Q_{16} = Q_{61} = 0 Q_{66} = G_{12} \qquad Q_{26} = Q_{62} = 0$$
(3.6)

To determine the ply's elastic response defined in the laminate coordinate system (X-Y), both the stress and strain vectors must be rotated an angle θ about the "3" axis (Note: the "3" and Z axes are colocated):

$$\sigma'_{i} = \sum_{j=1,2,6} T_{\sigma_{ij}} \sigma_{j}$$
 (i = x,y,xy) (3.7)

$$E'_{i} = \sum_{j=1,2,6} T_{e_{ij}} E_{j}$$
 (i = x,y,xy) (3.8)

The transform matrix $[T_{\sigma}]$ (for the case of stress) is derived from the trigonometric relations:

$$T_{\sigma ij} = \begin{bmatrix} m^2 & n^2 & 2mn \\ n^2 & m^2 & -2mn \\ -mn & mn & m^2-n^2 \end{bmatrix}$$
 $m = \cos$ (3.9)

Recall that engineering shear strain (γ_{\circ}) differs from tensorial shear strain (ϵ_{6}) by a factor of 2: $\epsilon_{6} = 2\gamma_{6}$. The strain transform matrix elements $T_{\epsilon 16}$ and $T_{\epsilon 26}$ become man and $T_{\epsilon 61}$ and $T_{\epsilon 62}$ become 2mm. Using matrix algebra, the now transformed reduced laminate stiffness matrix [Q'] can be expressed in matrix form as:

$$[Q'] = [T_{\sigma}] [Q] [T_{\epsilon}]^{-1}$$
(3.10)

A laminate is built from the stacking of a number of these rotated plies. The designer may easily tailor the laminate using various ply thicknesses and orientations.

The integration of each ply's [Q'] matrix through the laminate thickness (h) gives the normalized inplane stiffness matrix:

$$[A] = \int_{-h/2}^{h/2} [Q'] dz$$
 (3.11)

Stress and moment resultants are defined by integrating stress through the laminate thickness:

$$\{N\} = \int_{-h/2}^{h/2} \{\mathbf{\sigma}\} dz \qquad (3.12)$$

$$\{M\} = \int_{-h/2}^{h/2} \{\mathbf{O}\} z dz.$$
 (3.13)

The stress resultant vector $\{N\}$ is related to the strain vector $\{\mathcal{E}\}$ by the laminate inplane stiffness matrix [A] in equation 3.14:

$$\begin{pmatrix}
\mathbf{N}_{\mathbf{X}} \\
\mathbf{N}_{\mathbf{Y}} \\
\mathbf{N}_{\mathbf{X}\mathbf{Y}}
\end{pmatrix} = \begin{bmatrix}
\mathbf{A}_{11} & \mathbf{A}_{12} & \mathbf{A}_{16} \\
\mathbf{A}_{21} & \mathbf{A}_{22} & \mathbf{A}_{26} \\
\mathbf{A}_{61} & \mathbf{A}_{62} & \mathbf{A}_{66}
\end{bmatrix} \begin{pmatrix}
\boldsymbol{\epsilon}_{\mathbf{X}} \\
\boldsymbol{\epsilon}_{\mathbf{Y}} \\
\boldsymbol{\epsilon}_{\mathbf{X}\mathbf{Y}}
\end{pmatrix} (3.14)$$

The laminate, while thin, demonstrates resistance to bending governed by the ply stiffness and the square of the distance from

the midplane $(\pm z)^2$. Integrating through the laminate's thickness:

$$[D] = \int_{-h/2}^{h/2} [Q'] z^2 dz.$$
 (3.15)

Laminates with unsymmetric layups (where opposing plies at ±z do not have identical thickness, properties and principal axis orientation) exhibit coupling between strain and curvature (k). This follows since each side of the midplane exhibits different material properties. Any applied inplane stress will induce some curvature. The bending-extension coupling matrix [B] is:

[B] =
$$\int_{-h/2}^{h/2} [Q'] z dz$$
 (3.16)

It follows, therefore, that in perfectly symmetric laminates [B] must evaluate to zero.

The combined bending-extension properties of a laminated plate can be expressed as a sixth-order symmetric matrix which relates stress and moment resultants to strain and curvature:

1. Laminate Properties

LMSC provided the initial data on material properties of cured HMF330C/34 G/Ep fabric. In order to validate it for this program, a solid panel (PX \not 0), one without the 1.00 inch cutout, was manufactured and tested. The laminate material properties

required slight revision (less than 4%) to match the the actual response of the solid panels to loading. These results are discussed in detail in Section V.B.l. The [0,±45,90,core]_s solid laminate exhibited different modulii in tension and compression. In addition, it exhibited a slightly nonlinear stress-strain curve in compression (see Table VI and Figure 5.4). The elastic modulus parallel to the applied load (principal modulus, E_y) varied from 7.8 to 6.5*10⁶ psi as the applied load varied from 0 to panel failure at -57 ksi; as the load increased the panel stiffness monotonically decreased. This characteristic is most probably due to the woven plies (Figure 2.2) compressing within the elastic matrix, but it was not further investigated.

The finite elements chosen for this analysis assumed linear elastic material properties. Nonlinear analysis was possible using different elements, but would have yielded little more accuracy at a tremendous increase in computation time. At an applied far-field stress $(\overline{\sigma}_n)$ of -10.0 ksi the stress induced in an unreinforced quasi-isotropic panel with a cutout varies from -10 to -30 ksi and thus E_y would vary from 7.46 to about 6.95 msi. Since the compressive stress field and thus the material properties vary continuously over a panel with a cutout, it became necessary to select one principal modulus, indeed, all the material constants $(E_1, E_2, G_{12}, \nu_{12})$ and ν_{21} for use in the FEA. The material properties listed in Table III are valid (at 70°F) throughout the range of tension but in compression they are exact only at -15 ksi; for other values they are approximate but introduce only a small error.

Jones [Ref. 40: pp. 16-21] discussed the bimodulus phenomenon and proposed an improved analysis method he called the

TABLE III

MATERIAL PROPERTIES OF HMF330C/34 CLOTH G/EP

Tension	E 1:	10.9×10^6 psi E_2 : 10.3×10^6 psi
Compression	E ₁ :	10.2×10^6 psi E_2 : 9.6×10^6 psi
Shear	G ₁₂ :	1.0x10 ⁶ psi
Poisson ratio	v_{12} :	0.09 v ₂₁ : 0.09
Thickness	t:	0. 014 inch (fully cured ply)

TABLE IV

LAMINATE STRESS RESULTANT AND MOMENT PROPERTIES (COMPRESSION)

***************************************		******
	A MATRIX	
8.876E+05 2.212E+05 1.362E-01	2.212E+05 8.876E+05 -1.467E-01	1.362E-01 -1.467E-01 3.334E+05
	B MATRIX	
6.250E-02 0.0 1.221E-04	0.0 6.250E-02 1.221E-04	1.221E-04 1.221E-04 5.078E-02
	D MATRIX	
6.907E+04 1.711E+04 3.270E+01	1.711E+04 6.868E+04 3.268E+01	3.270E+01 3.268E+01 2.580E+04

weighted compliance matrix. If a more complete analysis is required, this model should be considered.

The bending-extension matrices (Eqn. 3.17) were calculated using conventional thin laminate analysis (based on experimentally derived material properties) for the HMF330C/34 [0,±45,90,core]_S laminate in compression. The results (the [A], [B] and [D] matrices) are listed in Table IV.

The symmetry of the basic laminate is apparent from the magnitude of the [B] matrix particularly in relation to [A] and [D]. The reinforced laminate also had [B] = 0 since it was symmetric. The very small relative values of the elements of the [B] matrix (as well as elements A_{31} , A_{32} , A_{13} and A_{23}) are more due to round-off error in the computer, using single precision numbers, than an indication of an unsymmetric layup.

Pipes [Ref. 37: pp. 5-4] notes that when analyzing composite laminates it is often more convenient to treat them as homogeneous plates. For symmetric laminates it is possible to express orthotropic material constants in terms of the inplane stiffness matrix [A]. The laminate material properties may be determined in the X-Y plane from [A] using equations 3.18 through 3.22.

$$E_x = (A_{11} * A_{22} - A_{12}^2)/(h * A_{22})$$
 (3.18)

$$E_y = (A_{11} * A_{22} - A_{12}^2)/(h * A_{11})$$
 (3.19)

$$\nu_{xy} = A_{11}/A_{22}$$
 (3.20)

$$\nu_{yx} = A_{12}/A_{11}$$
 (3.21)

$$G_{yx} = A_{66}/h$$
 (3.22)

Table V lists the (experimentally derived) panel material properties at -15.0 ksi. For the purpose of linear elastic analysis these are assumed to be constant over the stress field for the particular laminate at any load. When these modulii were used in the finite element analysis ($\overline{\sigma}_n = -10.0$ ksi) the maximum error in strain at any point in the field was less than $\pm 3\%$.

B. LINEAR ELASTIC STRESS FIELD SOLUTION

Savin [Ref 7: Chapt. II] gives a solution for the stress distribution in various anisotropic plates and beams with cutouts. Garbo and Ogonowski [Refs. 8 and 41] coded the solutions in FORTRAN for the case of a for the case of a thin, infinite-width orthotropic plate with a circular cutout. Their program, revised by the author for the IBM 370, is listed in Appendix P.

TABLE V
MATERIAL PROPERTIES OF THE LAMINATES

	-2-22		:======	=======		332333
Layup	Plies	$\mathbf{E}_{\mathbf{x}}$	Ey	^G xy	$ u_{xy} $	SCF
[0,±45,90,c] _s	8	7.28	7.28	2.78	0.321	3.00
[0 ₂ ,±45,90,c] _s	10	7.94	7.79	2.40	0.269	3.19
[0 ₃ ,±45,90,0] _s	12	8.36	8.11	2.17	0.236	3.33
	(Mo	odulii *	10 ⁶ psi)			

Note: The 0.50" thick honeycomb core (\overline{c}) had no effect on the inplane modulii. The panel had an 8 ply layup except under the reinforcement. The 10 and 12 ply layup gives the material properties under the one and two ply reinforcement.

The general biharmonic equation for an orthotropic material is given in Equation 3.24. The S coefficients are members of the third order laminate compliance matrix [S], the inverse of [A]:

$$\{\boldsymbol{\epsilon}\} = [S] \{N\}$$
 (3.23)

$$s_{22} \frac{\partial^{4} F}{\partial x^{4}} - 2s_{26} \frac{\partial^{4} F}{\partial x^{3} \partial y} + (2s_{12} + s_{66}) \frac{\partial^{4} F}{\partial x^{2} \partial y^{2}}$$
$$- 2s_{26} \frac{\partial^{4} F}{\partial x \partial y^{3}} + s_{11} \frac{\partial^{4} F}{\partial y^{4}} = 0$$
(3.24)

Based on the original research by Savin [Ref. 7], Garbo and Ogonowski point out that the stress function F depends upon the roots of the associated characteristic equation:

$$F = 2Re[F_1(Z_1) + F_2(Z_2)].$$
 (3.25)

 $F_1(Z_1)$ and $F_2(Z_2)$ are the analytic functions of the complex variables $Z_1 = X + R_1 Y$ and $Z_2 = X + R_2 Y$ where R_1 and R_2 are the complex roots of the characteristic equation. The expressions for the three inplane stresses are:

$$\sigma_{x} = 2\text{Re}[R_{1}^{2}\phi_{1}'(z_{1}) + R_{2}^{2}\phi_{2}'(z_{2})]$$
 (3.26)

$$\sigma_{y} = 2 \text{Re}[\phi_{1}(z_{1}) + \phi_{2}(z_{2})]$$
 (3.27)

$$\sigma_{xy} = -2Re[R_1 \phi_1^*(Z_1) + R_2 \phi_2^*(Z_2)]$$
 (3.28)

The functions $\phi_1(\mathbf{z}_1)$ and $\phi_2(\mathbf{z}_2)$ are defined:

$$\phi_1(z_1) = \frac{\partial F(z_1)}{\partial z_1} \qquad \phi_2(z_2) = \frac{\partial F(z_2)}{\partial z_2} \qquad (3.29)$$

These equations have been slightly modified from their original form in order to apply in this report where there is no internal load on the hole. For a full development and explanation

of the equations, the reader should refer to Garbo [Ref. 41: p. 586] or Savin [Ref. 7].

C. FINITE ELEMENT ANALYSIS

Finite-width and reinforcement effects cannot be addressed using these two methods because of the discontinuities in thickness and material properties at the edge of the reinforcement. Finite element analysis has demonstrated its ability to accurately analyze the majority of problems in elasticity. The quality of the solution is, however, dependent on the size of both the available computer core memory and the analysis budget, since the quality and cost of the solution are functions of the fineness of the element mesh. The solution time and cost increase at least with the cube of the degrees of nodal freedom (DOF) in the model [Ref. 42: pp. 391-402]. In a full three-dimensional analysis each element node point may be displaced in the X, Y and Z directions and also rotated about each of the three axes. Thus there are six possible DOF per node: three displacements and three rotations. The dimension of the stiffness matrix is the sum of the degrees of freedom at each node point in the model.

The structural finite element analysis method, in its simplest form, is the determination of the relationship between the load on and the displacements in a body. The two are related by the stiffness characteristics of the body. The body is divided into a number of smaller volumes (or areas) termed elements, each element is then assigned a local "stiffness" and these are then combined in matrix form to establish their inter-relation. The result is termed the stiffness matrix [K]. Each element is made up of nodes at its corner points which can be fixed, at which a force can act and which can deflect if not fixed. The vector of forces {F}

acting on each node equals the product of [K] and the vector of deflections $\{\delta\}$.

$$\{F\} = [K]\{\delta\} \tag{3.30}$$

Since the forces are generally known and it is the displacements which are desired, the stiffness matrix must be inverted:

$$\{\delta\} = [K]^{-1}\{F\} \tag{3.31}$$

The order of the [K] matrix is determined by the sum of nodal degrees of freedom. The matrix inversion to [K]⁻¹ is not a trivial computational task in any realistic finite element model.

The art in FEA is in defining a mesh fine enough to give adequate solution accuracy while suppressing as many DOF as possible to keep the cost of solution within reason. Zienkiewicz, in his excellent text on the subject [Ref. 43], covers this method of structural analysis in some depth.

1. DIAL finite Element Program

A finite element analysis program named DIAL as well as a significant allocation of computer time on a Digital Equipment Corporation VAX 11/780 was made available by LMSC for this research. DIAL is a flexible, general purpose finite element code for the analysis of two- and three-dimensional structures. It has a modular architecture in which individual subprograms are executed as the model is being defined, the mesh generated, the equation bandwidth optimized and the solution found. As each subprogram (called a "processor") is executed, it extracts required data from a data base, processes it, updates the solution and adds to the data base. This architecture provides an invaluable restart capability at the last successful process which

				_						
252	263	254	265	266	267	268	259	270 	27:	272
251	252	253	254	25 5	256	257	259	253	260	261
240	241	242	243	244	245	246	247	248	249	250
229	230	231	232	233	234	235	236	237	239	239
2:9	219	225	221	222	223	224	225	225	227	228
237	205	209	215	21:	212	2:3	214	215	215	217
196	197	198	. 39	200	201	202	203	204	205	206
185	:85	187	188	189	190	191	192	:93	194	195
:74	175	:76	177	175	:79	180	191	182	193	. iō÷
163	184	165	165	167	168	169	170	171	172	173
:52	:53	:54	155	:5€	157	:58	159	:::0	151	162
141	142	:43	144	145	146	:47	148	149	150	151
3: /	3. 32 93 94 105 106					:36	137	. 38	: 133	: 4C
71 -2	95 96 127 74 95					130	131	132	133	134
53 54 75 86 97 108					123	124	125	:25	: :27	129
		57 57 58 58	\	109	117	:18	:19	:40	121	. 22
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Figure 3.1 Typical Finite Element Mesh

can significantly conserve analysis time [Ref. 44]. The following DIAL processors were used in the linear elastic analysis of the experimental test panels:

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- MESH The geometric grid of elements to be analyzed, called a mesh, is generated by specifying points coincident with the quadralateral element corner nodes in an orthogonal I-J coordinate system. Certain points key in the I-J system are then givenlocations in the X-Y plane and the MESH processor automatically maps appropriately shaped elements. Figure 3.1 show a typical element mesh. The processor allows partial meshes to be generated individually and then merged to each other creating a larger model. The heavy lines in Figure 3.1 outline these. Building a complete FEA model from a series of smaller partial meshes reduces the manhours required to generate the model and allows more complex geometry. Merging adjacent partial meshes eliminates any redundant nodes and degrees of freedom. The panel models for this analysis used from three to five partial meshes. Boundary conditions are specified and DOF suppressed within the MESH processor to adequately simulate the structure.
- * BAND It is not necessary to store the entire finite element stiffness matrix; the Betti-Maxwell reciprocal theorem requires that the stiffness matrix must be symmetric. It can be decomposed into a lower and upper triangular matrix, recovering almost half the memory or storage area originally required. Further improvement can be gained by reordering the node numbers to optimize the matrix bandwidth and storing it using the "skyline" method. BAND offers a number of options to do this including Collin's and the Gibbs-Poole-Stockmeyer algorithms.

* SETUP The undeformed finite element data sets are generated and a series of error checks are done verifying the element grid.

- * MATL The material properties of each ply are defined in MATL. The processor uses classical laminate theory to compute the bending-extensional properties. The strength of the processor architecture now becomes apparent. It possible to vary the material properties of the model without regenerating the complete element mesh, optimizing the band width or generating new element data sets.
- * LOAD The LOAD processor generates consistent load vectors for any combination of pressure, traction, body forces, inertia loads and temperature variations. It allows the variation of loads without regeneration of the stiffness matrix.
- * DIAL The nodal deflection analysis and stress-strain computation is done within the DIAL processor. It uses the total Lagrangian formulation method to handle geometric nonlinearities. FORTRAN double precision representation (64 bit) and sequential improvement to convergence was used to increase the accuracy of the solution. This insured the best possible solution but increased the equation solution time by a factor of about eight. The effect of using double precision and convergence can be seen in the figures in Appendices A-N where shear strain is resolved to as low as $\pm 0.003\%$ of the value of E_V long the X axis.
- * GEOM The data generated by even a small model is extensive and difficult to evaluate in tabular form. DIAL provides an extensive array of post-processing choices to present the data in graphical or tabular form. GEOM generated the strain contours for each panel which are presented in the appendices as

well as the extrapolation of strain data from element Gauss points to the nodes.

2. Formulation of the Finite Element Model

Each panel reinforcement configuration required a separate finite element model. A modified thick-shell elastic quadralateral element was used for the analysis. It used the laminate material properties developed in the MATL processor and ply thickness with any offset from the Z axis (specified during the mesh development) to define and individual element stiffness matrix. The greater the Z offset--the greater the resistance to bending. Several of these elements may be stacked through the thickness by merging partial meshes. Stacking meshes results in the direct addition of element stiffness. Element properties are projected to a reference plane (z = 0.0" for this model) which contains the nodes points. Element bending resistance is determined by its stiffness and offset from this reference plane. The advantage of this type of element is that it allows modeling a thin three-dimensional laminate using a two dimensional element, thereby greatly reducing the number of individual element nodes. The modified thick shell element's shortcoming is that it cannot give stresses in any of the stacked partial meshes and the strain is valid only at z = 0. Further, thin plate theory is used which gives strain and the stress resultant \N\ vector. In these models the true thickness varied over the surface of the panels. Plots of stress resultants in this case would be, at best, misleading. Strain was used as the basis for comparison among the panel configurations.

During the experimental phase of the research, premature facesheet separation from the honeycomb core became an unpredicted

failure mode of some of the specimens (panels RR22, RR42, RR51, RS51 & RH31). This type of stability failure could not be predicted employing two-dimensional analysis only. It was postulated that the $[0,\pm45,90]$ facesheet layup or the $[0_2,\pm45,90]$ (or $[0_3,\pm45,90]$) reinforcement could be generating sufficient out-of-plane $(\pm z)$ forces to tear the facesheet away from the core.

To answer the question, a three-dimensional analysis using thick shell elements representing the facesheet, combined with isoparametric solid elements, representing the honeycomb core, for a 3-D analysis. These results (for panel RR22) are given in Appendix O (results showed no significant out-of-plane stress). While DIAL can handle a 2-D element with an aspect ratio (length/ width) up to 20 with little loss in accuracy, an effort was made to keep this ratio below three. At high aspect ratios the interpolation assumptions within each element are no longer valid. The meshes employed were also designed to keep interior element angles as close to 90° as possible, again to increase the accuracy of the solution. Figure 3.2 shows the elements (numbered from 1 to 30) and node points (numbered from 1 to 117) next to the cutout. These elements' dimensions remained unchanged (except for the added reinforcement thickness) for each model, allowing direct comparison among reinforcing configurations in the region near the cutout. Since the plate was symmetric about all three axes only the upper right quadrant of each specimen was modeled.

In the experimental fixture, the compressive load was applied to each 8.50" wide specimen using clamps 8.00 inches wide. The outside edges of each panel had 1/4 of an inch inside a slot in the vertical member which could not be loaded. To simulate a -10 ksi far-field load in the FEA model a constant line load $\{N\}$

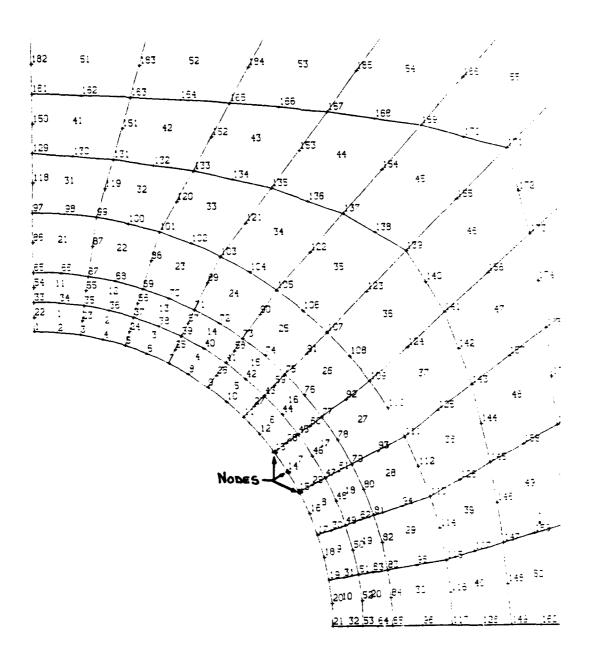


Figure 3.2 Elements and Nodes Next to the Cutout.

of -1,120 lb/in was applied to the 0.112 inch thick plate (neglecting the core). The effect of modeling the test fixture can be seen in the quarter-panel contour plots in the appendices (for example Figure A.4): there is an obvious stress concentration in the upper right-hand corner of the panel. The effects of this stress concentration die out rapidly as the distance into the panel from the line of load application increases.

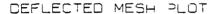
3. Interpreting Finite Element Analysis Results

DIAL, like most finite element programs, produces voluminous data files giving the stress, strain and displacement at each element's integration points. Meaningful comparison of these files among the various panel configurations would be tedious as well as unenlightening. The items of interest were the distribution of stress along the X axis and around the cutout and the strain fields on each panel resulting from the reinforcement. Graphical comparison was chosen as the best method both to present and to compare the panels.

The results from tests of each of the 14 test specimens with a cutout is presented in individual appendices (A through N). Each configuration has a plot of the element mesh and a comparison of strain both along the X axis and around the hole under a farfield normal stress load of -10 ksi. In addition, strain contours for $\overline{\mathbf{O}}_n$ = -10 ksi are shown for each panel's upper right quadrant and for the region near the cutout. Experimental data are correlated with the finite element analysis for each panel.

A plot of a deflected element mesh is presented in Figures 3.3 and 3.4 to illustrate the analytical and experimental boundary conditions imposed on the test panels. Figure 3.3 shows the entire upper right quadrant of the panel. Figure 3.4 shows the

elements close to the cutout. The dashed lines represent the outlines of the elements prior to the application of the load. The solid lines show the elements in the panel compressed under a -10 ksi load. The deflections shown are, of course, an exaggeration of those actually present in the panel, but they are accurate representation in relative scale.



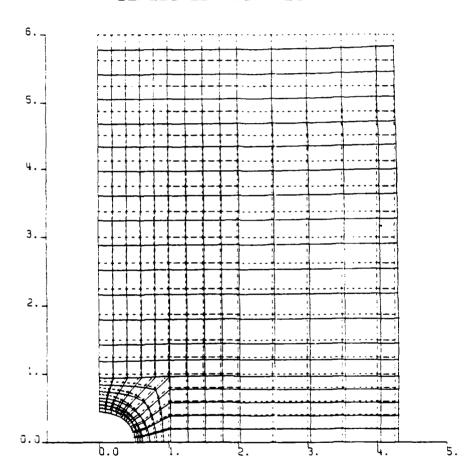


Figure 3.3 Typical Deflected Mesh Plot.

The boundary conditions imposed on the quarter panel are clear: the X axis, representing the longitudinal bisection of the

panel allows no movement in the Y direction but allows Poisson expansion the X direction. The panel boundary on the Y axis was constrained in X displacement but was allowed to move vertically.

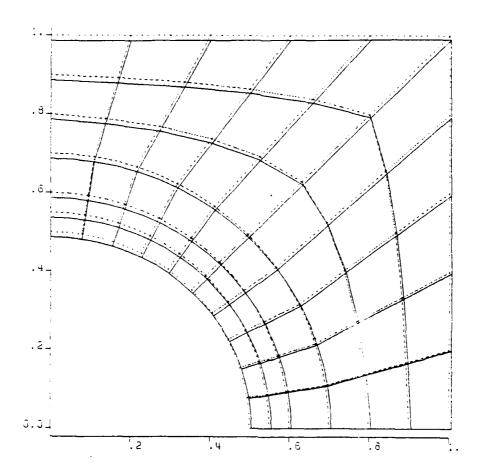


Figure 3.4 Element Deflection Next to the Cutout.

A point to note is the boundary condition at the top of the panel. It was necessary to firmly clamp the upper 8.00" x 1.00" inch area of the panel to assure complete and even load transfer into the G/Ep facesheets. The results of the boundary condition can be seen in the deflected mesh plot; Poisson expansion was not allowed where the panel was clamped. This very closely modeled the experimental setup.

In Figure 3.3 the top edge of the panel has a slight slope upward as X increases from 0.0 to 4.25". This is the result of applying a constant stress boundary condition along the edge rather than constant displacement, which would more closely model the experimental apparatus. This tends to slightly increase the SCF at the hole because the panel finite element model appears somewhat less stiff directly above the cutout than the solid portion.

A test case using constant displacement boundary conditions, which closely approximated the experimental setup, produced less than a 0.5% increase in the SCF. Since each panel has a slightly different stiffness in the Y direction, it would have been exceptionally difficult to impose an identical load on each for comparison.

Hong and Crews [Ref. 25: pp. 4-6] reported significant differences in results between constant stress and constant displacement boundary conditions. In the final analysis, the researcher, understanding the differences and the compromises, must choose the model best suited to his work.

IV. EXPERIMENTAL ANALYSIS

A program of experimental verification was developed in order to determine if the analytical results of the finite element analysis represented the actual strain field. Each reinforcement geometry previously described was manufactured, instrumented and tested.

A. TEST SPECIMEN MANUFACTURE

The test panels were manufactured by Lockheed Missiles and Space Company using methods similar to those for verification of Trident missile structures. The initial uncured prepreg plies of HMF330C/34 cloth G/Ep were laid up on a stainless steel plate in a 4 ply ([0,±45,90]) facesheet. A precut uncured reinforcement (one or two plies) was then placed in position on the top of the uncured layup and retained in place by a small pin. Two identical facesheets were made for each geometry. A standard "bagging" process and cure cycle for the 350°F (450°K) Fiberite 934 epoxy prepreg was used. This included a hold in the autoclave at 360 ±10°F (455 ±5°K) for two hours. Using acid digestion techniques this cycle typically yields a fiber volume of 62 ±2% and a void content less than 1%. One facesheet was joined and cured to a 0.50 inch thick Hexel fiberglass/phenolic honeycomb sheet using 3M Inc.'s AF-126 (250°F curing temperature) film adhesive (known as "Blue Glue"). Once the first facesheet and honeycomb had been bonded an aluminum/epoxy potting compound was poured into the honeycomb cells within 1.25 inches of each end. The aluminum/ epoxy potting compound provided dimensional stability for the

panel, assisted the load transfer and prevented crushing the honeycomb in the panel ends when they were clamped into the compression test frame. The second facesheet was then joined and the now complete rough panel put through a third and final cure cycle. The panel configuration, excluding the one or two ply 0° reinforcement, became [0,±45,90,core]_s. The core's elastic modulii in the X and Y directions were virtually nil and did not contribute to the panel's inplane stiffness.

The center of the reinforcement was marked and a starter hole drilled with a No. 4 carbide-tipped steel drill rotating at approximately 2200 rpm. The hole was enlarged in steps using 0.50 and 0.75 inch diameter carbide-tipped drill bits. The final 1.00 inch finished hole was cut using a carbide-tipped boring head rotating at 1600 rpm moving in depth at 0.0015" per revolution. This method provided a very smooth and almost perfectly circular cutout. Each facesheet was drilled using stiff fiberglass sheets as backing to minimize the breaking of fibers on the bottom ply when the drill bit broke through. Fiberglass tabs (8.0" x 1.0" x0.25") were applied on both sides at either end to provide for load transfer from the test frame into the panel. The rough panel was then cut to the specified size (8.50" x 10.00") using a diamond-coated circular saw. Great care was taken to both keep tne cutout in the center of the panel and to insure the two edges to be loaded were parallel. The general dimensions of the specimens are shown in Figure 4.1.

B. TEST APPARATUS AND PROCEDURES

In compression, much more so than tension, lack of attention to maintaining proper boundary conditions can quickly invalidate experimental results. Great care was taken in the design and

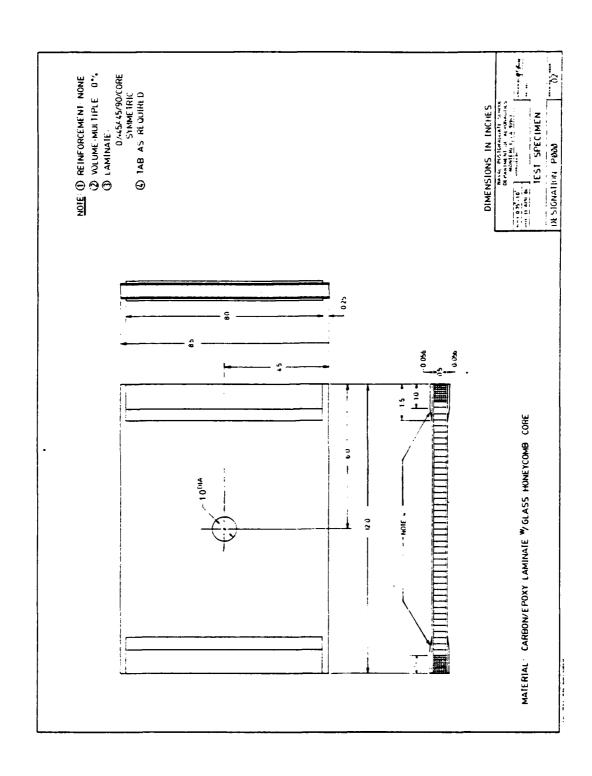


Figure 4.1 Compression Panel Dimensions

construction of the test frame to insure that it was <u>extremely</u> stiff, that the compression surfaces were parallel and that they would remain so during the entire compression sequence.

1. Test Apparatus

a. Load Application

A Material Test System (MTS) Series 810 hydraulic test machine was used produce the compressive loading. The compression test frame was designed to be strong enough to utilize the 100,000 lb. maximum load of the MTS machine. It consisted of a fixed horizontal base and vertical side posts and a sliding horizontal top cross member. Both horizontal members were machined from 7075-T6 aircraft-grade aluminum. The vertical posts were turned to a diameter of 2.000" from diameter mild steel bar stock. The horizontal members were fitted with a means of clamping the test specimens. Each had a 0.250" thick tempered tool steel base plate positioned to transfer the compressive load into the test specimen and to prevent damage to the surface of the aluminum frame. These load plates were carefully adjusted during installation to ensure that they were parallel within a tolerance of ±0.0005 inch.

A 0.614 \pm 0.001" slot was milled in both steel vertical members to accommodate the panel and to allow some vertical movement while preventing out-of-plane deflection. The lower horizontal member was held fixed relative to the frame while the top one was allowed to slide vertically. Bronze bushings were pressed into the upper and lower frame members and then machined to within a \pm 0.001" tolerance. The vertical posts' ends were fitted into these bushings. A special effort was made during the design and manufacture of the test frame to keep tolerances as

small as possible to maintain proper and repeatable test boundary conditions.

Figure 4.2 shows some details of the compression test frame. The following numbers indicate some of the parts and features of the frame and correspond to the numbers in Figure 4.2:

- 1 Tempered tool steel compression support plate.
- 2) Bottom horizontal frame member.
- (3) Vertical steel post.
- (4) Slot to hold edge of the test specimen.
- (5) Bronze bushing.

The test frame was allowed to "float" in the MTS machine. Steel bearing surfaces were fitted to the top and bottom which allowed the test fixture to slide parallel to the floor for centering. These also eliminated the possibility of transfer of any moments from the MTS machine to the frame. Each steel bearing block was made of three pieces: one threaded to mate to the MTS moving piston, a circular 2.000" diameter lubricated cylindrical bearing and one threaded to mate with the test frame. Figure 4.3 show the test frame positioned in the MTS for a test. The bearing blocks can be seen in the figure between the test frame and the machine.

b. Strain Measurement Equipment

A Vishay Measurements Group, Inc System 4000, shown in Figure 4.4, was used to record the strain gage indications. It consisted of a Hewlett-Packard 98258 microcomputer linked through a Measurements Group, Inc., Instrument Division Model 4200

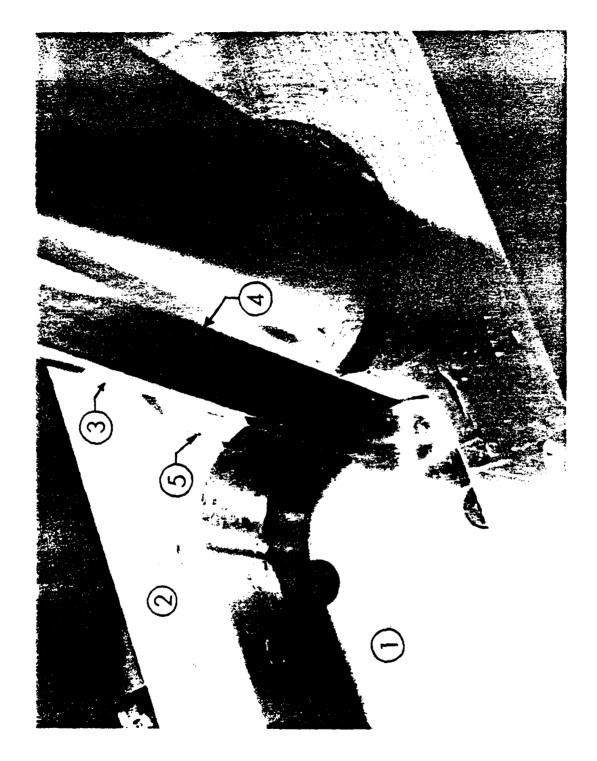


Figure 4.2 Compression Test Frame Details.

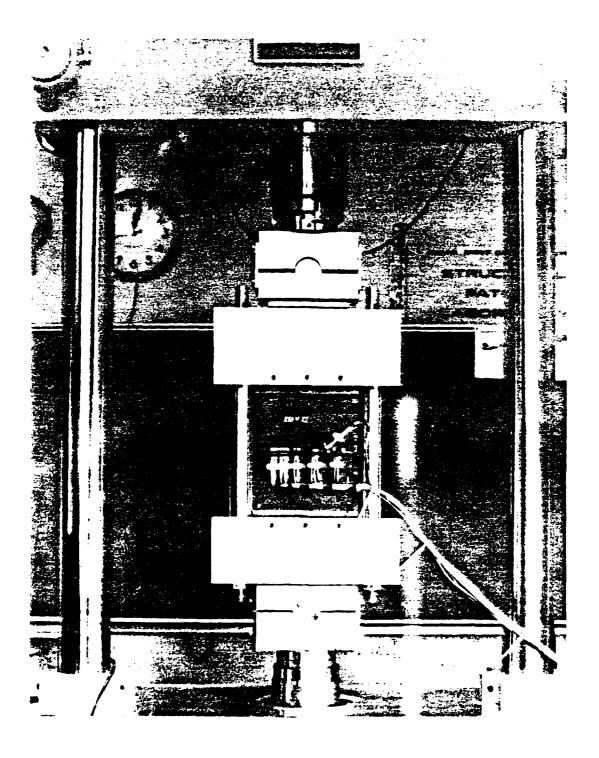


Figure 4.3 Compression Test Frame.

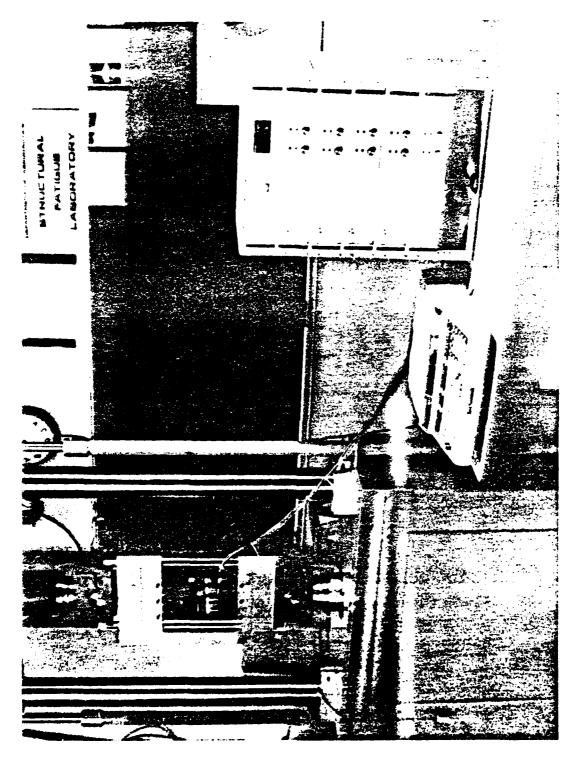


Figure 4.4 System 4000.

controller to Model 4270 strain gage scanners. Integral software provided for gage identification, calibration and strain reading, conversion and printing. The entire experimental test station is shown in Figure 4.5.

2. Instrumentation Procedures

Each panel was instrumented with a variety of strain gages principally located along the X axis and oriented in the Y direction. The primary purpose of the reinforcement was to reduce the maximum strain, and thus the SCF, at the edge of the hole 90° to the applied load. The 0.50 inch honeycomb core was used to eliminate panel buckling. The panel was designed to maintain, as closely as possible, equal strain on opposite facesheets. The gages were located on either side of the hole, but on only one facesheet. In retrospect, gages on both sides of the cutout on both facesheets would have given additional insight into the failure mechanisms.

The choice of strain gages was based on the strain gradient near the cutout, the panel strain field and the heat transfer properties of the G/Ep panel.

a. Measurement of Strain Near a Cutout

The measurement of strain near a cutout in the presence of very high strain gradients is not a straight-forward exercise. Reference 45 points out that an electrical gage effectively integrates the strain field under its grid. When that field changes very rapidly the accuracy of the measurement can be strongly affected. The typical strain field studied here demonstrated gradients as high as 16,000 microstrain per inch within 0.025" of the cutout at -10.0 ksi far-field load.

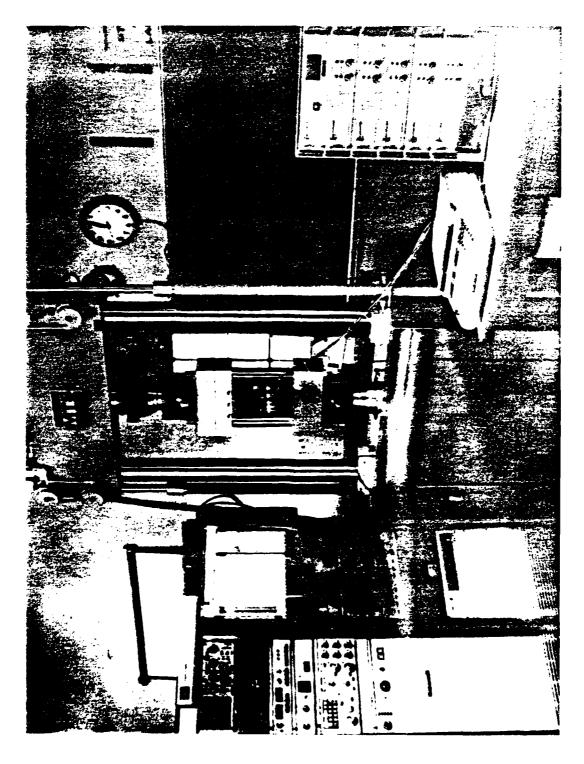


Figure 4.5 Experimental Test Station.

As recommended by Ref. 45, a number of techniques were used to accurately measure the strain field along the X axis. The smallest possible gages were chosen for use for next to the cutout; a series of in-line gages close to the hole gave strain gradient data. Special care was taken to accurately measure the position of each gage. A Rockwell Corp. electronic, digital-readout gurney gave the gage center location to within ±0.002 inch. This resulted, at the -10.0 ksi test point, in about ±30 microstrain or ±1% maximum uncertainty in strain due to gage position error.

b. Strain Gage Excitation Level

Strain gages require some electrical excitation to allow measurement of the change in resistance in the gage grid caused by tension or compression. This results in some degree of resistive self-heating within the grid. This self-heating characteristic can cause significant drift in indicated strain from the true value. When measuring strain in most metals, there is little heat buildup due to their superior heat transfer characteristics. What little there is can usually allowed for by self-temperature-compensation (STC) in the gage. STC requires the matching of coefficients of thermal expansion (a) of the gage and the specimen. The heat transfer characteristic of G/Ep is low compared to metals: The temperature under a gage can rise enough to invalidate the indicated strain reading.

Reference 46 recommends a maximum power density of 0.1-0.2 watt/in² for materials with low thermal conductivity such as G/Ep. Power density (PD, watts/in²) is a function of gage active grid area (A, in²), gage resistance (R, ohms), and gage excitation level (E, volts) according to the relation:

$$PD = E/(4*R*A).$$
 (4.1)

A typical $120\,\Omega$, $0.040\,\mathrm{in^2}$ gage at 5.0 volts excitation has a PD of 1.3 watt/in². As noted above, gages with a small grid area were necessary to accurately measure high-gradient strain. A Measurements Group, Inc. EA-xx-030CM-030 gage (A = 0.0025 in²) [Ref. 47: p. 7L] which could meet the size requirements has a PD in excess of 21 watts/in².

Clearly, high strain gradients and composite materials require extreme care in selecting and using strain gages. A combination of lower than usual excitation levels and higher gage resistance were used too in this research, where required, to keep the power density within acceptable limits.

c. Strain Gage Application

Gages were applied to the panels one facesheet on either side of the cutout along the X axis. They were applied in accordance with the manufacturer's recommended procedures [Refs. 48 through 51] using M-Bond 200 adhesive. Figure 4.6 shows a typical strain gage layout on a test panel. It should be noted that, although similar, each panel had a unique gage layout. Several gages were mounted at points other than along the X axis to verify the analytical strain field.

3. Test Procedures

The test specimens were allowed to age for 180 days at 70°F and 50% relative humidity to reach hygrothermal equilibrium. Immediately after the strain gages were installed the panel was mounted in the compression test frame and loaded to failure.

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The test consisted of initially loading the panel to -2000 psi to set it in the test fixture. The load was then removed and the gage readings reset to indicate zero strain and then

recalibrated. The compressive load was slowly reapplied in increaments to failure. The MTS load control was adjusted in manuality to give each sequentially increasing load, held for about 4-seconds for strain gage reading and then increased. Panels PX\$3,
PO\$\$\phi\$\$, RR11 and RR22 were loaded in 2000 psi steps.

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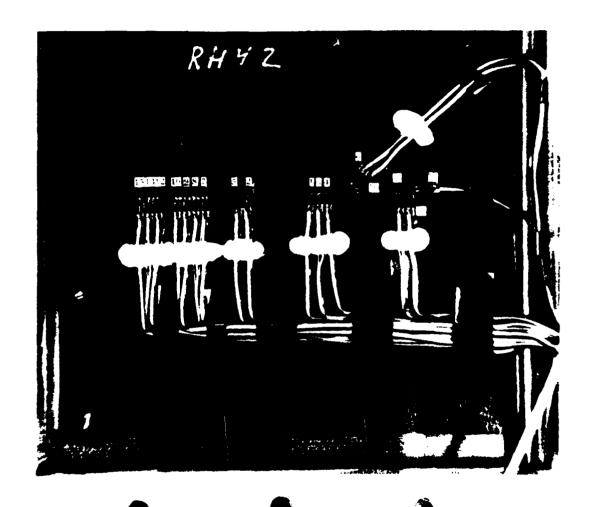


Figure 4.6 Typical Strain Gage Layout

When it became apparent that finer increments were required, 1000 psi steps were used in all subsequent tests. A

typical test required 15-20 minutes to complete. There were some variations in this straight line load procedure which are noted in the appendices for the affected panels.

V. DISCUSSION OF RESULTS

A. COMPARISON OF COMPUTATIONAL RESULTS

All computational analysis were done at a far-field applied stress of -10.0 ksi. These analyses assumed the material had linear elastic properties. This assumption was adequate to reasonably predict the strain field below the material yield point. There are some significant nonlinear yield characteristics of composite materials that require more sophisticated treatment than is given in this report.

1. Open Versus Closed-Form Analysis for an Unreinforced Panel A comparison of open and closed-form strain distribution around a cutout in an unreinforced panel (POØØ) is shown in Figure 5.1. The lines represent the infinite plate width strain computed using the stress function (Equation 3.24) by the FORTRAN program "RBSFM" in Appendix P [Refs. 8 & 40]. The triangular points indicate the LEFEA strains at the node points for the finite-width (8.50") plate The effect of the finite panel width and the constant stress loading boundary condition may perhaps be more easily seen in Figure 5.2 where the FEA strain results are represented by The maximum FEA computed strain is higher increased at the edge of the cutout (x = 0.50) compared with the closed-form results. At distances more than 2 hole diameters away from the cutout (x > 2.0) the FEA model gives slightly less strain. differences between the two analysis in Figures 5.1 and 5.2 are small; it is the similarity of the two that is striking.

The increased FEA strain at the hole is due to the constant stress loading boundary condition. A constant displacement

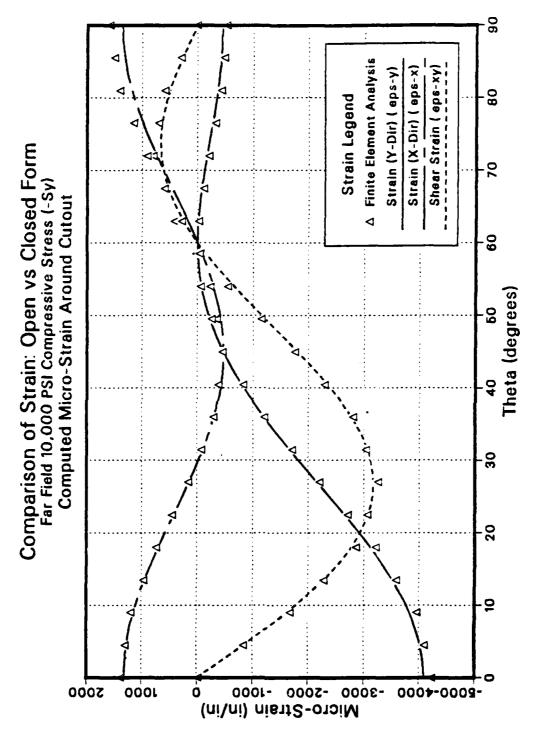


Figure 5.1 Strain Comparison Around the Cutout.

boundary condition would have almost entirely eliminated even this small difference. The reduced strain toward the panel's free edge is due to not applying the load to the outter 0.25 inches of the panel's top edge.

The point of these comparisons is to validate the finite element analysis method, the type element and the configuration chosen. It is assumed that the computational results are as valid for reinforced panels.

2. Finite Element Analysis Results

Table VI summarizes the most important data from the LEFEA. The three maximum strains (Y, X and shear) are given for each configuration as well as the finite-width stress concentration factors. The locations at the edge of the cutout are listed at the bottom of the table. These values are best used as a means of comparison among reinforcement geometries, not for and exact prediction of the micro-strain at the edge of the cutout. Recall the assumption made that the compressive modulus was constant for all strain. Two SCF's are given, one for a theoretical "infinite" plate and one for the 8.50" width panel used in this research.

These stress concentration factors are theoretical only. They are valid solely for a totally elastic strain field. Nuismer and Labor [Ref. 33: p. 50], among others, point out that at high strains (in the case of HMF330C/34 at strain in excess of $9000\,\mu\text{e}$) the fibers immediately next to the hole at the SCF begin to fail and transfer the load through the matrix to adjacent fibers. Compressive failure usually consists of matrix cracking, fiber micro-buckling, ply delamination and the transfer of the load from the failing region next to the hole away to fibers/matrix able to sustain the load. Failure in this manner is difficult to analyze

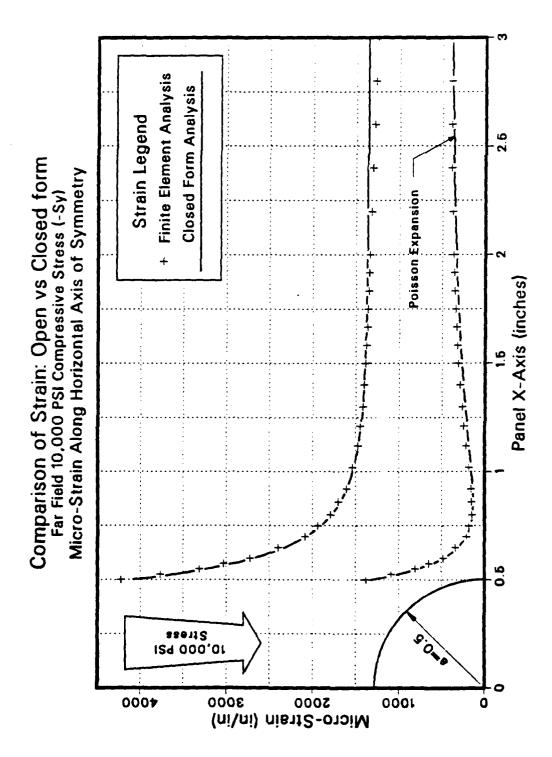


Figure 5.2 Strain Comparison on the X Axis.

using linear methods because of the rapidly changing material properties during the process.

TABLE VI
FINITE ELEMENT ANALYSIS RESULTS

Panel		n Strain Cutout	Strain Concen- tration Factor			
Designation	eps-y	eps-x	eps-xy	w = 00	w = 8.5"	
POØØ	-4230	1596	- 3253	3.00	3.11	
RR11	-3739	1420	-3211	2.65	2.75	
RR22	-3363	1284	-3113	2.39	2.48	
RR31	-3605	1320	-3106	2.56	2.65	
RR42	-3231	1186	-2998	2.29	2.37	
RR51	-3539	1267	-3056	2.51	2.60	
T 11	-3719	1382	-3170	2.64	2.74	
k531	-3545	1254	-3058	2.51	2.60	
RS51	-3465	1193	-2999	2.46	2.55	
RH11	-4261	1777	-3298	3.02	3.13	
RH22	-4097	1821	-3188	2.91	3.02	
RH31	-3983	1545	-3097	2.82	2.92	
RH42	-3727	1645	-2947	2.64	2.74	
RH51	-3997	1475	-3094	2.83	2.93	

eps-y @ $\theta = 0^{\circ}$, eps-x @ $\theta = 90^{\circ}$, eps-xy @ $\theta = 27.0^{\circ}$

Figure 5.3 shows a comparison of the maximum Y direction strains (eps-y in Table VI) at the edge of the cutout. These correspond to the theoretical stress concentration factors. Several facts become apparent:

- Panels RR22 and RR42 gave the best theoretical reduction in SCF. They had most of their reinforcement concentrated next to the cutout in 2 plies (thick) per facesheet.
- In no case was the 500% (single ply) reinforcement appreciably superior to the 300% (single ply) configuration in reducing the SCF. Reinforcement relatively far removed from the hole edge added little strength to the panel.
- The square reinforcement configuration provided very slightly more strain reduction compared with equivalent round.

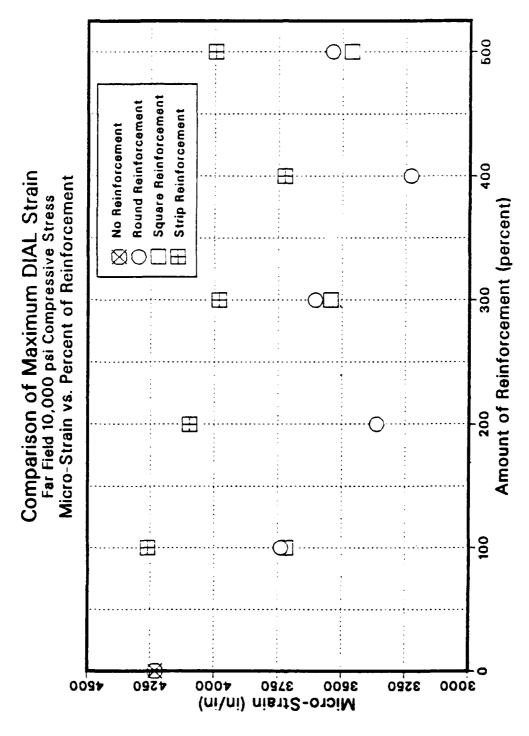


Figure 5.3 Comparison of Maximum FEA Strains.

The strip reinforcement resulted in about 12% higher strain for the same amount (percentage) of reinforcement compared with the other two configurations.

B. COMPARISON OF EXPERIMENTAL RESULTS

1. Solid Panel

Panel PXØØ was tested to provide a basis for comparison and an indication of the ultimate strength of a panel without a cutout or stress concentration. The panel was subjected to two loading sequences: the first up to $\overline{\sigma}_n = -45.0$ ksi (about two-thirds the estimated ultimate load) and the second to failure at -57.0 ksi. Two load runs were used to determine if there was any residual damage from the first load. After the first run, residual damage would be indicated by reduction in inplane stiffness (the effective modulus E_y) due to matrix degradation. Table VII shows the results of the test. The first run was a maximum load of approximately 80% of the ultimate; no significant difference is apparent between the two runs. It appears that this G/Ep material is elastic, at least up to about 80% of its ultimate compressive strength.

The monotonically decreasing stress-strain curve (noted in Section III.A.1) is significant. It most probably results from the decreasing ability of the crimped harness weave fibers to carry the compressive load as the load increases. The close correlation in strain (Eps-y) and modulus (E $_{y}$) between runs 1 and 2 would seem to eliminate matrix cracking or delamination, at least below -45.0 ksi, as a source of the nonlinear behavior; it's nonlinear and elastic.

Figure 5.4 shows the stress-strain curves for both load sequences. Test sequence No. 1 is almost exactly duplicated by No. 2. These curves came from the average of 10 gages mounted

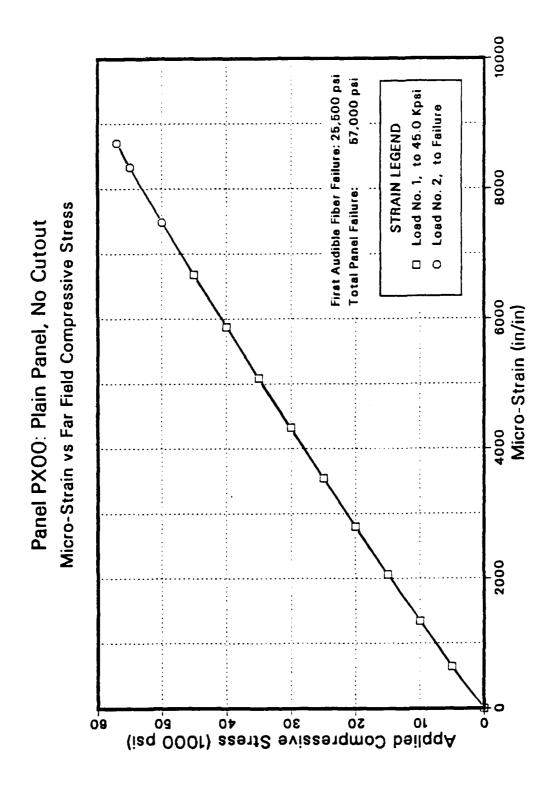


Figure 5.4 Stress-Strain Curve for Solid Panel (PX)).

transversely (on the X axis) on the panel. The gages were all the various sizes and resistance values used on the other panels. The standard deviation of all the values was within $\pm 4\%$ of the average for each load. This could be taken as the typical limit of accuracy for any one gage. When including consideration for the position error noted above it would not be unreasonable to consider any experimentally measured strain to be within about $\pm 4\%$ of the true value. It is doubtful that more accurate measurement is possible without taking extraordinary measures.

TABLE VII
PANEL PXØØ TEST RESULTS

22223333		Run #1		#24 22 3#22:	Run #2				
Load (- ksi)	eps-y (μ€)	E. (m š i)	ν_{12}	eps-y (µ€)	E. (msi)	$\boldsymbol{\gamma}_{12}$			
5 10 15 20 25 30 35 40 45 50 55	644 1341 2065 2799 3543 4323 5092 5879 6683 	7.76 7.46 7.26 7.15 7.06 6.94 6.87 6.80 6.73	0.311 0.315 0.314 0.314 0.315 0.315 0.316 0.317 0.318	636 1342 2060 2793 3544 4302 5073 5891 6663 7485 8328 8702	7.86 7.45 7.28 7.16 7.05 6.97 6.90 6.79 6.75 6.68 6.60 6.55	0.336 0.322 0.320 0.319 0.318 0.318 0.319 0.320 0.321 0.321			

2. Panels with Stress Concentrations

The results of the experimental program are summarized in Table VIII. Individual panel experimental and computational results are discussed in the appendices. The loads in (ksi) are listed for the first audible ply failure (FAPF) and ultimate. The

FAPF was nothing more than the first "pop" heard during the loading sequence. While this hardly seems to be a rigorous definition, in every case the FAPF appeared to be a predictor of the ultimate load. Stress concentration factors (SCF) were taken from the finite element analysis. In the strength reduction column the calculated value came from equation 2.6 using a. = 0.33", the value determined by LMSC for HMF330C/34 cloth G/Ep. Nuismer and Whitney [Ref. 26: pp. 122-3] state that there is some evidence that the value of ao remains "constant for all laminates of all fiber reinforced/resin matrix composites...at least for what has been referred to as 'fiber of filament-dominated' laminates in glass/epoxy, boron/epoxy, and graphite/epoxy systems." There seems to be some difference, however, between tape (a. = 0.28" for AS/3501-5) and fabric (a. = 0.33" for HMF330C/34). The actual strength reduction is based on the ratio of the solid panel $(PX\emptyset\emptyset)$ ultimate strength to that of each panel with the stress concentration. The percent difference (% Δ) between calculated and actual strength reduction is [(calculated-actual)*(100/calculated)]. This value serves to compare the relative magnitude of observed strength among test specimens. A positive value of ${}^{\$}\Delta$ indicates a panel which demonstrated higher strength than predicted by the SCF computed by the LEFEA. Note the close correlation among FAPF, actual strength reduction and failure type.

3. Types of Panel Failure

There were two types of panel failure: (Type-1) delamination at the point of highest stress concentration ($\theta = 0^{\circ}$ on the edge of the cutout) followed immediately by total failure and (Type-2) facesheet separation followed at some higher load by catastrophic failure. Type-2 failures occurred far below the

expected stress level. A panel with a Type-2 failure not taken to to a complete failure was designated Type-2'.

TABLE VIII
COMPARISON OF EXPERIMENTAL RESULTS

Panel	FAPF	Ultimate		Streng	th Reduc	tion	Failure
Desig.	Load	(psi)	SCF	Calc.	Actual	₹Δ	Type
PXØØ POØØ	25,500 17,000	57,460 30,000	1.00	0.00 1.89	0.00 1.88	0.0	_
RR11 RR22 RR31 RR42 RR51	18,500 16,000 17,500 13,500 5,500	29,950 21,050 28,000 21,900 16,000	2.65 2.39 2.56 2.29 2.51	1.87 1.87 1.87 1.86 1.87	1.92 2.73 2.05 2.61	- 2.7 -46.0 -9.6 -40.3	1 2 1 2 2
RS11 RS31 RS51	17,000 17,500 7,000	31,000 32,550 19,600	2.64 2.51 2.46	1.87 1.87 1.87	1.85 1.77 **	+1.1 +5.3 **	1 1 2
RH11 RH22 RH31 RH42 RH51	19,000 18,000 9,500 21,000 16,500	29,960 31,640 21,530 36,990 31,630	3.02 2.91 2.82 2.64 2.83	1.89 1.88 1.88 1.87 1.88	1.92 1.82 2.67 1.55 1.82	-1.6 +3.2 -42.0 +17.1 +3.2	1 1 2 1

Strength reduction calculation used as = 0.33 in. from LMSC test data. Panels marked with ** were not taken to total failure.

Failure Types: 1 - Failure originates at Strain Concentration

2 - Facesheet Separation & Buckle

2' - Facesheet Separation & Buckle (not loaded to ultimate)

It has been noted that in compression there exists a tensile Poisson stress $(+\sigma_z)$ which is greatest at the point of highest stress concentration on the edge of of the cutout and tends to pull the plies apart. It was not possible from this experimental procedure to determine if ply delamination, interlaminar shear stress or micro-mechanical fiber buckling was the initiator of the failure. In fact, failure probably resulted from

two or all three of these working together, possibly in conjunction with both fiber and matrix flaws. Figure 5.5 shows a typical compressive panel (Type-1) failure. All Type-1 failures were almost identical in appearance; they differed only in the ultimate load sustained.

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All Type-2 and Type-2' failures were also similar to each other; the facesheet began to pull away from the core at some point away from the edge of the cutout. This began with the formation of a small bulge or "bubble" which increased in total area and distance from the face of the core to inside surface of the facesheet. The initial separation was not visible until well into the load cycle, however, in some cases the FAPF may have well been the sound of the initial adhesive failure. Once the leading edge of the separation reached the cutout the panel failed totally.

Type-2' failure was this facesheet separation not taken to total failure. The partially failed panels were removed from the test apparatus and subjected to non-destructive (NDI) and destructive inspections in an attempt to determine the possible cause of the core-facesheet separation.

Panels RR22, RR42, RR51 RS51 and RH31 failed by facesheet separation. The stress-strain curves for these panels appear in the individual appendices and all clearly show the result of the facesheet separation—the slope of the curve dramatically increased. This was due to the decreasing panel stiffness and the picking—up of the load as the area of separation and facesheet curvature increased.

When this failure mode appeared an additional FEA was considered necessary to examine in detail the core-facesheet

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Figure 5.5 Typical Test Panel Failure in Compression.

interface. A three-dimensional analysis was made of panel RR22 to determine if any significant out-of-plane stress was causing the separation. The results are given in Appendix O. The interface (the idealized adhesive surface) showed very low stresses in the tz, or out-of-plane, direction. From this it may be assumed that facesheet separation was the result of an incomplete or bonding process or other manufacturing error.

The Type-2' failure panels were subjected to non-destructive inspection using C-Scan and X-ray methods to attempt to locate the source of the defect(s). No obvious flaws or manufacturing errors were apparent. Panels virtually identical to those Type-2 and -2' failures were manufactured and tested under the same experimental conditions. In each case the panels sustained Type-1 failure and carried an ultimate load into the -29 to -35 ksi range.

VI. SUMMARY, CONCLUSIONS AND RECOMMENDATIONS

A. SUMMARY

This study examined three geometric configurations of co-cured reinforcement of graphite/epoxy honeycomb plates with circular cutouts subjected to uniaxial compressive loading and compared them to identically loaded unreinforced notched and solid plates. The test specimens were modeled using linear elastic finite element analysis (LEFEA) to analyze the strain field around the cutout. The objective of the study was to determine if a relatively simple, inexpensively manufactured reinforcement of a cutout could significantly reduce the stress concentration it induced, decrease the local strain and thereby increase the ultimate (failure) strength of the panel.

Table IX is a summary of the important analytical and experimental results. The computed SCF is derived from the LEFEA. The predicted failure stress is based on the actual failure of the unreinforced panel (POØØ) and the analytical SCF. More than many any other experimental results, compressive failure in composite plates should be classed a stochastic function. It would take a number of identical panels of each configuration to arrive at a statistically significant predicted failure stress. However, from the data of this study, the average of the eight Type-l failures was 93.5% of the predicted failure stress. The strip reinforcement (four Type-l failures) failed at 100.5% of the predicted applied stress. A three-dimensional linear finite element analysis of a typical Type-2 failure (Panel RR22) was attempted (see Appendix O). It failed, however, to predict the

actual failure loading or to provide a reason for the premature facesheet separation.

The test program reported here confirmed that, properly used, the linear elastic finite element method provided an exceptionally accurate strain field representation even in a material with nonlinear response (see Appendices A-O). The failure stresses were harder to predict using linear methods, but this is hardly surprising considering the material is a composite and the loading is compression.

TABLE IX
SUMMARY OF ANALYTICAL AND EXPERIMENTAL RESULTS

======				######################################	======
Test	Compute	Failure Str		% Predicted	Failure
Panel		Predicted	Actual	Load	Type
POØØ	3.00		30,500	100	1
RR11 RR22 RR31	2.65 2.39 2.56	34,500 38,250 35,750	29,950 21,050 28,000	86.8 55.0 78.3	1 2 1
	2.29 2.51	39,950 36,500	13,500	33.8	2 2'
RS11 RS31 RS51	2.64 2.51 2.46	34,650 36,500 37,200	31,000 32,550 19,000	89.5 89.2 51.1	1 1 2'
RH11 RH22 RH31 RH42 RH51	3.02 2.91 2.82 2.64 2.83	30,250 31,500 32,500 34,650 32,300	29,960 31,640 12,000 36,990 31,630	99.0 100.0 36.9 106.8 97.9	1 1 2 1

B. CONCLUSIONS

From data in Table IX it can be seen that reinforcement reduced computed stress concentrations up to 20% in some configurations. The reinforcement added little more than 1 to 4%

additional weight to each panel. While it is difficult to directly compare the improvement reported here with configurations in an actual application in a large, complex structure, it is easy to see that for a small increase in weight a significant reduction in stress concentration is both predicted and realized.

Small amounts of graphite/epoxy reinforcing lamina(e) co-cured with thin composite sheets of the same material can significantly reduce stress concentrations and increase ultimate failure load. This reinforcement method involves some additional manufacturing effort, but it yields excellent strength-to-weight comparisons. The analytical results indicate that using several small reinforcement plies concentrated close to the cutout provides the most attractive strength-to-weight ratios. The strip configuration also gives excellent results and seemingly very predictable failure levels.

This experimental program reaffirmed the well-known fact that even minor manufacturing defects can be a severe problem in compression testing. Improper or incomplete bonding of the face-sheets to the honeycomb core can significantly affect the ultimate failure load in graphite/epoxy specimens. In five cases the facesheet began separating from the core at a point away from the cutout. A "bubble" then formed reducing the facsheet's load resistance and transferring the load to the opposite, still intact facesheet. The panel then began to exhibit greatly decreased stiffness. As the load was increased, panel stiffness decreased in proportion—similar to Euler column buckling.

It was not possible to locate the source of the bonding failure or even prove conclusively that improper bonding was the source of the premature failure. However, since the "bubble"

usually initiated at low load levels and at points well away from the stress concentration, bonding failure appears to be the most logical explanation. Prior to testing the panels were subjected to NDI which failed to discover any unbonded areas between the core and facesheet. These failures could have been a case of weak or only partial adhesive bonding.

C. RECOMMENDATIONS

The research reported here investigated only a few of the possible reinforcement geometries. Any number of significant questions remain unanswered in the research reported here. Additional work is suggested in the following areas:

1. Further Testing of Reported Geometries

Time and money limited testing to one specimen of each geometry. Several of the most promising reinforcement configurations (RR22, RR42, RH42, etc.) should be subjected to further testing to obtain statistical confirmation of these results.

The reaction of some of the strain gages remains unexplained, at least in part. For example, panel RS31 (Appendix H, Figure H.4) the gages closest to the cutout show points where an increase in load causes no corresponding strain increase. At a higher applied stress the gage begins to react normally and stress-strain curve resumes an offset but parallel course (also see panel RH22, Figure K.4).

2. Additional Reinforcement Geometries

The three geometries reported here hardly exhaust the possibilities. Some additional promising configurations include oval (when the principal load direction is known or is predictable), several different "wedding cake" methods and moving the strip configuration closer to the cutout.

3. The Effects of Reinforcement Stiffness

Reinforcement plies identical to the reinforced material was used in this study. It would be interesting to observe the effects of stiffer reinforcement such as laying G/Ep tape reinforcement 0° to the applied load.

4. Improvements to Experimental Methods

A dense strain gage network next to the cutout on both sides of each facesheet may better explain the mechanics of failure. Much closer load increments are necessary, 1000 psi steps were not sufficient for a full explanation of the high strain notched panel response.

A micro-photographic sequence of the stress concentration at the edge of the cutout at high load (starting at 80% of $\sigma_{\rm ult}$) might yield significant information on the way the graphite/epoxy panels fail in compression.

The MTS machine used in this research maintained a constant (or constantly increasing) load using an electronic feedback loop. When the panel began yeilding, stiffness was reduced and the rate of head travel increased in an attempet to maintain the indicated load. At failure, the head moved about 1/3" - 1/2" and crushed the panel. This precluded detailed examination of the delamination at the stress concentration at failure. A constant displacement compression test machine is recommended in subsequent research.

APPENDIX A

PANEL POSS: ANALYTICAL AND EXPERIMENTAL DATA

Panel POØØ served as the basis for comparison between reinforced and unreinforced compression specimens. It had a centered 1.00" diameter hole with no reinforcement around the cutout. Two identical specimens were produced, instrumented and tested. They both failed at the hole edge (Type-1) at an average applied normal compressive stress ($\overline{\sigma}_n$) of -30,500 psi.

The panel finite element model (mesh) is illustrated in Figure A.1. Figure 5.1 shows the distribution of strain around the cutout comparing open and closed-form computation methods. Table X gives the (finite element) computed strain data around the cutout. Figure A.2 shows the correlation between computed strain (solid and dashed lines) and the experimentally measured strain (triangles) along the X axis at an applied normal stress of -10,000 psi. Figure 5.2 shows the correlation between open and closed-form analysis along the X axis. Table XI lists the computed values of the strain parallel to the applied load (Eps-Y) and Poisson expansion (Eps-X) along the X axis.

Note that in Figure A.2 between the 1.25 and 2.75 inch stations on the panel's X axis the indicated gage strain seems to alternate slightly up and down. Gages indicating high were on the right side of the hole while those indicating slightly lower were on the left. In order to best illustrate the effect of the stress concentration, left and right side gages are superimposed on the right side of the cutout. It appears that the right side saw

about 1 to 2% higher strain than the left. The strain difference is attributed to either a very slight test fixture misalignment or a difference in panel length between each side of the hole amounting to about to somewhat less than 0.0005"

Figure A.3 shows graphically the experimentally measured values of strain at different locations on the X axis. The numerical strain data are given in Table XII. The center of gage #1's resistive grid at x = 0.570" was 0.070" from the edge of the hole. The strain indicated was appropriate to the applied load taking into account the nonlinearities discussed in Chapter 5. Between -7,000 and -9,000 microstrain on gage #1, there appears to be a slight anomaly where the strain does not increase as fast as it had up to that point, but it then appears to "catch up." This may be attributed to minor fiber failure, nonlinear load transfer or local delamination. This is a phenomenon that becomes much more apparent in the tests of reinforced panels.

Figures A.4 through A.7 show the strain field contours at an applied normal stress of -10,000 psi computed and plotted using DIAL. Figure A.4 is the full quarter panel which shows the effect of not loading the full width of the top edge. Figures A.5 through A.7 show the strains contours close to the cutout. The computed strains are very close to that for the ideal infinite—width panel.

Figures A.8 through A.11 plot panel stress contours at the -10,000 psi loading. The type of element used in the LEFEA required the applied load to be input as a stress resultant (N, 1b/in) and produced plots in the same units. Since all the reinforced panels had different thicknesses over their surfaces, the plots of stress resultant were not valid and are not given for

any other panels. Plots of stress are included to be compared with the classic notched plate solution to validate the analysis.

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Figure A.8 shows the full quarter panel with the stress concentration in the upper right corner due to the panel clamping modeling and the imposed boundary conditions. Figures A.8 and A.9 show the maximum resulting stress parallel to the load. The maximum induced stress (at θ = 0°) is 31,100 psi which compares to 30,500 psi (Equation 2.3) for the finite-width panel. This is just 3.6% over that predicted for an infinite plate. This minor difference is accounted for by the loading and boundary conditions.

PANEL PODO: NO REINFORGEMENT PANEL MESH LAYOUT

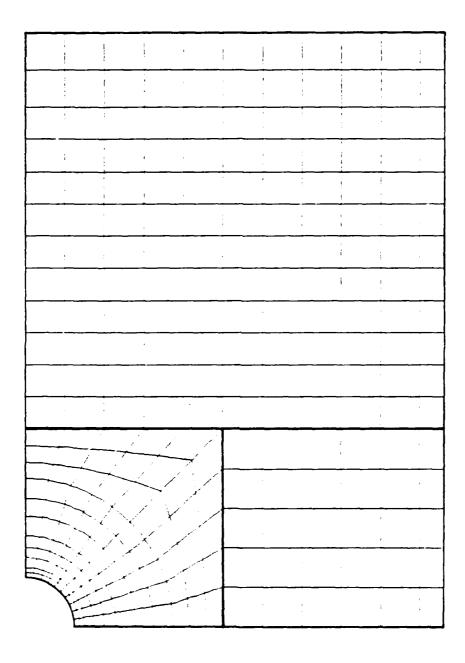


Figure A.1 Panel POM: DIAL Finite Element Mesh.

PADI U V

PANEL POSS: LEFEA STRAIN DISTRIBUTION AROUND THE CUTOUT (-10,000 PSI).

EP S-XY	中では、
EPS-X	00000000000000000000000000000000000000
EPS-Y	2202222222222222222222222222222222222
Y COORD	00000000000000000000000000000000000000
X COORD	00000000000000000000000000000000000000
NODE	

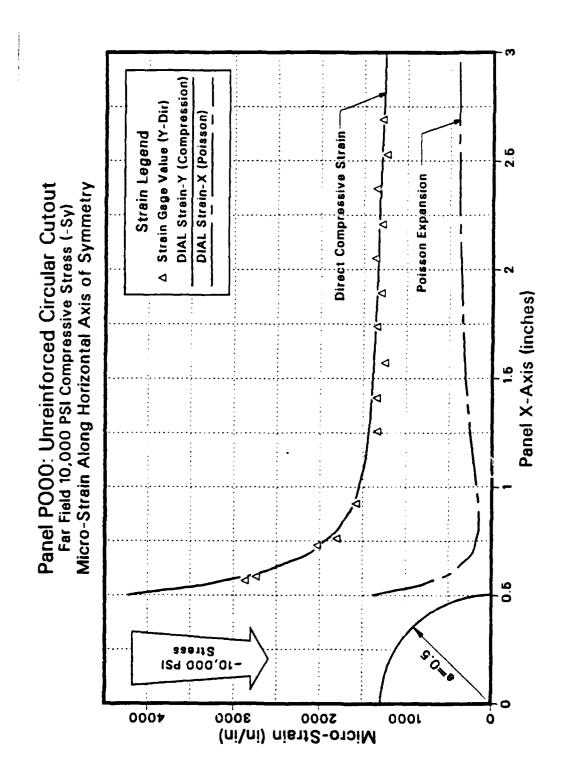


Figure A.2 Panel PO99: Strain Comparison Along the X Axis.

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(-10,000 PSI).	1-2	11111 00000000000000000000000000000000	3698E-
THE X AXIS (-10	7 SQ 7	00000000000000000000000000000000000000	3689E-0
DISTRIBUTION ALONG) >= '	11111111111111111111111111111111111111	0.1127E-0
STRAIN)))		.0000E+0
PANEL POGG: LEPEA		00000000000000000000000000000000000000	. 4250E+
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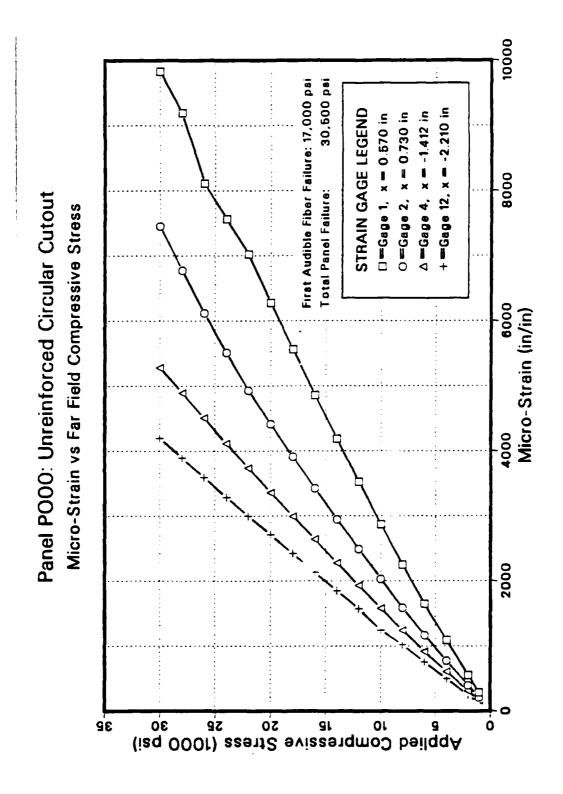


Figure A.3 Panel POM: Mircostrain vs. Copressive Stress.

TABLE XII

PANEL POSS: SELECTED STRAIN GAGE VALUES DURING LOAD.

Load (psi)	Micro	c-strain I	ndicated b	y gage:
(527)	#1	‡ 2	#4	*12
20000 240000 800000 111460000 112460000 112460000 1122222233	- 1044591379826129 - 1162462318579826129 - 122314855726129 - 1223148579826129	7538617810629546 1150494211301746 12223394951756	-130143 : 573 6517 -1462739641008 -1112223371508 -1212233374492	159530 -1249530 -2495249 -1156530 -1156

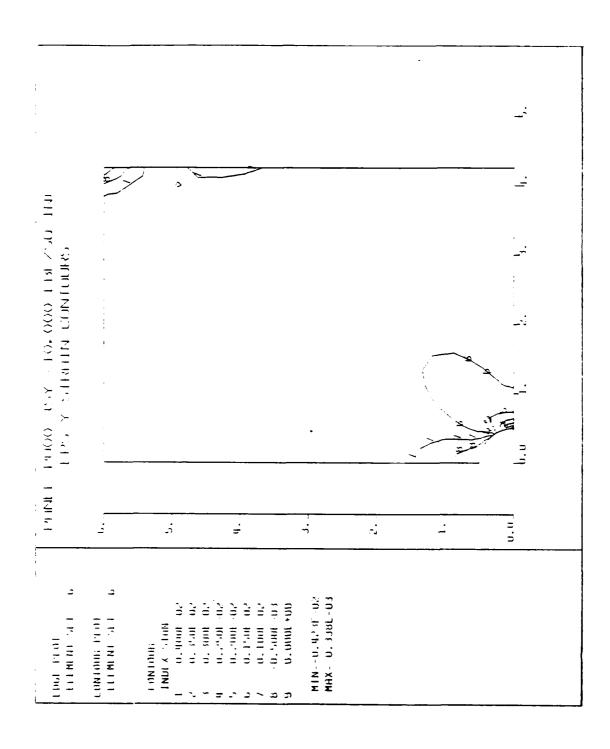


Figure A.4 Panel POFF: Eps-Y FEA Contours.

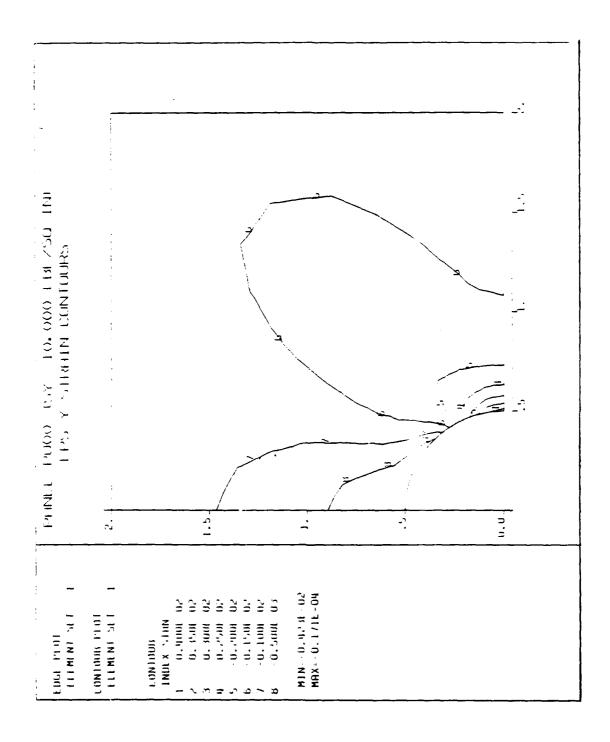
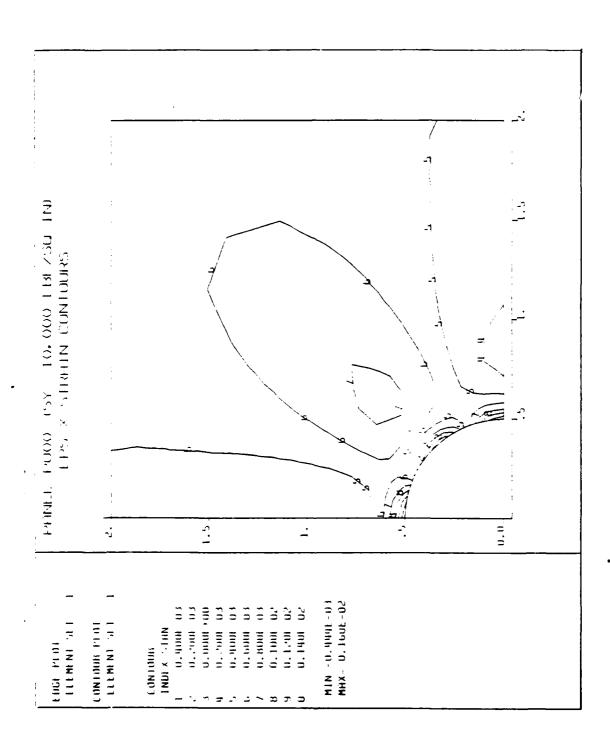


Figure A.5 Panel POFF: Eps-Y FEA Contours Near the Cutout.



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Figure A.6 Panel POFF: Eps-X FEA Contours Near the Cutout.

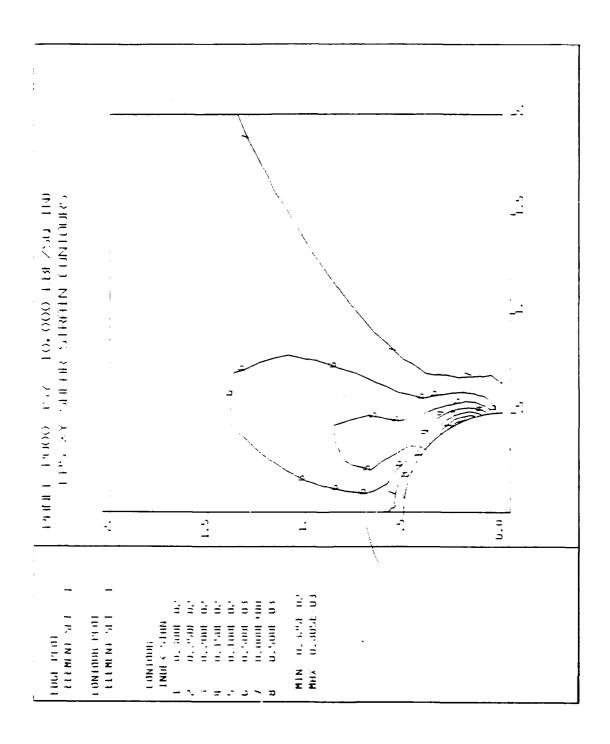


Figure A.7 Panel POFF: Eps-XY FEA Contours Near the Cutout.

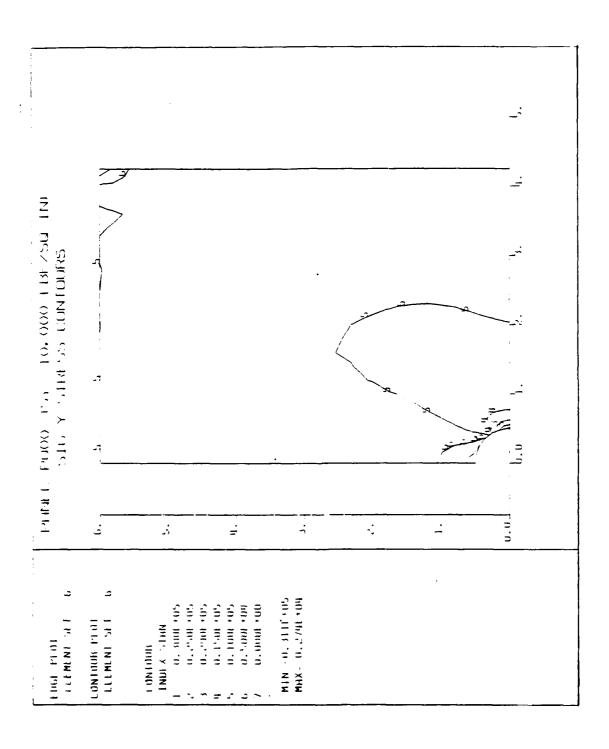


Figure A.8 Panel POFF: Sig-Y FEA Contours.

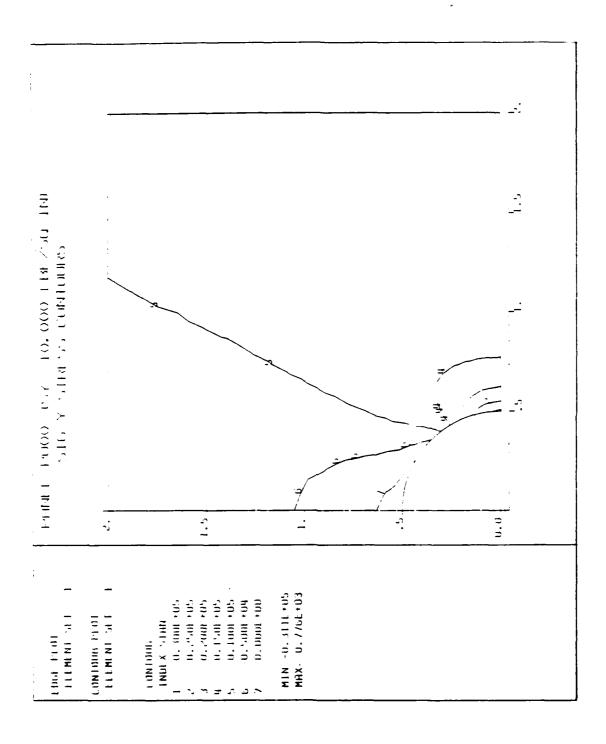


Figure A.9 Panel POFF: Sig-Y FEA Contours Near the Cutout.

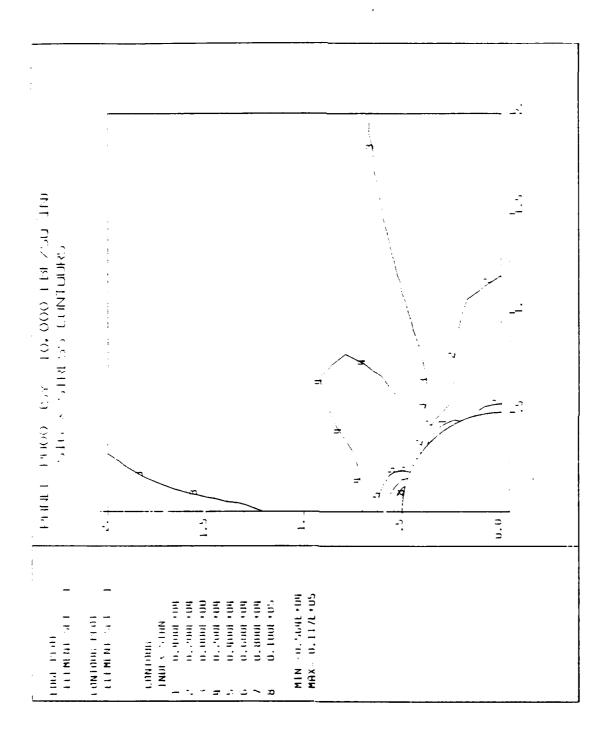


Figure A.10 Panel PO##: Sig-X FEA Contours Near the Cutout.

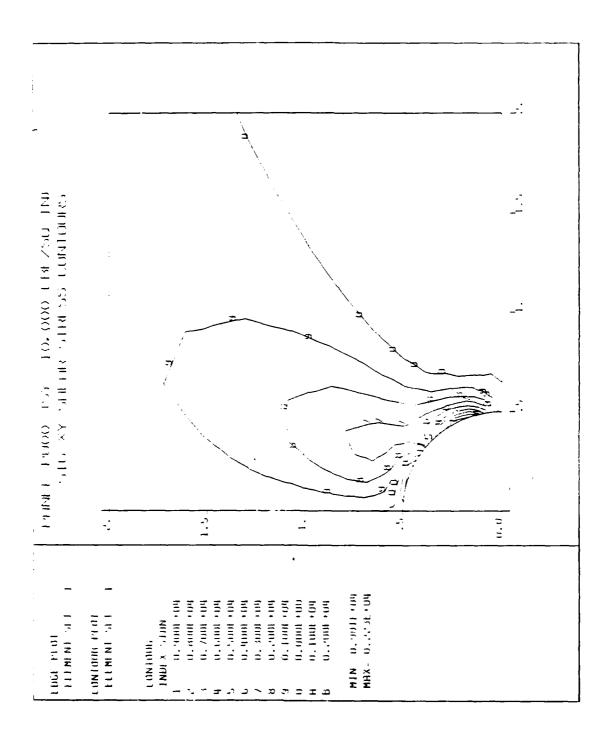


Figure A.11 Panel POFF: Sig-XY FEA Contours Near the Cutout.

APPENDIX B

PANEL RR11: ANALYTICAL AND EXPERIMENTAL DATA

Panel RR11 was reinforced with one round co-cured ply of G/Ep concentric with the cutout placed on the outside of each facesheet. The reinforcement had the following dimensions:

Shape:	Round		
Inside Diameter:	1.00	in	
Outside Diameter:	2.24	in	
Thickness (each):	0.014	in	(1 ply)
Area (each face):	3.16	in^2	
Total Volume:	0.088	in^3	
Net Cross Section:	0.035	in^2	

The panel failed at the hole edge (Type-1) at an applied normal compressive stress of -29,950 psi. Based strictly on the failure of the unreinforced panel and the computed stress concentration factor of 2.65, the predicted failure was $\bar{\sigma}_n$ = -34,500 psi. Failure was at only 87% of the predicted load. There was no obvious reason for the early failure. No manufacturing errors were apparent on post-test visual or non-destructive inspection of the facesheet-honeycomb bonding.

The finite element model (mesh) is shown in Figure B.1. The area of round reinforcement is denoted by the area inside the bold outline around the cutout.

Figure B.2 compares the computed (finite element) strains around the cutout between the unreinforced panel (PO \emptyset \emptyset) and RR11.

Table XIII gives the computed distribution of strains around the cutout in the Y and X directions as well as shear (Eps-X, Eps-Y and Eps-XY).

Figure B.3 compares the finite element models (solid and dashed lines) and the experimental values (triangles) of strain at -10,000 psi applied normal stress. It shows the very close correlation between the analytically predicted and experimental strain with some minor variation on either side of the panel. The LEFEA strain values are listed in Table XIV. The edge of the reinforcement extended to 1.12" in on the X axis. This is apparent from the figure as the inflection point in the direct compressive strain (solid line) where it abruptly begins to increase.

Figure B.4 shows the stress-strain state during the load sequence from 0 to -30 ksi. Experimentally measured strain gage values are given in Table XV. At -16 ksi the gage next to the hole (x = -0.571") suddenly indicates a severe loss of local stiffness. This is reflected to a smaller, but no less dramatic degree in gage $\ddagger 3$ on the other side of the cutout at x = 0.749". Gage $\ddagger 1$ demonstrates what appears to be a continuous increase in local stiffness starting at -18 ksi; as the load increases the strain decreases. Between -22 and -24 ksi the strain is rapidly changing from compressive to tensile next to the hole. No visible buckling or delamination, which might help to explain part of this behavior, was noted next to the cutout under visual inspection.

Figures B.5 through B.3 show the LEFEA computed strain contours at an applied normal compressive stress of -10,000 psi computed and plotted using DIAL. Figure B.5 is the full quarter panel with strain parallel to the applied load. This shows some strain contours at the top right of the panel illustrating the

effect of not loading the full width of the top edge. Figures B.5 through B.8 (Eps-Y, Eps-X and Eps-XY) show the strains in detail close to the cutout.

PANEL RRIL: ROUND REINFORCEMENT PANEL MESH LAYOUT

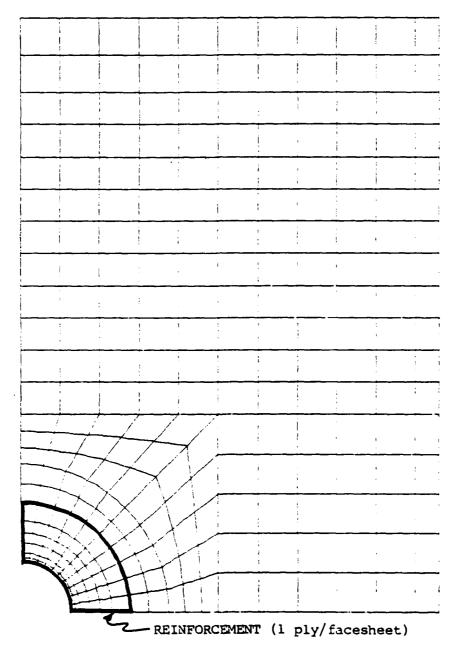


Figure B.l Panel RR11: DIAL Finite Element Mesh.

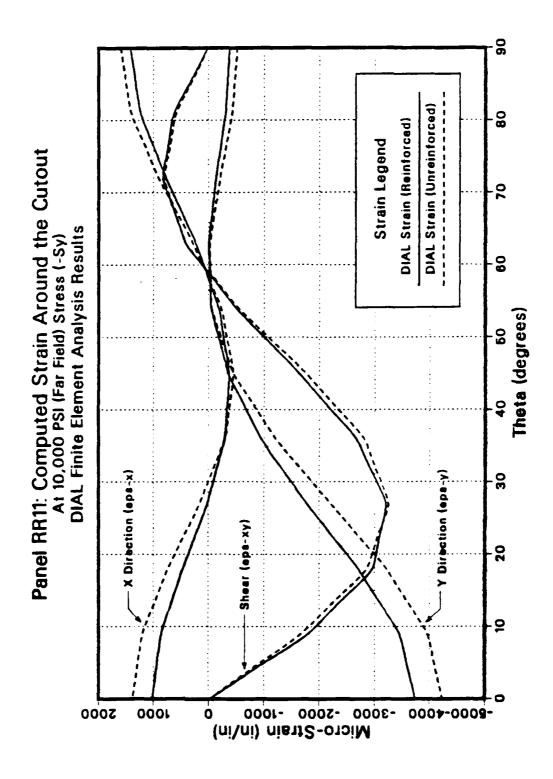


Figure B.2 Panel RR11: Strain Comparison Around the Cutout.

TABLE XIII

PANEL, RRII: LEPEA STRAIN DISTRIBUTION AROUND THE CUTOUT (-10,000 PSI).

EPS-XY	00000000000000000000000000000000000000
EPS-X	00000000000000000000000000000000000000
EPS-Y	22222222222222222222222222222222222222
Y COOKD	00000000000000000000000000000000000000
X COORE	00000000000000000000000000000000000000
NCDE	してしまましましてののとうられをてよくこともよりしましましましまって

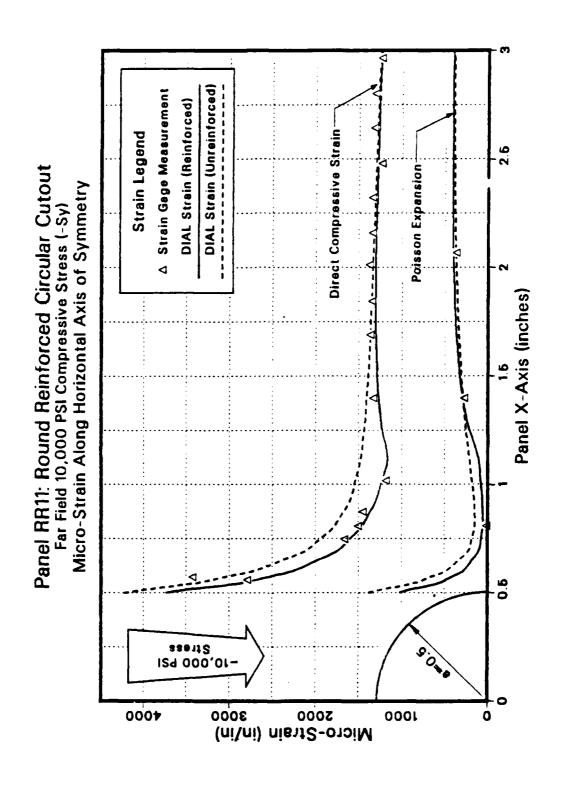


Figure B.3 Panel RR11: Strain Comparison Along the X Axis.

(-10,000 PSI).	EPS-XX	1111 000000000000000000000000000000000
THE X AXIS (-10	EP S-X	Manual
distribution along t	EPS-Y	
STRAIN	х соокр	
EL RRII, LEPEA	X COORE	00000000000000000000000000000000000000
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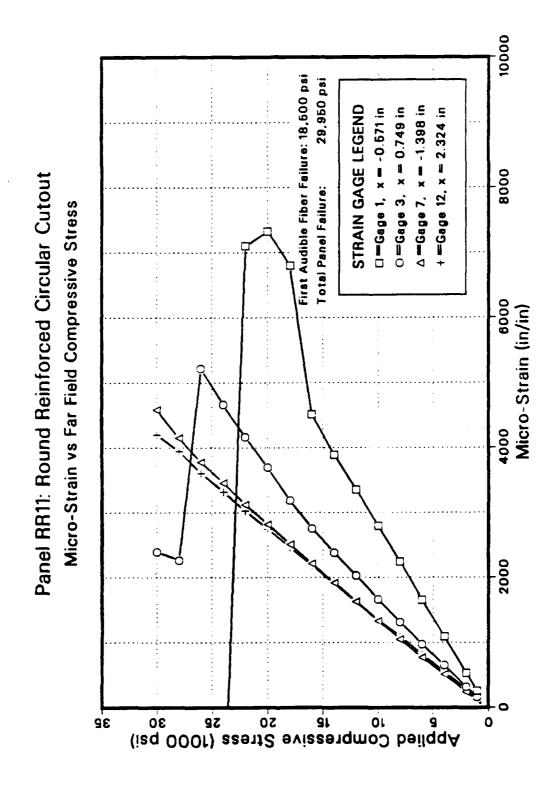


Figure B.4 Panel RR11: Microstrain vs. Compressive Stress.

TABLE XV

PANEL RR11: SELECTED STRAIN GAGE VALUES DURING LOAD.

Load	Micro	c-Strain I	ndicated b	y Gage:
(psi)	#1	#3	# 7	#12
00000000000000000000000000000000000000	25316120373619500 1122338500219500 122338500219500 133500219500 133500	136935256253651946 1369360371616223 1112223344522	-12073 -25073 -13073 -13073 -13073 -13073 -13073 -13073 -1223 -1223 -1223 -13774 -145	-1458 -127886997 -138497 -11620847 -11620847 -122702179 -23336047 -33360432 -33360432

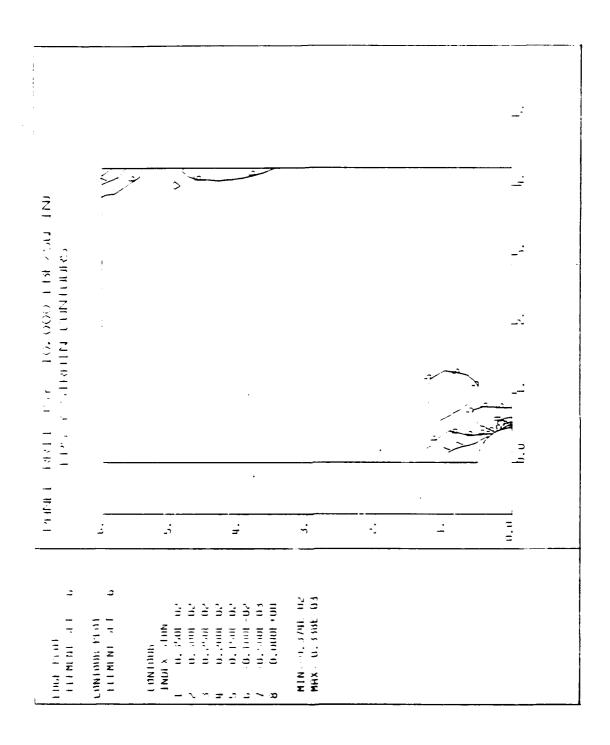


Figure B.5 Panel RR11: Eps-Y FEA Contours.

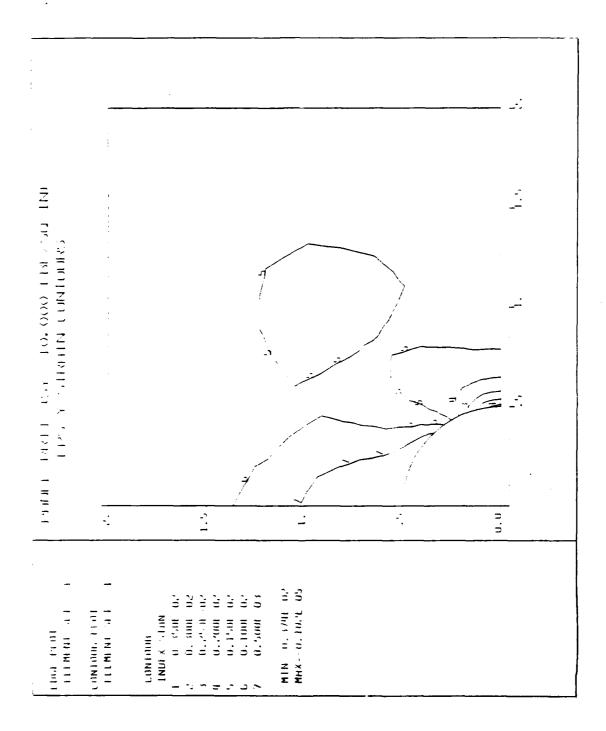


Figure B.6 Panel RR11: Eps-Y FEA Contours Near the Cutout.

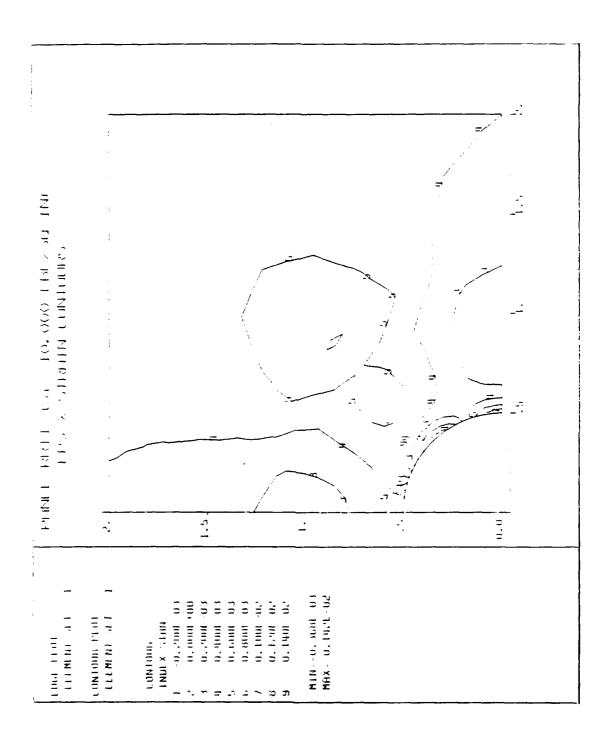


Figure B.7 Panel RR11: Eps-X FEA Contours Near the Cutout.

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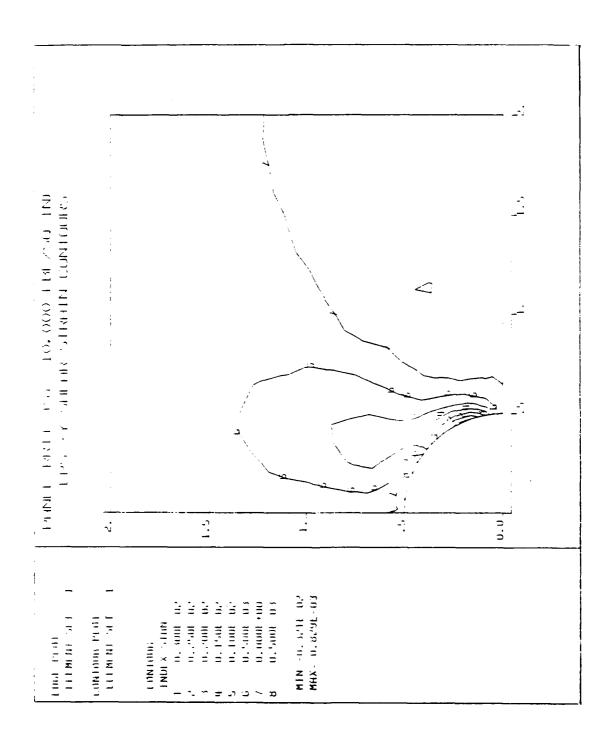


Figure B.8 Panel RR11: Eps-XY FEA Contours Near the Cutout.

APPENDIX C

PANEL RR22: ANALYTICAL AND EXPERIMENTAL DATA

Panel RR22 was reinforced with two round co-cured plies of G/Ep concentric with the cutout on the outside of each facesheet. The reinforcement had the following dimensions:

Shape: Round

Inside Diameter: 1.00 in

Outside Diameter: 2.24 in

Thickness (each): 0.028 in (2 plies)

Area (each face): 3.16 in²

Total Volume: 0.176 in³

Net Cross Section: 0.069 in²

The panel failed by facesheet separation and buckling (Type-2) almost immediately upon initial application of the load. It failed totally at an applied normal compressive stress ($\overline{\sigma}_n$) of -21,050 psi. Based strictly on the failure of the unreinforced panel and the computed stress concentration factor of 2.39, the predicted failure was $\overline{\sigma}_n$ = -38,250 psi. This reinforcement configuration should have been among the most efficient: stacking the most additional thickness closest to the point of highest stress concentration.

The finite element model (mesh) is shown in Figure C.1. The round area of reinforcement is outlined by the heavy lines next to the cutout. The reinforcement is two plies thick on the outside of both facesheets.

Figure C.2 shows the comparison between finite element computed strains around the cutout between the unreinforced panel (PO \emptyset \emptyset) and RR22 at -10,000 psi applied normal stress. Table XVI gives the computed values of the three strains (Eps-Y, Eps-X and Eps-XY) for the reinforced panel.

Figure C.3 compares the analytical (solid and dashed lines) and experimentally measured strain values (triangles) at $\overline{\sigma}_n$ = -10 ksi. The alternating strain gage values between x = 1.0" and 2.5" indicate the small experimental difference between gages on opposite sides of the cutout. While the facesheet separation began at the onset of the load, it covered only a small area and the strain gages were on the opposite side of the panel still giving reasonable indications at $\overline{\sigma}_n$ = -10 ksi. The edge of the reinforcement extended to x = 1.12". This can be seen clearly in Figure C.3 as the point where the strain along the X axis has an inflection point and begins increasing after a steady decrease moving away from the cutout edge. Table XVII gives the (finite element) computed distribution of strains around the cutout in the Y and X directions as well as shear (Eps-Y, Eps-X and Eps-XY).

Figure C.4 shows the stress-strain state during the load sequence from 0 to -20 ksi. Numerical strain gage data are given in Table XVIII. Gages #1, #3 and #4 all indicate a decreasing compressive strain rate with load application. It appears that a facesheet separated from the honeycomb core at or shortly after load application. When this is compared with the strain levels snown in Figure C.3, it appears that significant separation did not occur until after the -10 ksi load level.

Figures C.5 through C.8 show the analytical strain contours at an applied normal compressive stress of -10,000 psi computed and

plotted using DIAL. Figure C.5 is the full quarter panel with strain parallel to the applied load. This shows some strain contours at the top right of the panel illustrating the effect of not loading the full width of the top edge. Figures C.5 through C.8 (Eps-Y, Eps-X and Eps-XY) show the strains in detail close to the cutout.

Panel RR22 should have been the most efficient reinforcement configuration with the best ratio of volume-to-strength. While the volume of reinforcement was small, most of it was concentrated adjacent to the hole in the area of highest stress concentration.

Note: After this research program showed premature panel failure due to facesheet separation, two additional RR22 panels were fabricated by LMSC using identical materials (a different lot, however) and methods. They failed at $\overline{\sigma}_n \approx -41.5$ and -38.0 ksi or an average 104% of the predicted applied normal stress of -38.3 ksi.

PANEL RR22: ROUND REINFORGEMENT PANEL MESH LAYOUT

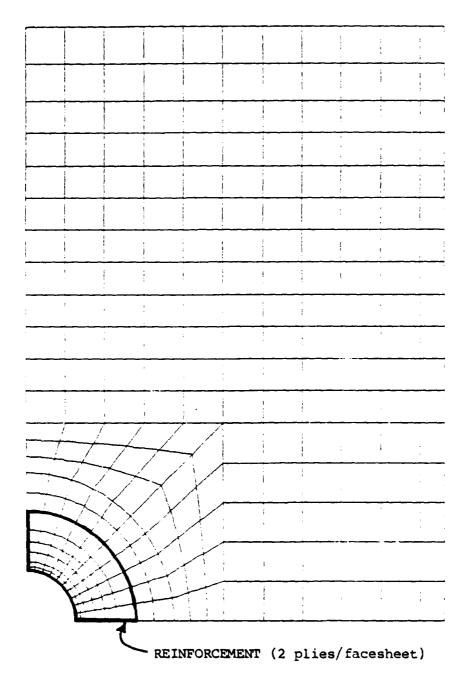


Figure C.1 Panel RR22: DIAL Finite Element Mesh.

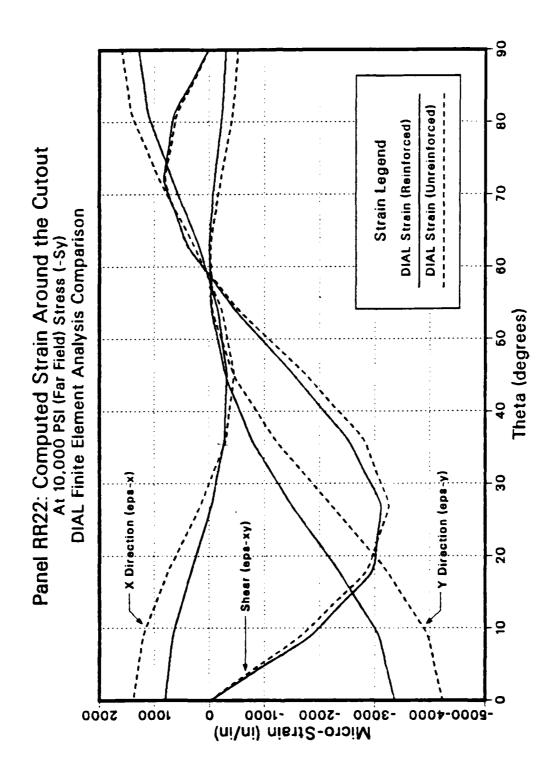


Figure C.2 Panel RR22: Strain Comparison Around the Cutout.

TABLE XVI

PANEL RR22: LEFEA STRAIN DISTRIBUTION AROUND THE CUTOUT (-10,000 PSI).

•	EPS-XX	00000000000000000000000000000000000000	0.28.178.00 0.31138-0 0.320458-0 0.29658-0 0.241688-0 0.92868-0 0.92868-0
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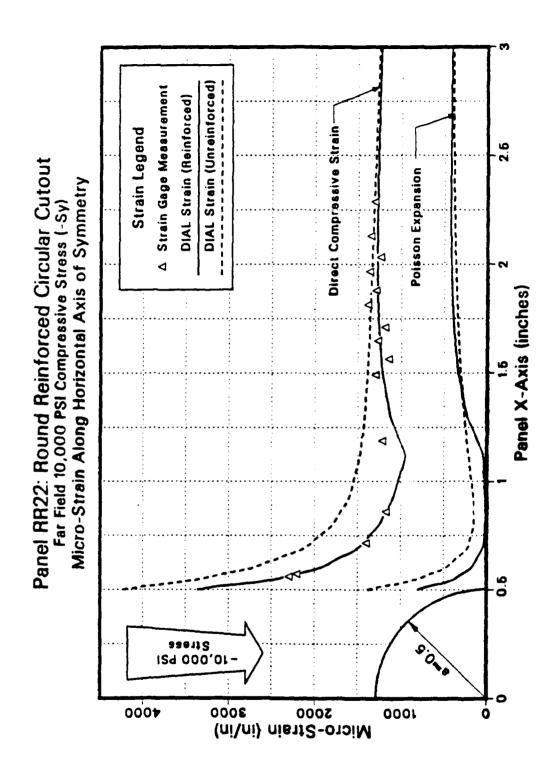


Figure C.3 Panel RR22: Strain Comparison Along the X Axis.

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TABLE XVII

PANKI, RR22, LEPKA STRAIN DISTRIBUTION ALONG THE X AXIS (-10,000 PSI).

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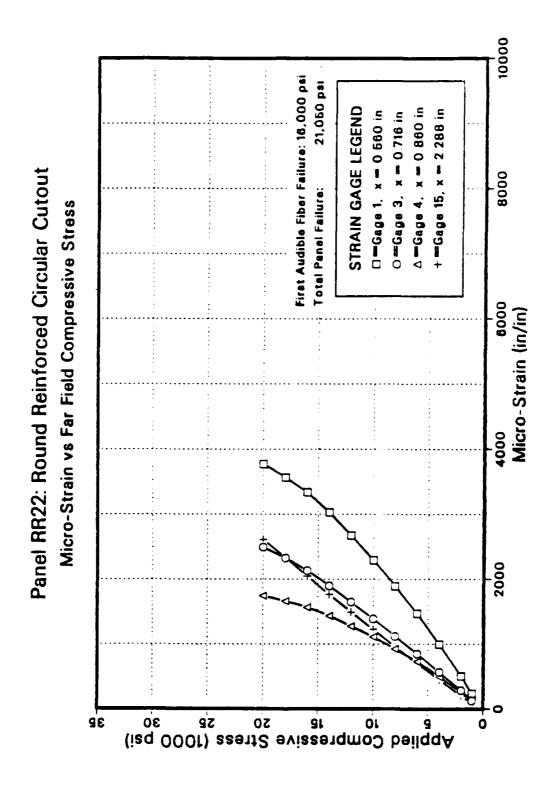


Figure C.4 Panel RR22: Microstrain vs. Compressive Stress.

TABLE XVIII

PANEL RR22: SELECTED STRAIN GAGE VALUES DURING LOAD.

Load	Micro	-Strain	Indicated h	y Gage:
(psi)	#1	#3	# 4	#15
1000 2000 4000 6000 10000 12000 14000 18000 20000	- 1223345 - 159970 - 149970 - 118296625 - 122233567 - 33577	-12860 -12860 -1384037 -11369329 -12349 -12349	-120 -253 -7299 -7224 -11277 -114661 -1742	-75 -2049 -79605 -79625 -12966 -12966 -123608

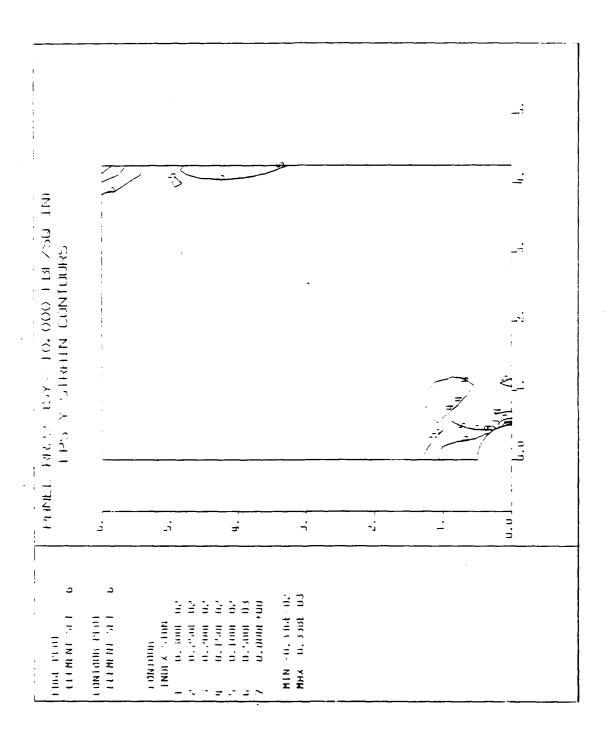
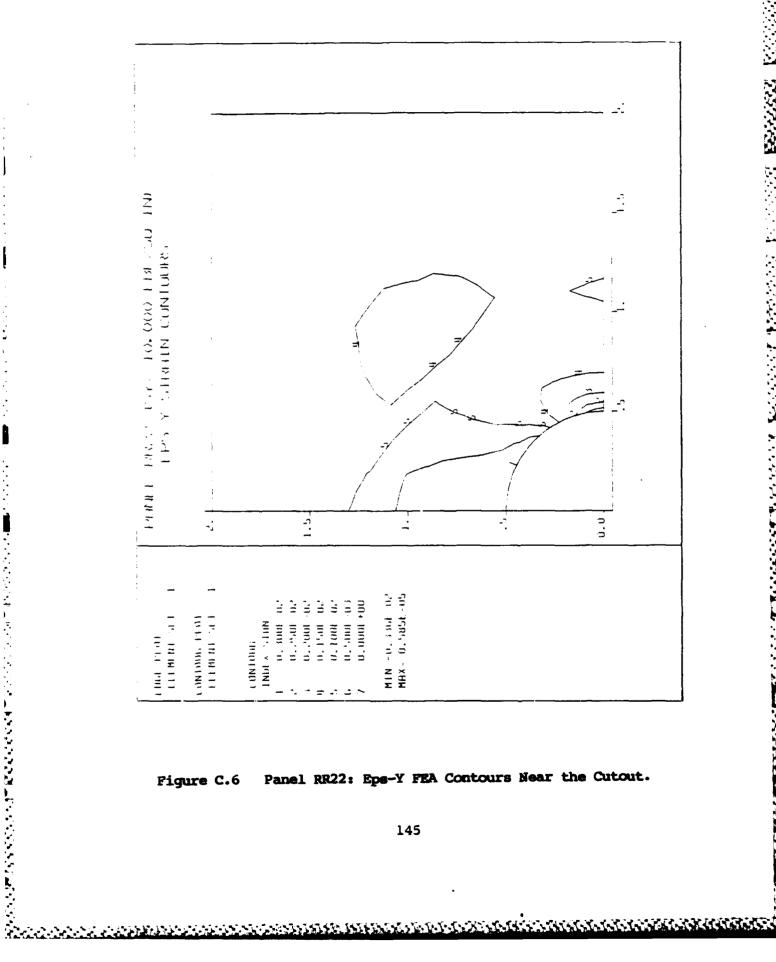


Figure C.5 Panel RR22: Eps-Y FEA Contours.



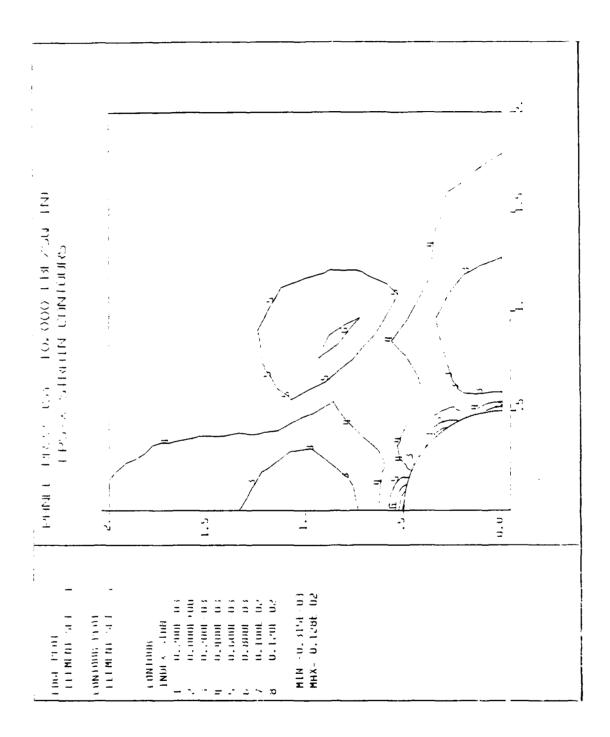


Figure C.7 Panel RR22: Eps-X FEA Contours Near the Cutout.

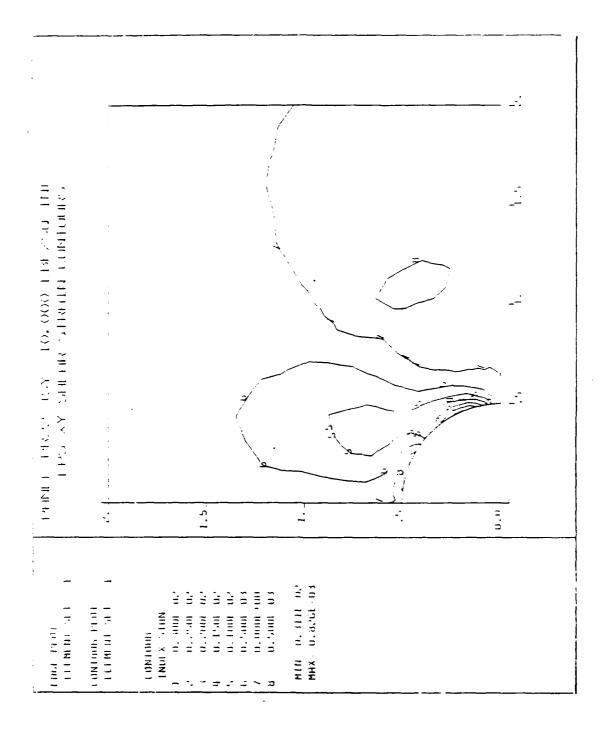


Figure C.8 Panel RR22: Eps-XY FEA Contours Near the Cutout.

APPENDIX D

PANEL RR31: ANALYTICAL AND EXPERIMENTAL DATA

Panel RR31 was reinforced with one round co-cured ply of G/EP around the cutout on the outside of each facesheet. The reinforcement had the following dimensions:

Snape:	Round			
Inside Diameter:	1.00	in		
Outside Diameter:	3.60	in		
Thickness (each):	0.014	in	(1	ply
Area (each face):	9.39	in^2		
Total Volume:	0.263	in ³		
Net Cross Section:	0.073	in^2		

The panel failed at the hole edge (Type-1) at an applied normal stress (σ_n) of -28,000 psi, only about 78% of that expected. Based strictly on the failure of the unreinforced panel and the computed stress concentration factor of 2.56 the predicted failure was $\overline{\sigma}_n$ = -35,700 psi.

The finite element model (mesh) is shown in Figure D.1. The area of round reinforcement is denoted by the area inside the bold outline around the cutout.

Figure D.2 compares the analytical values of strain around the cutout from $\theta=0^{\circ}$ to 90° between the unreinforced panel (POØØ) and RR31 in the Y and X directions as well as shear (Eps-Y, Eps-X and Eps-XY). Table XIX lists these computed strains around the cutout.

Figure D.2 compares the finite element model (lines) and the experimentally measured strain data (triangles) of strain at $\overline{\sigma}_n$ = -10,000 psi. It shows an almost perfect correlation between the analytically predicted and experimentally measured strain. The edge of the reinforcement extended to 1.80" in on the X axis. This is apparent from the figure as the slight inflection point where the strain begins increasing slightly. The computed strain field in an unreinforced panel (POØØ) is shown as dashed lines (Eps-Y & Eps-X). Table XX gives the values of the computed strain in the Y and X directions as well as shear.

Figure D.4 shows the stress-strain relation during the load sequence from 0 to -28 ksi. Experimentally measured strain gage values are given in Table XXI. Other than a minor "glitch" at $\overline{\sigma}_{\rm n}$ = -21 ksi, no exceptional anomalies were noted. Gage #3 at x = -0.770" showed little increase in strain between -21 and -22 ksi. This is not reflected in any of the other gage readings.

Figures D.5 through D.8 show the strain contours at an applied normal stress of -10,000 psi computed and plotted using DIAL. Figure D.5 is the full quarter panel with strain parallel to the applied load. As before, the strain contours at the top right of the panel are due to the effect of not loading the full width of the top edge. Figures D.6 through D.3 (Eps-Y, Eps-X and Eps-XY) show the strains in detail close to the cutout.

PANEL RR31: ROUND REINFORGEMENT PANEL MESH LAYOUT

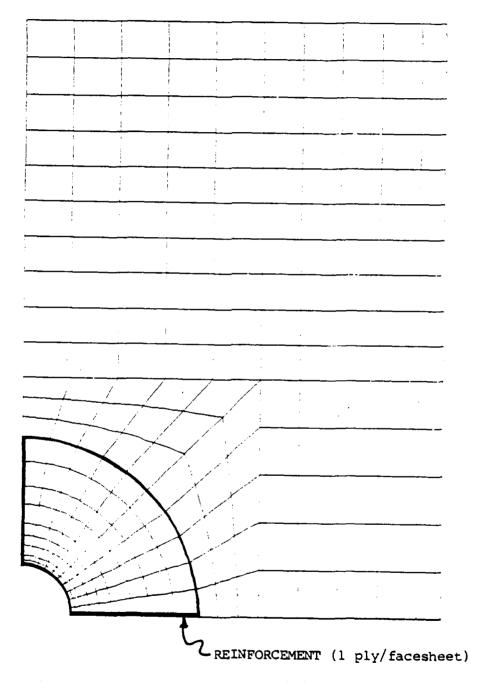


Figure D.1 Panel RR31: DIAL Finite Element Mesh.

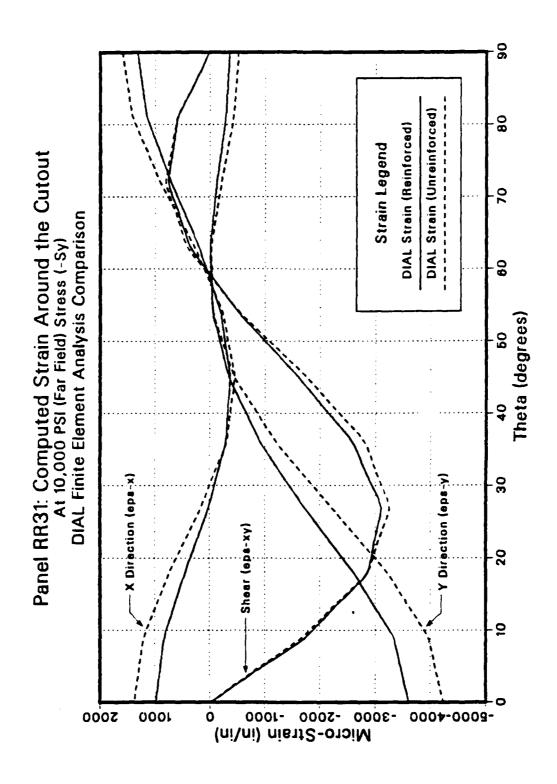


Figure D.2 Panel RR31: Strain Comparison Around the Cutout.

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PANEL RR31: LEPEA STRAIN DISTRIBUTION AROUND THE CUTOUT (-10,000 PSI).

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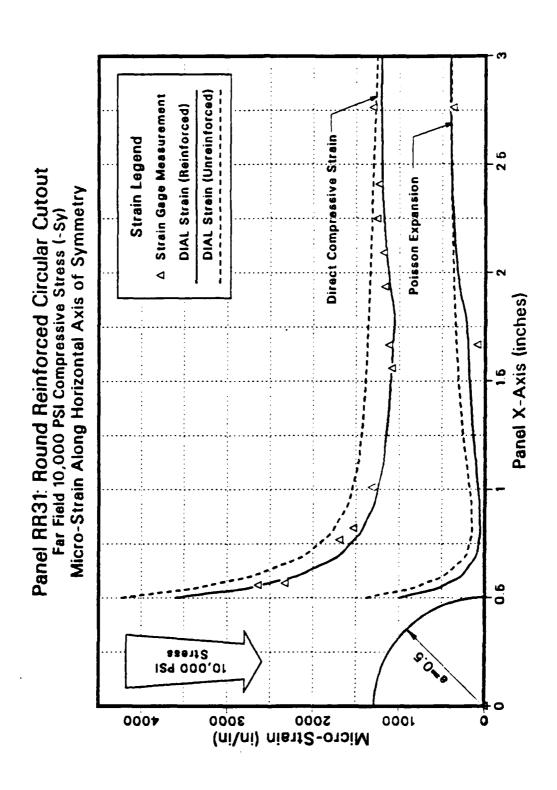


Figure D.3 Panel RR31: Strain Comparison Along the X Axis.

TABLE XX

PANEL RR31: LEPEA STRAIN DISTRIBUTION ALONG THE X AXIS (-10,000 PSI).

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EPS-Y	00000000000000000000000000000000000000
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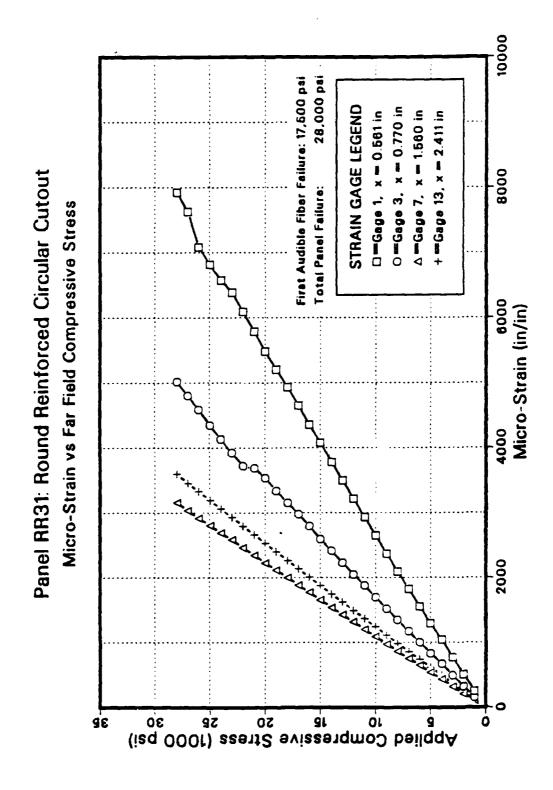
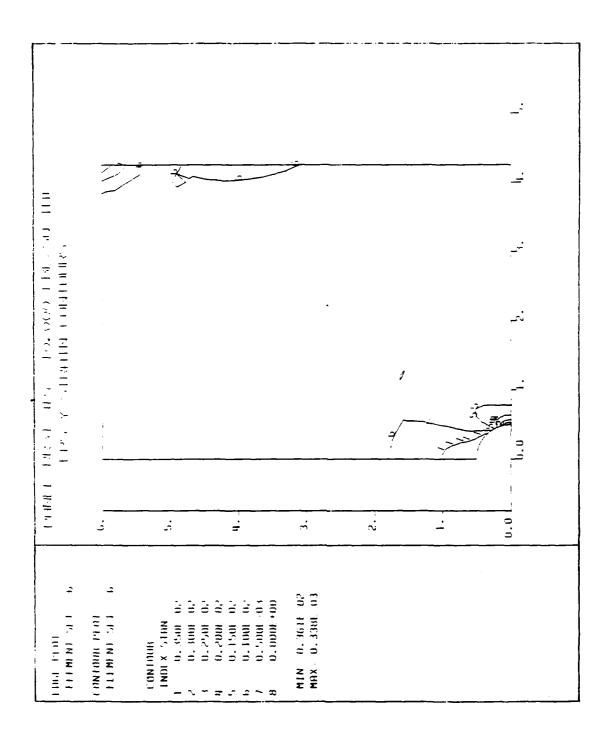


Figure D.4 Panel RR31: Microstrain vs. Compressive Stress.

TABLE XXI

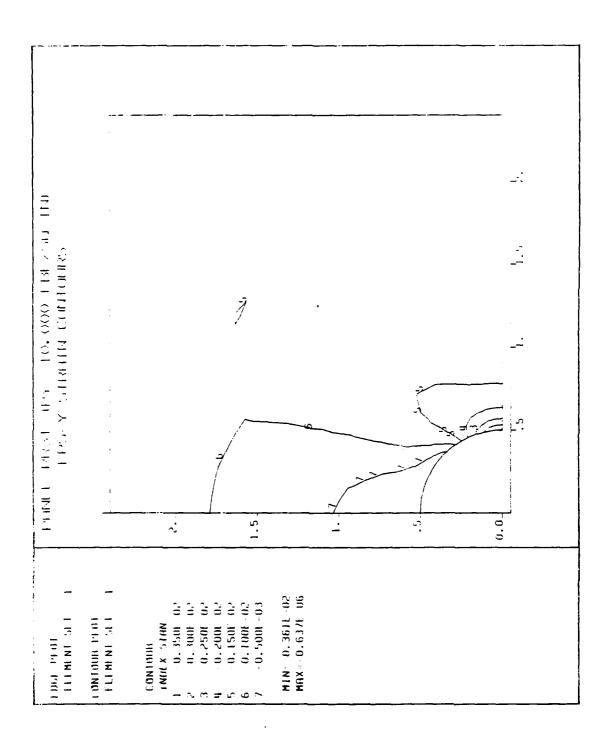
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RR31: SELECTED	Mic #1	MUNICACE TO THE TELL TELL TELL TELL TELL TELL TELL
PANEL	Load (PSI)	00000000000000000000000000000000000000



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Figure D.5 Panel RR31: Eps-Y FEA Contours.



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Figure D.6 Panel RR31: Eps-Y FEA Contours Near the Cutout.

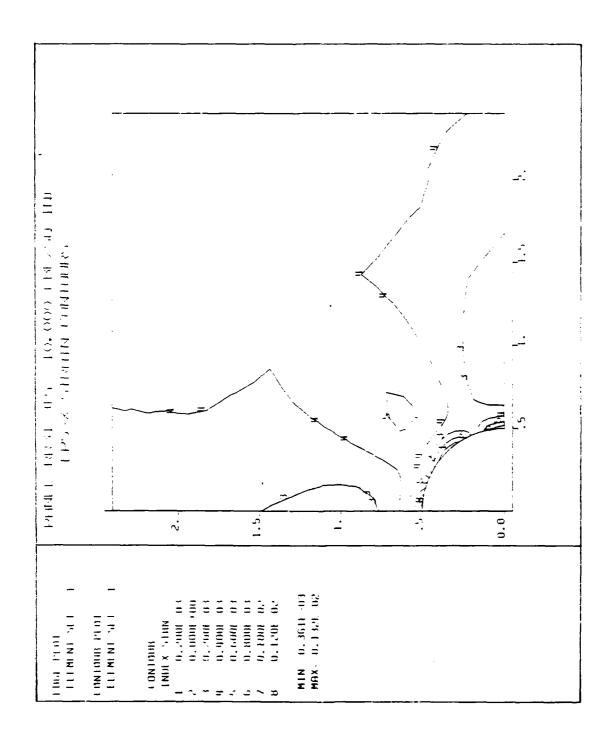


Figure D.7 Panel RR31: Eps-X FEA Contours Near the Cutout.

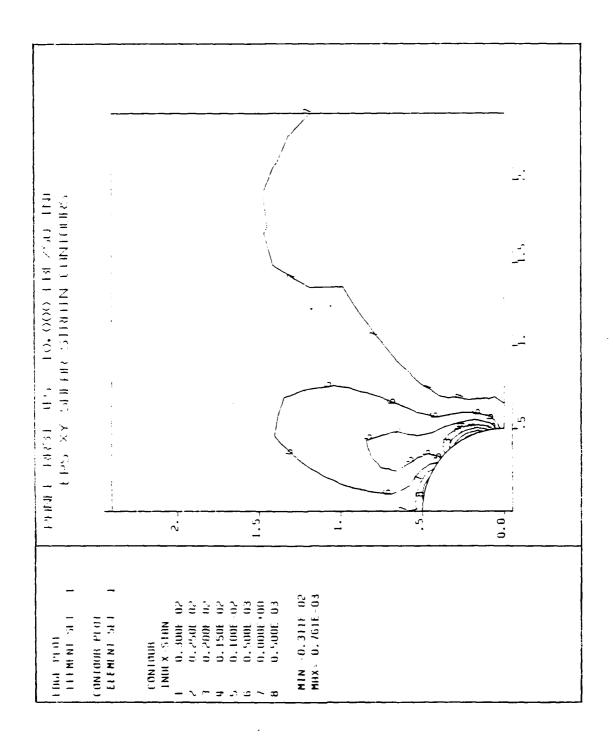


Figure D.8 Panel RR31: Eps-XY FEA Contours Near the Cutout.

APPENDIX E

PANEL RR42: ANALYTICAL AND EXPERIMENTAL DATA

Panel RR42 was reinforced with one co-cured ply of G/EP concentric with the cutout on the outside of each facesheet. The reinforcement had the following dimensions:

Shape: Round

Inside Diameter: 1.00 in

Outside Diameter: 3.00 in

Thickness (each): 0.028 in (2 ply)

Area (each face): 6.28 in²

Total Volume: 0.176 in³

Net Cross Section: 0.112 in²

The panel failed by facesheet separation and buckling (Type-2) at an applied normal stress ($\overline{\sigma}_n$) of -13,500 psi, less that 34% of the expected value. Based strictly on the failure of the unreinforced panel and the computed stress concentration factor of 2.29 for RR42, the predicted panel failure was $\overline{\sigma}_n$ = -40,000 psi.

The finite element model (mesh) is shown in Figure E.l. The area of round reinforcement is denoted by the area inside the bold outline around the cutout.

Figure E.2 compares the LEFEA values of strain around the cutout between the unreinforced panel (POØØ) and RR42 in the Y and X directions as well as shear (Eps-Y, Eps-X and Eps-XY). Table XXII lists these computed strains around the cutout.

Figure E.3 compares the finite element model (lines) and the experimentally measured strain data (triangles) of strain at $\overline{\sigma}_n$ = -10,600 psi. It shows very poor correlation between the analytically predicted and measured strain. At least one face-sheet separated from the honeycomb core over a significant area prior to the -10 ksi test point. The strain field at that applied stress was little more than 80% of that predicted. The computed strain field in an unreinforced panel (POØØ) is shown as dotted lines (Eps-Y & Eps-X). Table XXIII gives the values of the LEFEA computed strain in the Y and X directions as well as in shear.

Figure E.4 shows the stress-strain relation during the load sequence from σ_n = 0 to -21.9 ksi (failure). Measured strain gage values are given in Table XXIV. The strain, particularly in gages #3, #8 and #14, indicate that the panel stiffness decreased from the initiation of the load. The notable difference in slope between gages #3, #8 and #14 and gage #1 next to the cutout indicate that the separation "bubble" occurred away from the cutout. Failure seemed to occur when the bubble's edge reached the cutout.

This type of failure probably indicates that at least one facesheet was improperly bonded to the honeycomb core. Non-destructive inspection before and after testing did not indicate unbonded areas between the facesheet and the core. I suspect, in this and other panels that failed in a similar manner, that the adhesive was in place but either weak from an improper mixing or aging or was applied too thinly.

Figures E.5 through E.8 show the strain contours at an applied normal stress of -10,000 psi computed and plotted using DIAL. Figure E.5 is the full quarter panel with strain parallel to the

applied load. As before, the strain contours at the top right of the panel are due to the effect of not loading the full width of the top edge. Figures E.6 through E.8 (EPS-Y, EPS-X and EPS-XY) show the strains in detail close to the cutout.

PANEL RR42 PANEL MESH LAYOUT

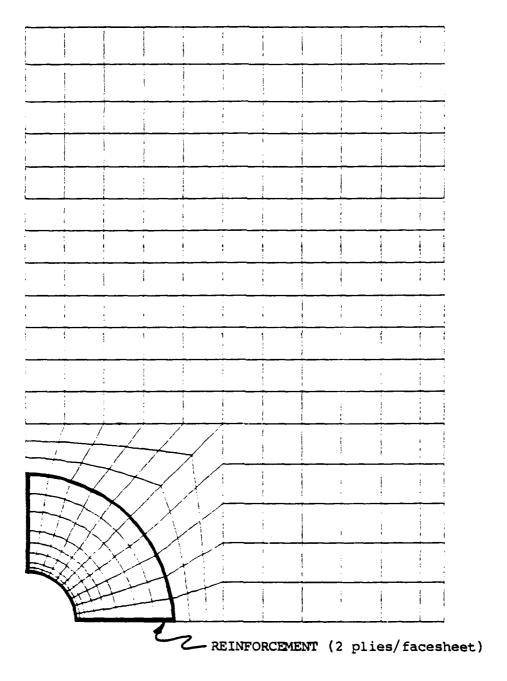


Figure E.1 Panel RR42: DIAL Finite Element Mesh.

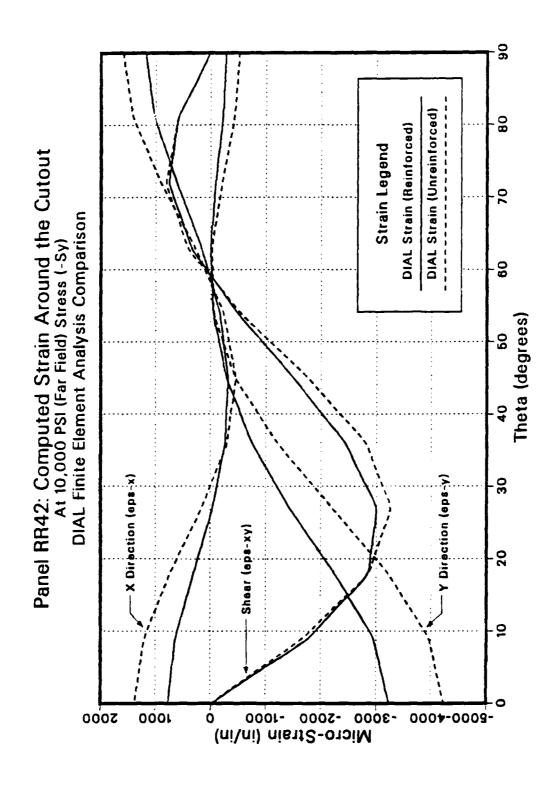


Figure E.2 Panel RR42: Strain Comparison Around the Cutout.

TABLE XXII

(-10,000 PSI).	EPS-XY	00000000000000000000000000000000000000
THE CUTOUT (-10	FPS-X	00000000000000000000000000000000000000
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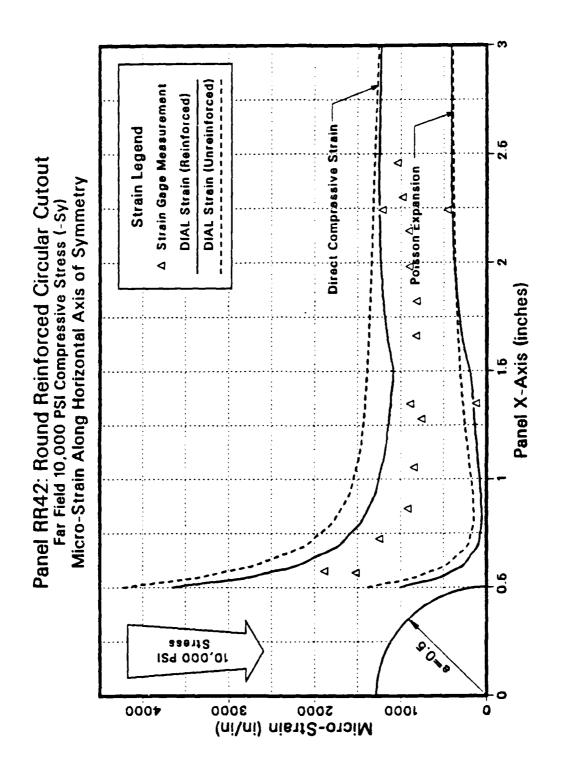


Figure E.3 Panel RR42: Strain Comparison Along the X Axis.

TABLE XXIII

PANKL RR42: LEFRA STRAIN DISTRIBUTION ALONG THE X AXIS (-10,000 PSI).

EPS-XY	.2726E- 1631E- 3055E-	0.1159E- 0.8493E- 0.6765E-	0.1525E-0 0.1566E-0 0.1899E-0	.2332E- .2485E-	2447E-3185E-3769E-	- 14 56E-	67.55 67.55 67.65 68.55	8086E- 9726E-	4025E-	.8002E- 3700E-	0.2069E- 0.8925E-	.6176E-	10 14 30E -	0.1574E-
EPS-X	. 77 50 E - 0 . 56 27 E - 0 . 35 58 E - 0	. 27 48E-0 . 17 73E-0 . 10 40E-0	0.3831E-04 0.2687E-04 0.1188E-04	- 16 10E-0 - 1988E-0 - 3851E-0	. 5719E-0 . 7389E-0 . 9012E-0	10 38E-0	. 26 (5E-0 . 29 9 1E-0	3375E-0 3604E-0	. 4073E-0	. 4237E-0 . 4229E-0	- 4157E-0 - 4050E-0	0-36-66 0-378-66 0-38-66-66	3834E-0 1 部24E-0	. 38 19E-0
EPS-Y	0.3231E-3 0.2778E-0 0.2340E-0	0.2126E-0 0.1890E-0 0.1658E-0	-0.14428-02 -0.13458-02 -0.12418-02	0.11/4E-3 0.1106E-0 0.1049E-0	0.99458-0 0.96748-0 0.93878-0	0.9142E-0	0.1020E-0	0.1107E-0	0. 1190E-0	0.1214E-0	0. 1206E-0 0. 1198E-0	0.1180E-0	0.1168E-0	0. 1168E-0
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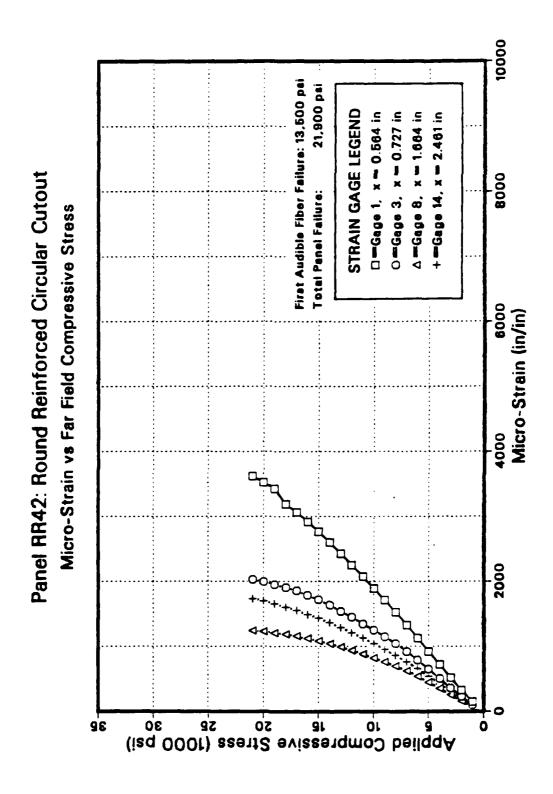


Figure E.4 Panel RR42: Microstrain vs. Compressive Stress.

TABLE XXIV

PANEL RR42: SELECTED STRAIN GAGE VALUES DURING LOAD.

Load	Micro-S	Strain Indi	cated by G	age:		
(psi)	# 1	#3	#8	#14		
1233456789000000000000000000000000000000000000	376705720030534753720 13579135780246768222 111578024679014333336 111112222223333333	47125898608604485253 92604813454443185059 123567901234567789999 1-1-1-1-1-1-1-1-1-1	39. 1.1 + 1. 1.339.4153.630.9 -123456678899.00111122 -1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-	4763741019203322933 790235665333196394405 11345678901223445666 111111111111111111111111111111111		
21000	- 36 20	-2025	-1241	-1698 -1732		

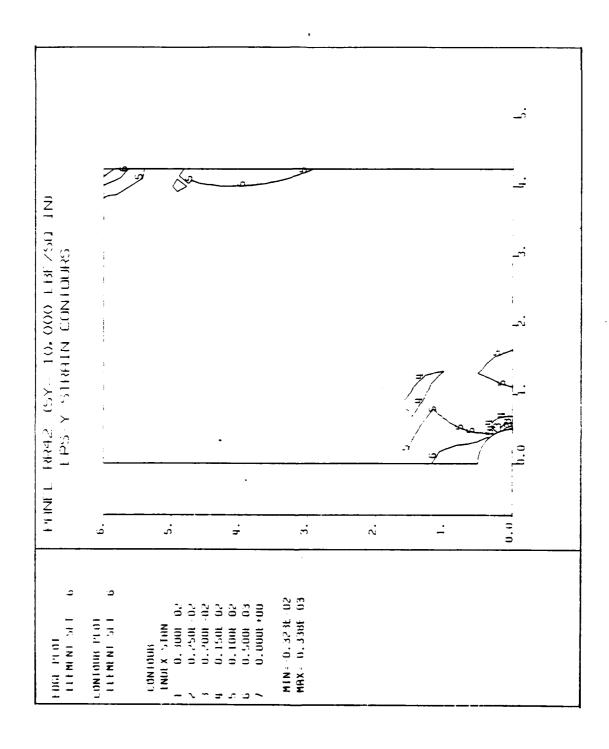


Figure E.5 Panel RR42: Eps-Y FEA Contours.

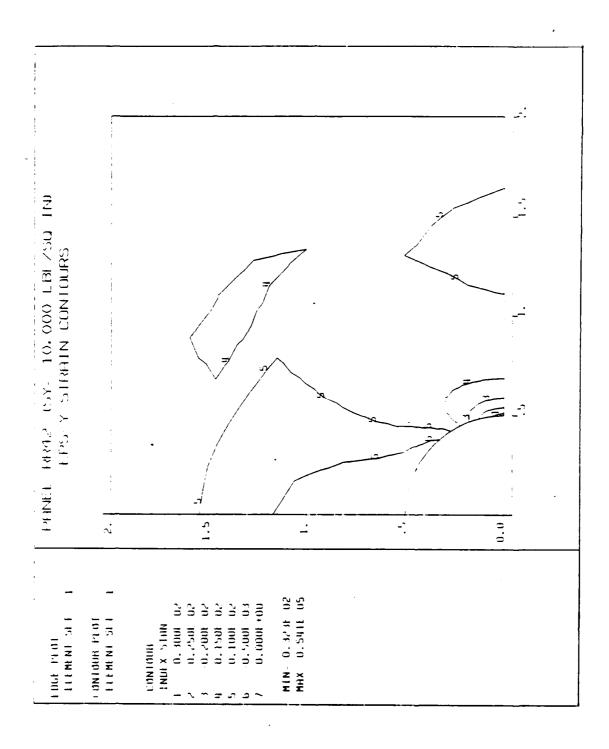


Figure E.6 Panel RR42: Eps-Y FEA Contours Near the Cutout.

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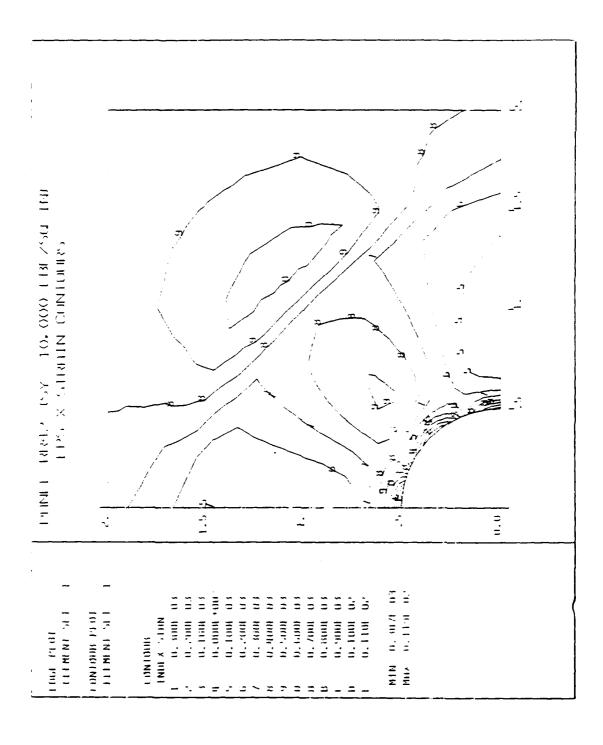


Figure E.7 Panel RR42: Eps-X FEA Contours Near the Cutout.

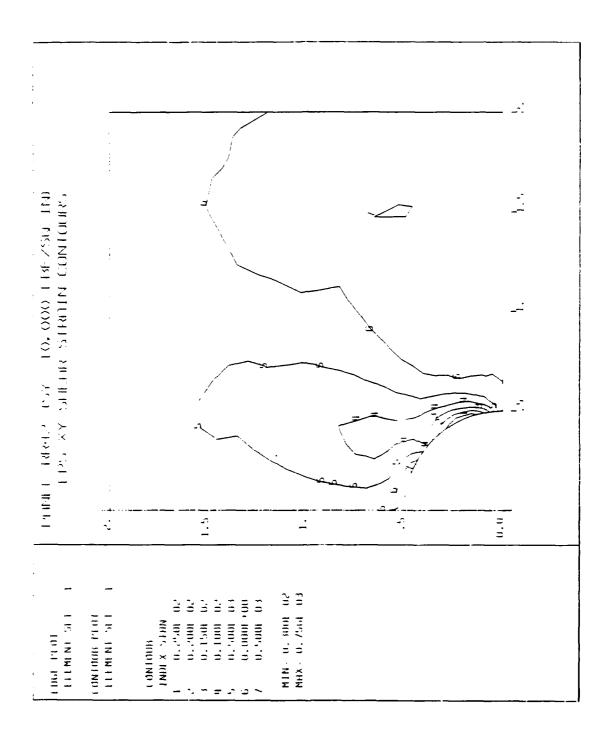


Figure E.8 Panel RR42: Eps-XY FEA Contours Near the Cutout.

APPENDIX F

PANEL RR51: ANALYTICAL AND EXPERIMENTAL DATA

Panel RR51 was reinforced with one round co-cured ply of G/Ep in a concentric with the cutout placed on the outside of each facesheets. The reinforcement had the following dimensions:

Round

Inside Diameter: 1.00 in

Outside Diameter: 4.60 in

Thickness (each): 0.014 in (1 ply)

Area (each face): 15.83 in²

Total Volume: 0.443 in³
Net Cross Section: 0.101 in²

Snape:

The panel failed by facesheet separation and buckling (Type-2') and was taken only to an applied normal stress of -16,000 psi, not to total failure. The series of premature panel failures due to facesheet separation required an intact panel for testing. Subsequent non-destructive testing showed the separation, but could not determine the reason for it. It is suspected that the adhesive, while properly applied, was not properly mixed or was overage. Based strictly on the failure of the unreinforced panel and the computed stress concentration factor of 2.51, failure was predicted at about $\overline{\sigma}_{\Omega}$ = -36,400 psi.

The finite element model (mesh) is shown in Figure F.1. The 15.83 square inch area of the one-ply reinforcement is outlined by the bold lines next to the cutout.

Figure F.2 compares the three (finite element) computed strains around the cutout between the unreinforced panel (POØØ) and RR51. These computed strain values are listed in Table XXV. Note the very significant decrease in the strain due to the reinforcement at the point of highest stress concentration ($\theta = 0^{\circ}$) compared to the unreinforced panel. A significant decrease in all three strains can be seen around the hole from 0 to 90 degrees.

Figure F.3 compares the LEFEA computed (solid and dashed lines) and experimental strains (triangles) in the Y and X (poisson expansion) directions in the panel and shows that there was a great disparity between opposite sides of the hole on the same facesheet. One side showed much higher strain than predicted at $\sigma_{\Omega} = -10,000$ psi. This is due to load transfer from the side with the buckled facesheet. The edge of the reinforcement can be seen in the figure by the very slight inflection point at x = 2.3". The effects of the one-ply reinforcement is apparent in the far-field as a significant decrease in computed Eps-Y compared to the unreinforced panel (POØØ). Table XXVI gives the computed values of the strains along the X axis.

Figure F.4 shows the stress-strain state during the load sequence from 0 to -16 ksi. Experimentally measured strain gage values are given in Table XXVII. Gage #1 and #4, on either side of the hole, show a positive slope of the derivative $\Delta\sigma/\Delta\varepsilon$. This is unusual and indicates some panel-honeycomb separation close to the hole.

Figures F.5 through F.8 show the strain contours at an $\overline{\sigma}_n =$ -10,000 psi computed and plotted using DIAL. Figure F.5 is the full quarter panel with strain (Eps-Y) parallel to the applied

load. Figures F.6 through F.8 (Eps-Y, Eps-X and Eps-XY) show the strains in detail close to the cutout.

The result of the wide reinforcement is to effect a thicker overall panel. A separate LEFEA of a $[0_2, +45, 90, \overline{\text{core}}]_s$ panel without reinforcement had an almost identical strain field near the cutout.

PANEL RR51 PANEL MESH LAYOUT

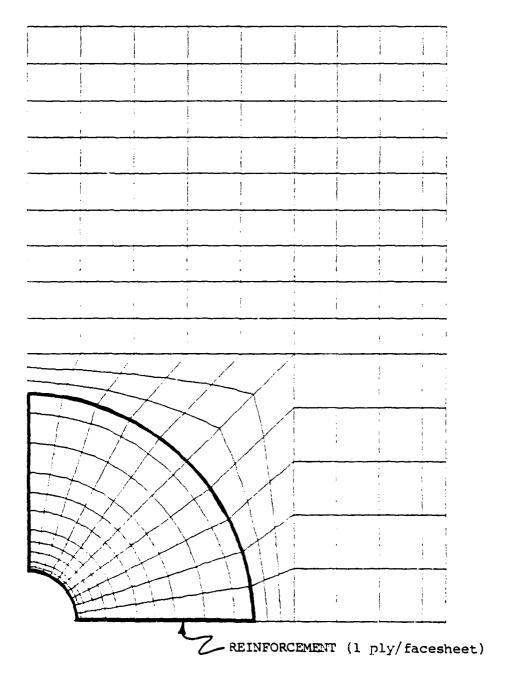
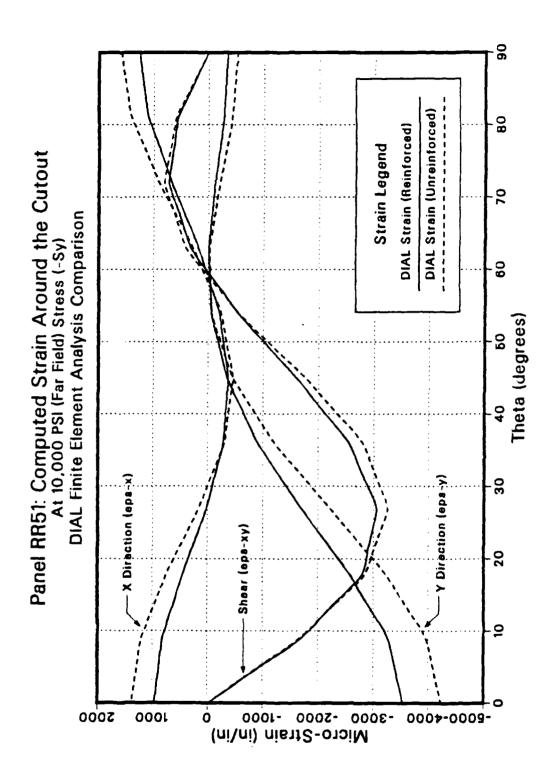


Figure F.1 Panel RR51: DIAL Finite Element Mesh.



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Figure F.2 Panel RR51: Strain Comparison Around the Cutout.

TABLE XXV

PAMEL RR51: LEFEA STRAIN DISTRIBUTION AROUND THE CUTOUT (-10,000 PSI).

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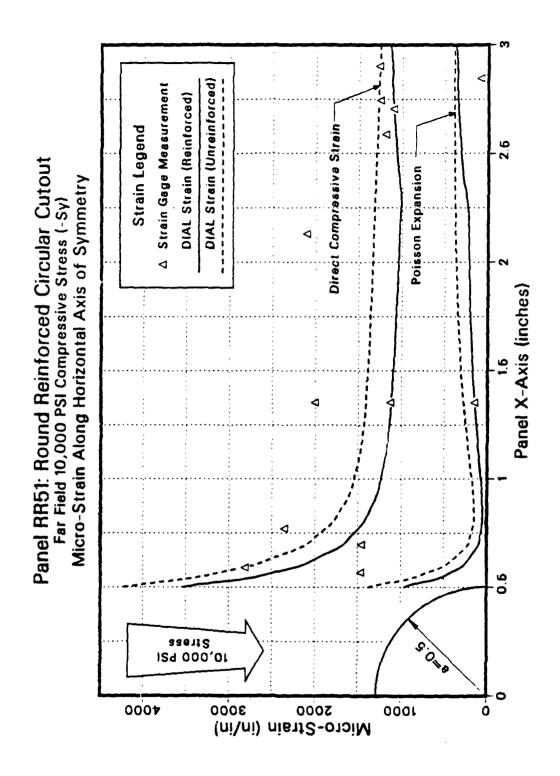


Figure F.3 Panel RR51: Strain Comparison Along the X Axis.

TABLE XXVI

(-10,000 PSI).	14	サンド・マー りょうしゅう りょうけん ちゅうしょう しゅうしゅうしゅうしゅう かんしゅう しゅうしゅう しゅう
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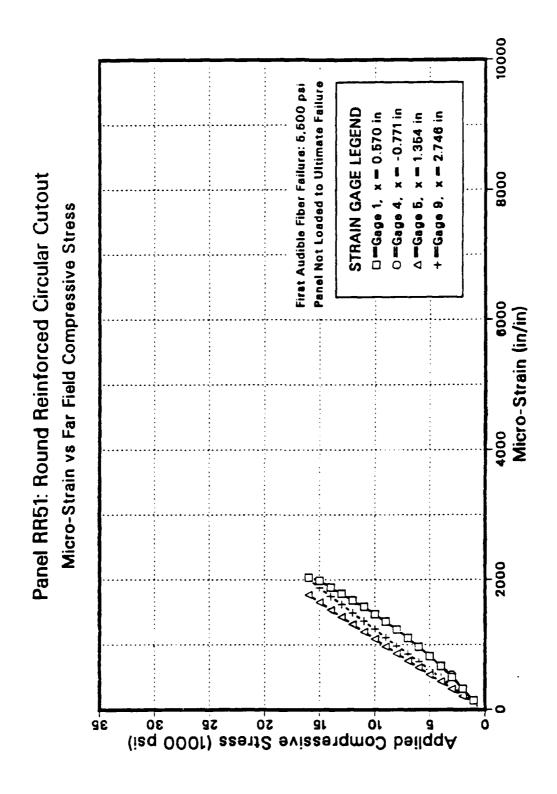


Figure F.4 Panel RR51: Microstrain vs. Compressive Stress.

TABLE XXVII

PANEL RR51: SELECTED STRAIN GAGE VALUES DURING LOAD.

Load	Micro	-Strain I	ndicated by	gage:
(psi)	#1	# 4	# 5	#9
10000000000000000000000000000000000000	- 13197 - 13197 - 13197 - 13197 - 16891 - 11235 - 115688 - 115688	72400332773443282 -135689123568889883 -112345678983 -112345678983	-12345.6789056979 -12345.6789056979 -112345.678912356	-117 -236941 -3691157 -4673571 -898098 -1123641 -1134918 -1167476

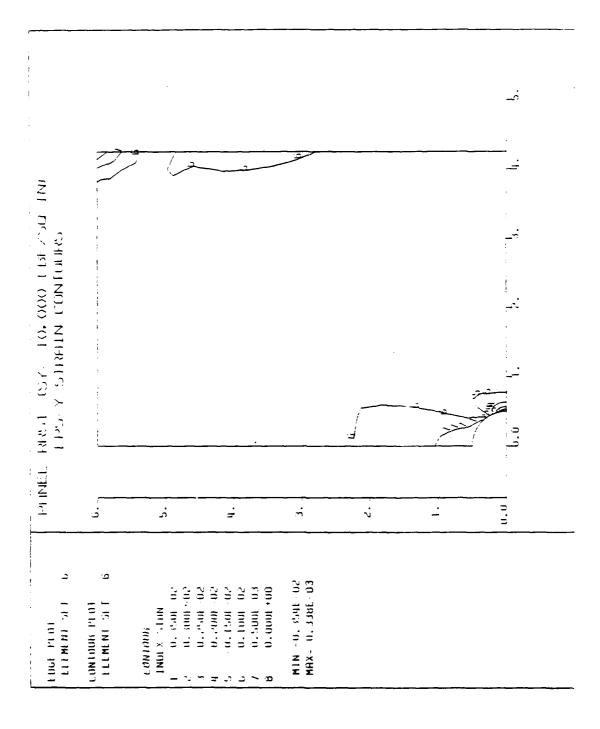
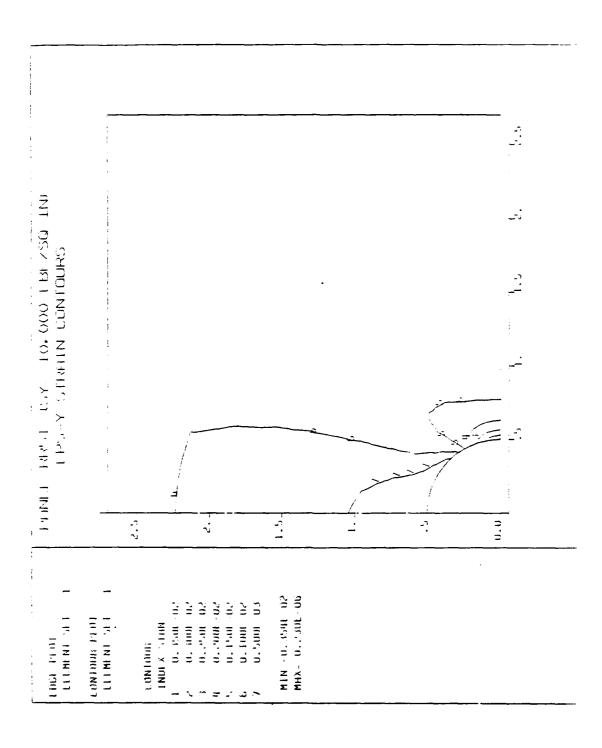


Figure F.5 Panel RR51: Eps-Y FEA Contours.



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Figure F.6 Panel RR51: Eps-Y FEA Contours Near the Cutout.

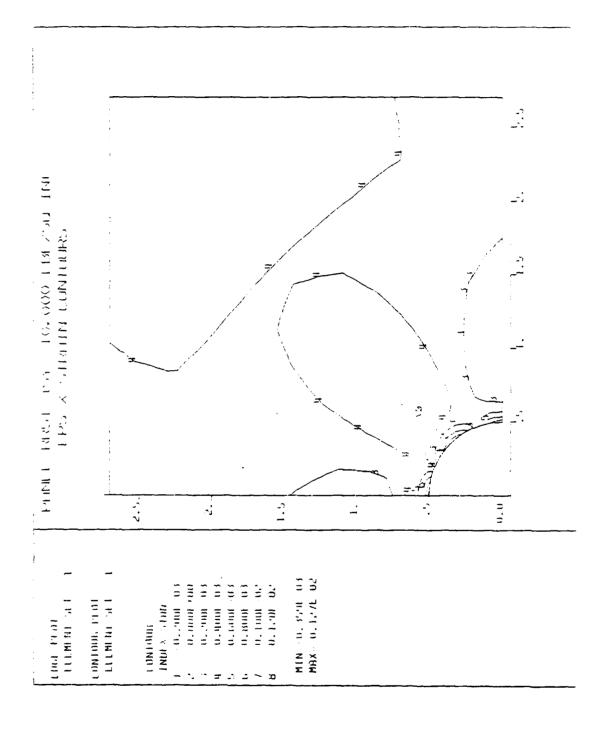


Figure F.7 Panel RR51: Eps-X FEA Contours Near the Cutout.

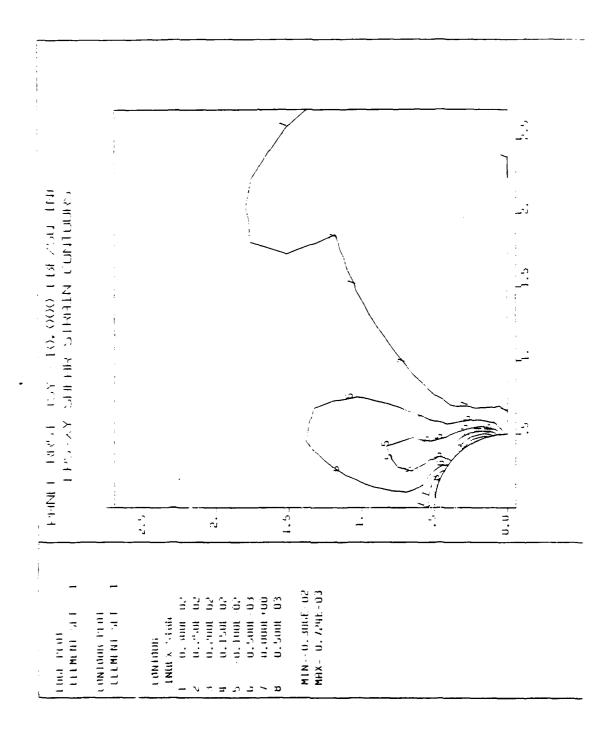


Figure F.8 Panel RR51: Eps-XY FEA Contours Near the Cutout.

APPENDIX G

PANEL RS11: ANALYTICAL AND EXPERIMENTAL DATA

Panel RS11 was reinforced with one square co-cured ply of G/Ep concentric with the cutout on the outside of each facesheet. The reinforcement had the following dimensions:

Shape:	Square	=		
Inside Diameter:	1.00	in		
Length & Width:	2.00	in		
Thickness (each):	0.014	in	(1	ply)
Area (each face):	3.22	in^2		
Total Volume:	0.088	in^3		
Net Cross Section:	0.028	in^2		

The panel failed at the hole edge (Type-1) at an applied normal stress of -31,000 psi, about 90% of the load predicted. Based strictly on the failure of the unreinforced panel and the computed stress concentration factor of 2.64, the predicted failure was $\overline{\sigma}_n$ = -34,600 psi.

The finite element model (mesh) is shown in Figure G.l. The square area of reinforcement is denoted by the heavy outline around the cutout.

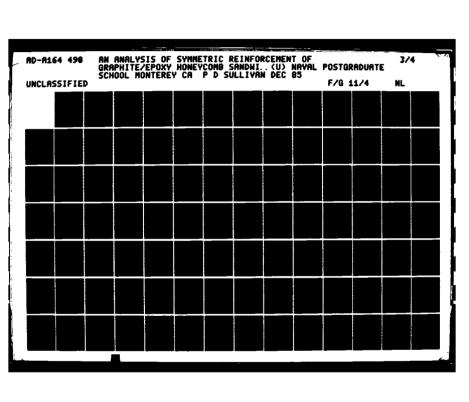
Figure G.2 compares the three (finite element) computed strains around the cutout between the unreinforced panel (POØØ) and RS11. These computed strain values are listed in Table XXVIII.

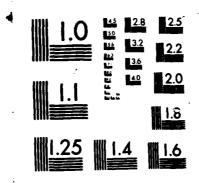
Figure G.3 compares the computed (solid and dashed lines) and experimentally measured (triangles) strain along the X axis in the Y and X (poisson expansion) directions in the panel and shows the excellent correlation between analytical and experimental strain at $\overline{\sigma}_n = -10,000$ psi. There was some minor strain variation between the left and right sides of the hole. Both are represented in the figure as strain gage values on the right side. The difference was small, but visible. The outside edge of the reinforcement can be seen in the figure as an inflection point in the direct compressive strain where it begins increasing at x = 1.1". Table XXVIX gives the computed values of the strain along the X axis.

Figure G.4 is the stress-strain state during the load sequence from $\overline{\sigma}_n = 0$ to -30 ksi. Experimentally measured strain values are given in Table XXX. Up to about -20 ksi the gage next to the hole (x = +0.561) shows an almost linear stress-strain relation. Gage #4 at x = -0.737" shows the expected degree of loss in local stiffness up to -20 ksi (see Table VI, Figure 5.4 and section III A.1 for a discussion). Gage #1 indicates, starting at about -20 ksi, what at first appears to be a slow but continuous increase in local stiffness indicated by a decreasing strain rate. At corresponding stress values gage #4 indicates an increasing strain rate. These gages were on opposite sides of the panel. What is actually happening is that $\overline{\sigma}_n = -28$ ksi the right side of the panel is showing significant matrix degradation and the load is being transferred to the left side of the panel next to the cutout. Gage #1 is propably not indicating the true state of strain under its grid. Since the panel was evenly loaded and well constrained

the strain at each side of the cutout 90° to the applied load should have been almost identical up to failure.

Figures G.5 through G.8 show the strain contours at $\overline{\sigma}_n =$ -10,000 psi computed and plotted using DIAL. Figure G.5 is the full quarter panel with strain (Eps-Y) parallel to the applied load. Figures G.6 through G.8 (Eps-Y, Eps-X and Eps-XY) show the strains in detail close to the cutout.





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PANEL RS11 SQUARE REINFORGEMENT PANEL MESH LAYOUT

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Figure G.1 Panel RS11: DIAL Finite Element Mesh.

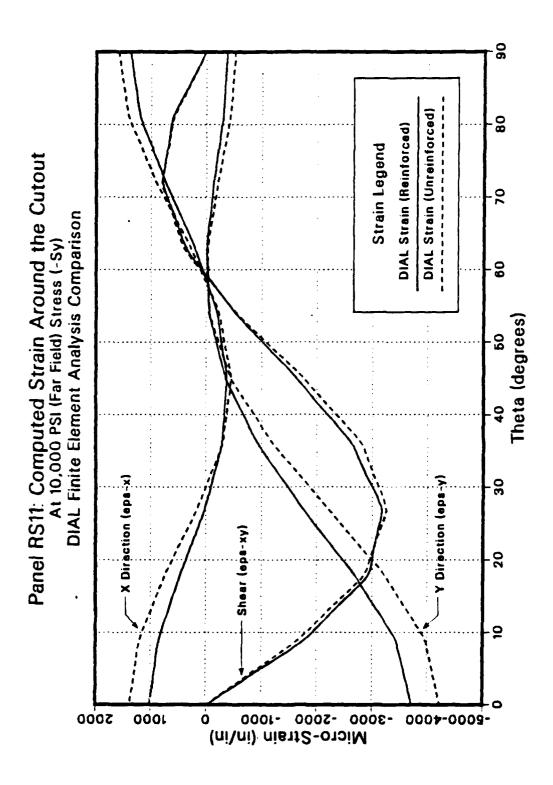


Figure G.2 Panel RSI1: Strain Comparison Around the Cutout.

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TABLE XXVIII

PANIEL RS11: LEPEA STRAIN DISTRIBUTION AROUND THE CUTOUT (-10,000 PSI).

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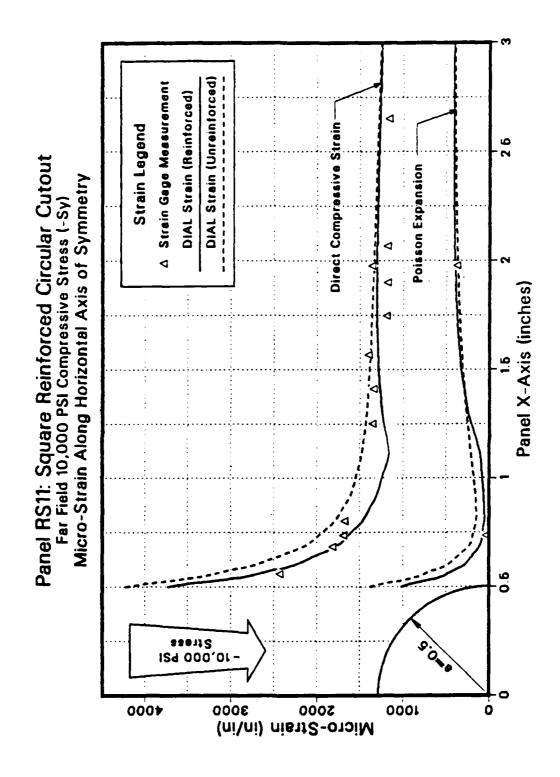


Figure G.3 Panel RS11: Strain Comparison Along the "Axis.

TABLE XXIX

PANEL RS11, LEPEA STRAIN DISTRIBUTION ALONG THE X AXIS (-10,000 PSI).

EPS-XY	
EP S-X	00000000000000000000000000000000000000
EPS-Y	00000000000000000000000000000000000000
Y COORD	
X COORE	00000000000000000000000000000000000000
NCDE	しては、これにしてもらしてもられるとしのもしでものできてこととことにことにことにことにことにことにことにことにことにことにことにことにこ

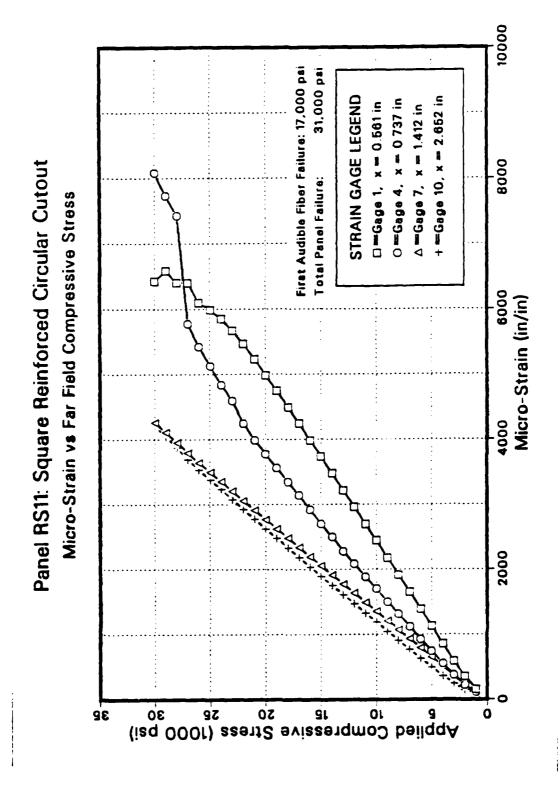


Figure G.4 Panel RS11: Microstrain vs. Compressive Stress.

TABLE XXX

PANEL RS11: SELECTED STRAIN GAGE VALUES DURING LOAD.

Load (psi)	Micr	c-Strain	Indicated	by Gage:
(521)	#1	# 4	#7	# 19
00000000000000000000000000000000000000	197733004972759822409068883739 13581369146924792478246848904454 1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-	811405880561 045964:0980 45413111 027542100988799134568493227338 123579135680246913579258147470 1111122222333334445555778	277800010 1131335713604 04413574 715059371 37 3350713604 0441357 	\$\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\

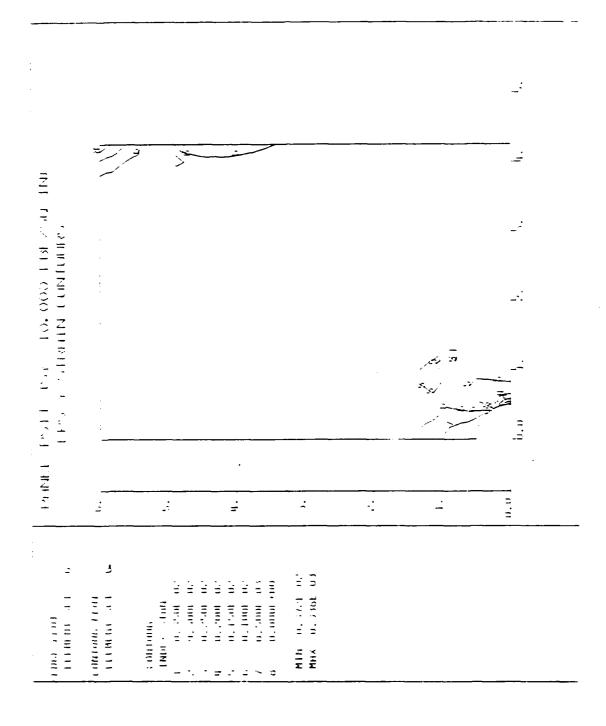


Figure G.5 Panel RS11: Eps-Y FEA Contours.

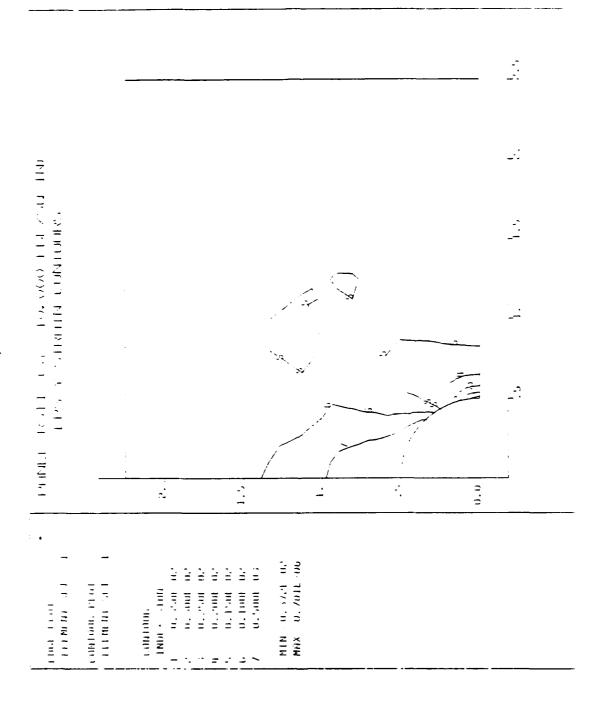
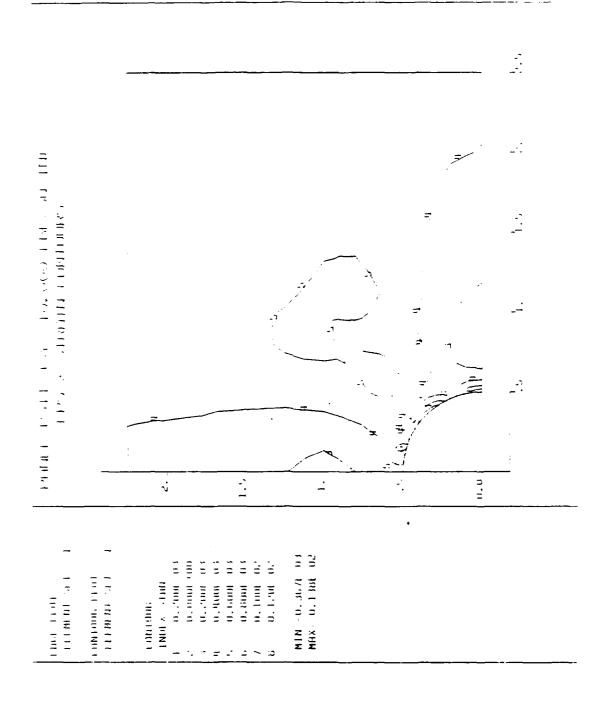


Figure G.6 Panel RS11: Eps-Y FEA Contours Near the Cutout.



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Figure G.7 Panel RS11: Eps-X FEA Contours Near the Cutout.

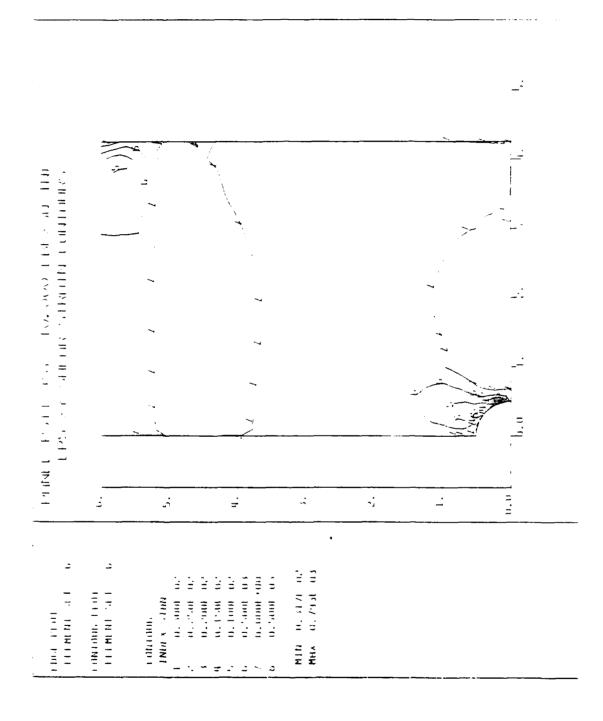


Figure G.8 Panel RS11: Eps-XY FEA Contours Near the Cutout.

APPENDIX H

PANEL RS31: ANALYTICAL AND EXPERIMENTAL DATA

Panel RS31 was reinforced with one square co-cured ply of G/Ep concentric with the cutout on the outside of each facesheet. The reinforcement had the following dimensions:

Stape:	Square
Inside Diameter:	1.00 in
Length & Width:	3.20 in
Thickness (each):	0.014 in (1 ply)
Area (each face):	9.455 in ²

 0.265 in^3

Net Cross Section: 0.062 in²

Chane.

Total Volume:

The panel failed at the hole edge (Type-1) at an applied normal stress of -32,550 psi, 89% of the ultimate load predicted. Based strictly on the failure of the unreinforced panel and the computed stress concentration factor of 2.51, failure was predicted at $\overline{\sigma}_n$ =:-36,400 psi.

. The finite element model (mesh) is shown in Figure H.1. The square area of reinforcement is denoted by the bold lines next to the cutcut.

Figure H.2 compares the three (finite element) computed strains around the cutout between the unreinforced panel (PO \emptyset \emptyset) and RS31. These computed strain values are listed in Table XXXI.

Figure H.3 compares the computed and experimental strains in the Y and X (poisson expansion) directions in the panel and shows

an almost perfect correlation between analytical and experimental strain at $\overline{\sigma}_n$ = -10,000 psi. There was virtually no strain variation between the left and right sides of the hole. The edge of the reinforcement is somewhat difficult to see in the Figure H.3 as a slight inflection point at about x = 1.6". Table XXXII gives the LEFEA computed strain values along the X axis.

Figure H.4 graphically shows the stress-strain state during the load sequence from $\overline{a}_n = 0$ to -32 ksi. The experimentally measured strain gage values are given in Table XXXIII. Up to about 20 ksi gage #1 next to the hole (x = +0.553") shows an almost linear stress-strain relation. At or just above -20 ksi, however, there appears what seems to be a sudden decrease in strain rate on the right side of the cutout which just as suddenly ends at -23 ksi where the previous stress-strain ratio resumes. I believe that this is, instead, a transfer of very localized stress (or the load path) away from the area next to the cutout to some other path in the field or possibly the opposite facesheet. It is important to note that gage #2 on the left side of the cutout at x = -0.597" shows no corresponding increase in strain that would be caused by the transfer of load. Gage #3 at x =+0.666" shows some correspondence with gage #1 degree of loss in local stiffness up to -20 ksi. If it were a malfunction of the strain gage or a partial debonding from the surface of the composite the strain rate would change.

Another anomaly occurs at $\overline{\sigma}_n$ above -27 ksi where the "stairstep" phenomenon occurs again. Gage #3 at x = 0.666" reflects what is occurring next to the cutout edge. This is not true of gages #6 and #11 at x = -1.48" and 2.54" respectively; they reflect only the expected stress-strain relation. At -30 ksi gage

#1 indicated a rapidly increasing rate of strain and subsequently failed.

Figures H.5 through H.8 show the strain contours at $\overline{\sigma}_n =$ -10,000 psi computed and plotted using DIAL. Figure H.5 is the full quarter panel with strain (Eps-Y) parallel to the applied load. Figures H.6 through H.8 (Eps-Y, Eps-X and Eps-XY) show the strains in detail close to the cutout.

PANEL RS31: SQUARE REINFORCEMENT PANEL MESH LAYOUT

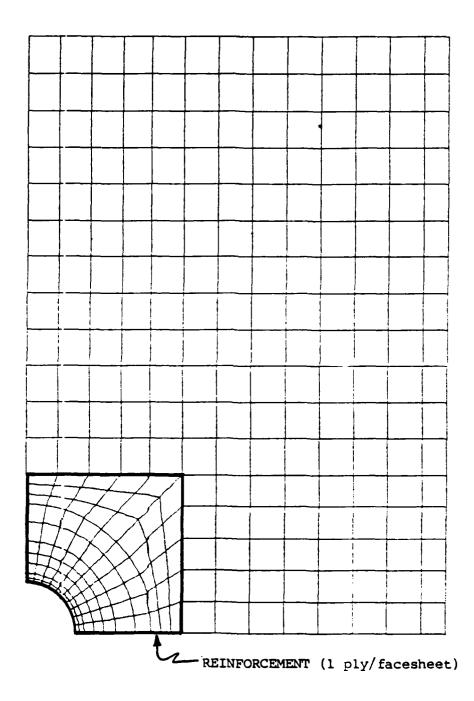


Figure H.1 Panel RS31: DIAL Finite Element Mesh.

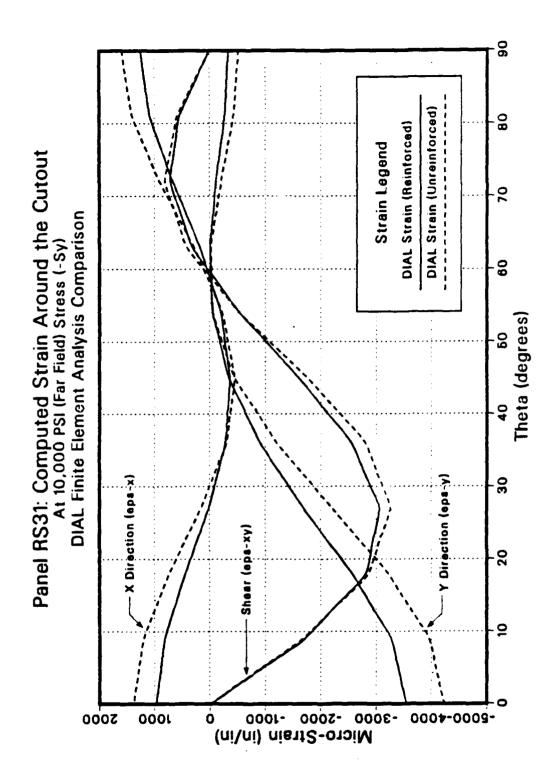


Figure H.2 Panel RS31: Strain Comparison Around the Cutout.

TABLE XXXI

CUTOUT (-10,000 PSI).	EPS-XY	0.000000000000000000000000000000000000
THE	EP S-X	00000000000000000000000000000000000000
PANEL RS31: LEPEA STRAIN DISTRIBUTION AROUND	X-Sda	22222222222222222222222222222222222222
STRAIN DISTRU	Y СООНЭ	00000000000000000000000000000000000000
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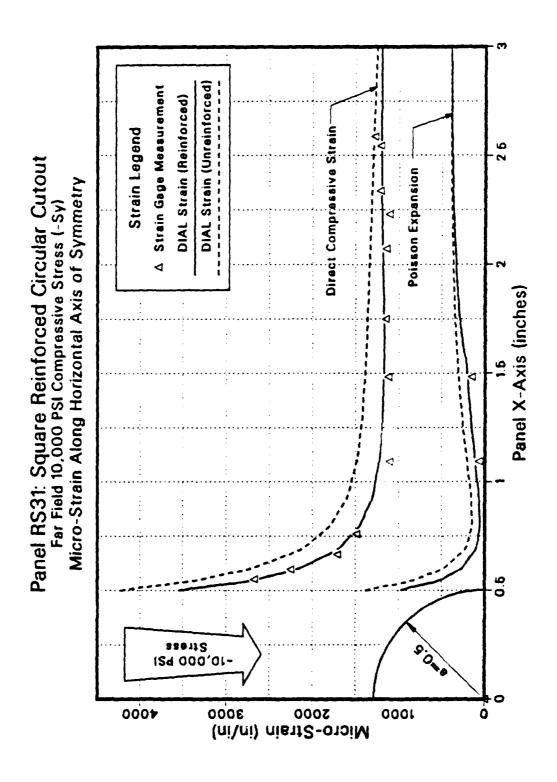


Figure H.3 Panel RS31: Strain Comparison Along the X Axis.

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TABLE XXXII

000 PSI).	EP S-XY	
X AXIS (-10,000	EP S-X	日本のでは、1000000000000000000000000000000000000
NUTION ALONG THE	EPS-Y	00000000000000000000000000000000000000
STRAIN DISTRIBUTION	Y COORD	
RS31: LEPEA	X COOKE	00000000000000000000000000000000000000
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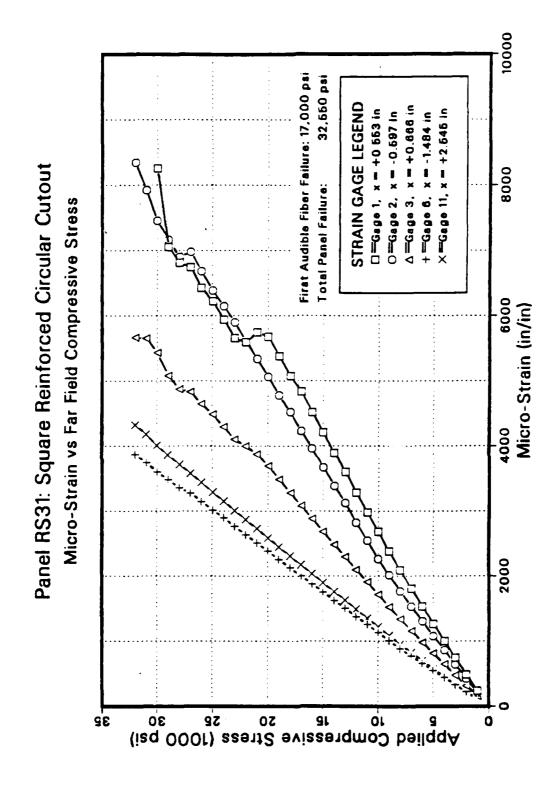


Figure H.4 Panel RS31: Microstrain vs. Compressive Stress.

TABLE XXXIII

PANEL RS31: SELECTED STRAIN GAGE VALUES DURING LOAD.

Load (psi)		Micro-Str	ain Indica	ted by Gage	:
•••	#1	#2	ڌ#	#6	#11
00000000000000000000000000000000000000	4523 44002191038074774080208752aaa 2470231988780902377774954238755517/ 111524223334445555555666678 	702071372343592002956694907344733 24680351642287632763094887065248 111270258136925703681369914935 1	338512216978054135264048712642729 5174180421090888888997009853783574 	7901770661355343821639554788632312 123445780357025703580369147580473 1234567801235678012346789 11111111122223222333333333333333333333	019079000000007070754100908800008861487707019079000000000000707716078078444770000000000000000000000000000

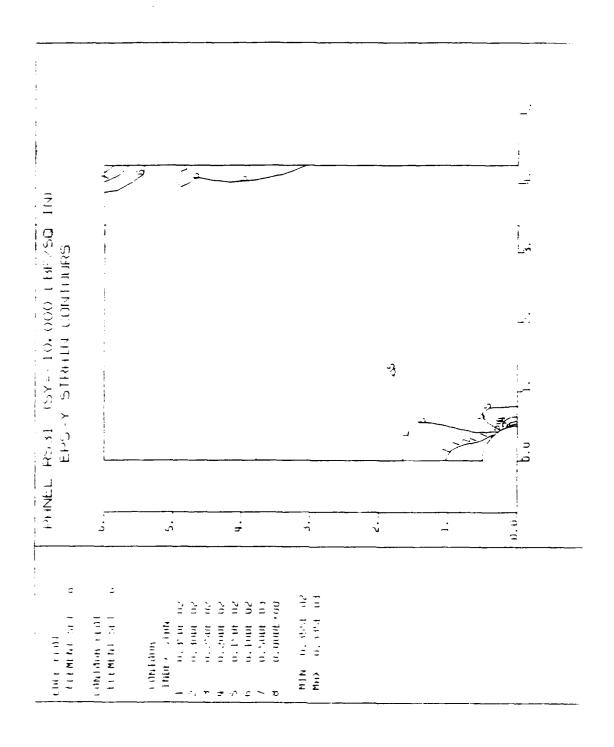


Figure H.5 Panel RS31: Eps-Y FEA Contours.

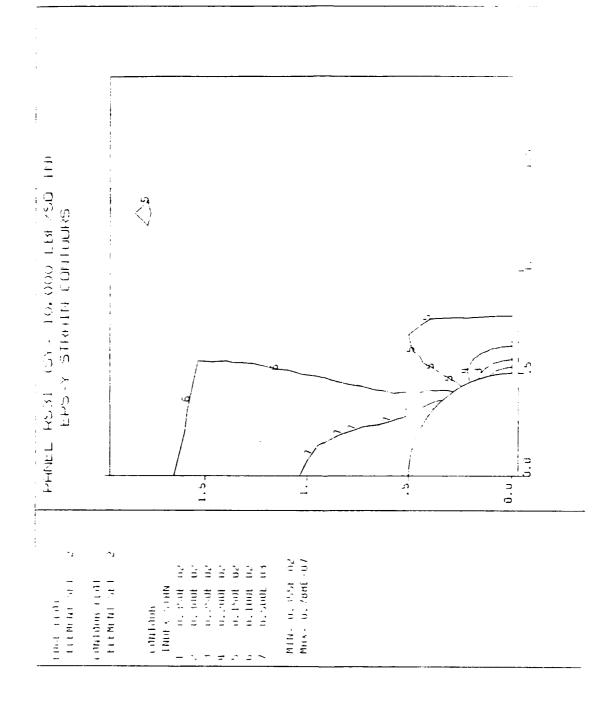
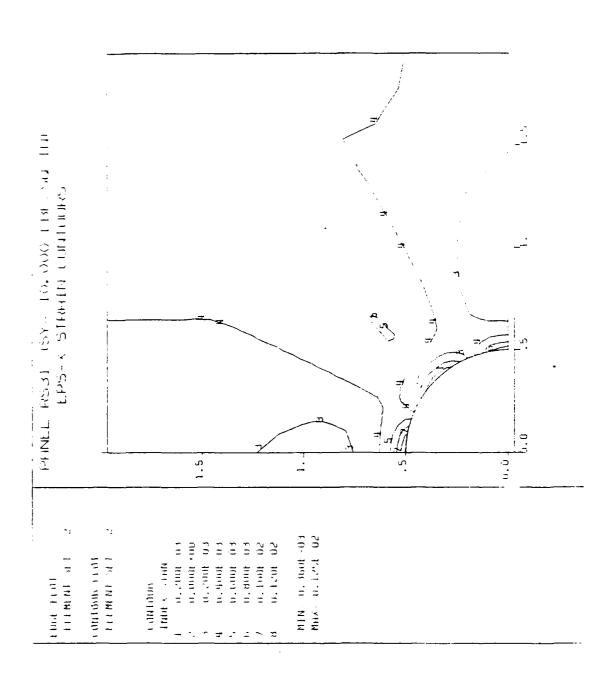


Figure H.6 Panel RS31: Eps-Y FEA Contours Near the Cutout.



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Figure H.7 Panel RS31: Eps-X FEA Contours Near the Cutout.

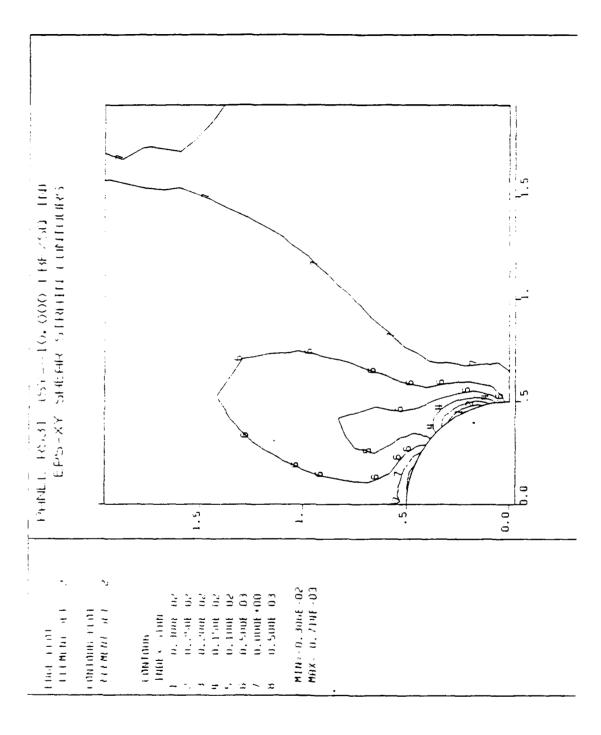


Figure H.8 Panel RS31: Eps-XY FEA Contours Near the Cutout.

APPENDIX I

PANEL RS51: ANALYTICAL AND EXPERIMENTAL DATA

Panel RS51 was reinforced with one square co-cured ply of G/Ep concentric with the cutout on the outside of each facesheet. The reinforcement had the following dimensions:

Shape: Square
Inside Diameter: 1.00 in
Length & Width: 4.10 in

Thickness (each): 0.014 in (1 ply)

Area (each face): 10.025 in^2 Total Volume: 0.449 in^3 Net Cross Section: 0.087 in^2

The panel failed at the hole edge (Type-1) at an applied normal stress of about -16,000 psi. Based strictly on the failure of the unreinforced panel and the computed stress concentration factor of 2.46, however, the failure should have been close $\overline{\sigma}_{\rm a} = -37,000$ psi.

The finite element model (mesh) is shown in Figure I.1. The square area of reinforcement is denoted by the neavy outline around the cutout.

Figure I.2 compares the three (finite element) computed strains around the cutout between the unreinforced panel (PO \emptyset) and RS51. These computed strain values are listed in Table XXXIV.

Figure I.3 compares the computed (solid and dashed lines) and experimental (triangles) strains in the Y and X (poisson

expansion) directions in the panel and shows excellent correlation between analytical and experimental strain at -10,000 psi applied normal stress. There was some minor strain variation between the left and right sides of the hole. The edge of the reinforcement is very difficult to see in the figure as a very slight inflection point at about x = 2.0". Table XXXV gives the analytical strain values along the X axis.

Figure I.4 graphically shows the stress-strain state during the load sequence from $\bar{\sigma}_n = 0$ to -21 ksi. Experimentally measured strain gage values are given in Table XXXVI. Up to about -16 ksi gage #1 next to the hole (x = +0.553") shows the expected almost linear stress-strain relation. However, just above $\overline{\sigma}_n$ = -16 ksi up to -19 ksi there begins a apparent loss in stiffness on the right side of the cutout which suddenly ends at -19 ksi where the strain next to the cutout drops to almost zero. Note that gage #3 on the right side of the cutout at x = 0.666" snows no corresponding increase in strain that would be caused by an increase in local stress near the cutout due to a shift in the load path. Gages #5 and #11 at x = 1.44" and -2.76" respectively reflect only the expected stress-strain relation. This can be explained by gages #1 and 3 showing the effect of a gage under compression when the facesheet under it suddenly buckles outward. The result was a near zero strain indication. It is difficult to see, but there is an appreciable increase in strain rate indicated in gages #5 and #11 at $\bar{\sigma}_n = -20$ ksi. This confirms that there is a sudden increase in load in an area relatively far from the cutout, just as would be expected when the material close to the cutout begins to fail and the load paths are displaced away from it increasing the stain in the far-field.

Figures I.5 through I.8 show the strain contours at $\overline{\sigma}_n =$ -10,000 psi computed and plotted using DIAL. Figure I.5 is the full quarter panel with strain (Eps-Y) parallel to the applied load. Figures I.6 through I.8 (Eps-Y, Eps-X and Eps-XY) show the strains in detail close to the cutout.

PANEL RS51 SQUARE REINFORCEMENT PANEL MESH LAYOUT

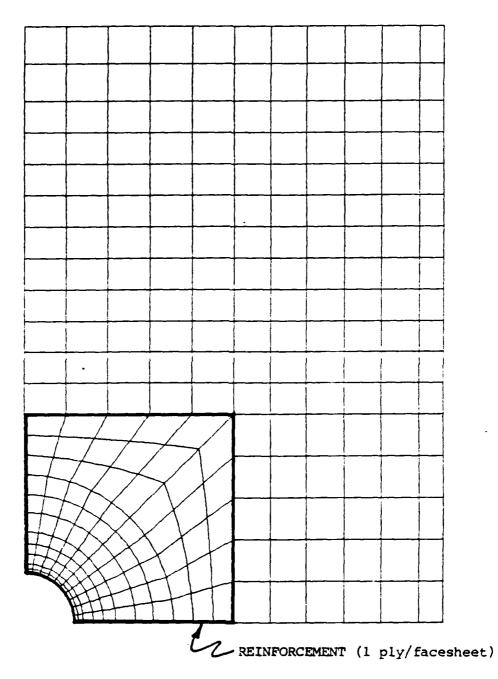


Figure I.1 Panel RS51: DIAL Finite Element Mesh.

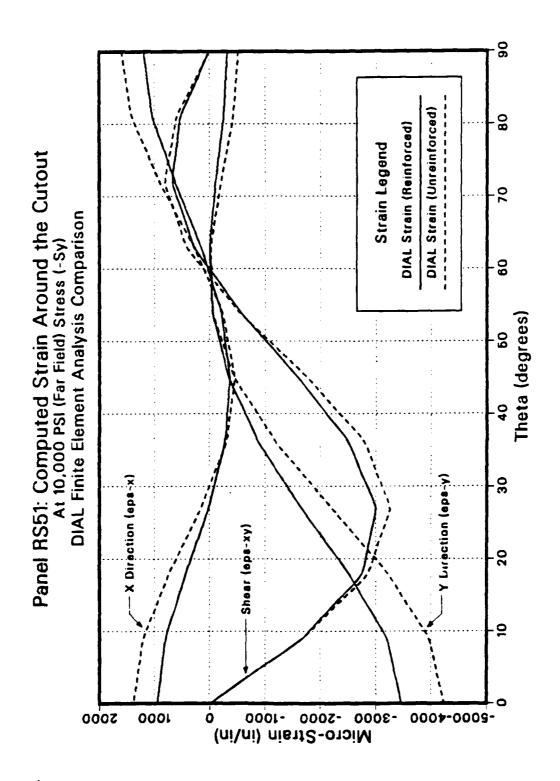


Figure I.2 Panel RS51: Strain Comparison Around the Cutout.

TABLE XXXIV

./153 000/0	EPS-XY	00000000000000000000000000000000000000
	EPS-X	00000000000000000000000000000000000000
STRAIN DISTRIBUTION AMOUND THE COLOGY (-10,000 EST).	EPS-Y	00000000000000000000000000000000000000
	Y COORD	00000000000000000000000000000000000000
PANEL RS51: LEPEA	X COORD	00000000000000000000000000000000000000
PAN	NODE	

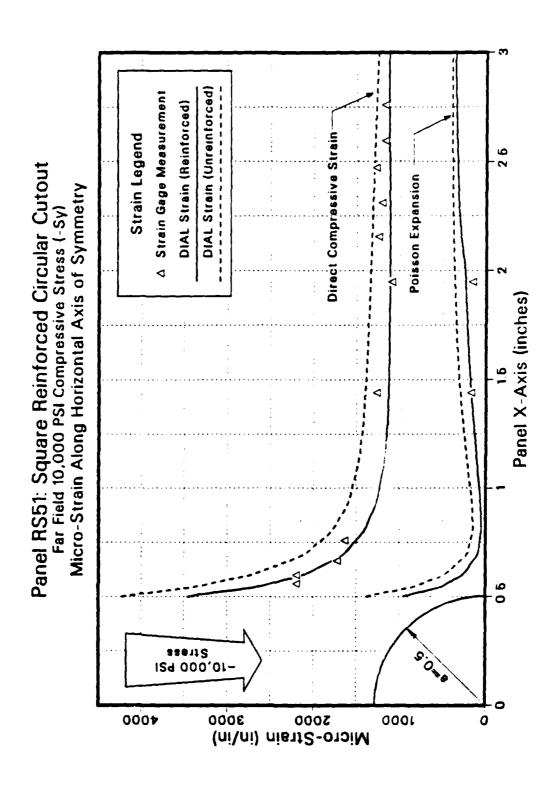
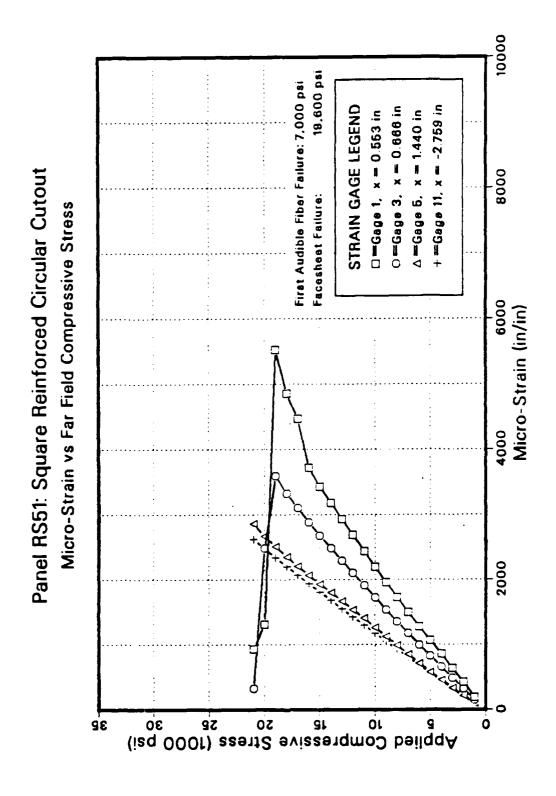


Figure I.3 Panel RS51: Strain Comparison Along the X Axis.

TABLE XXXV

(-10,000 PSI).	EPS-X)	11111
THE X AXIS (-10	EPS-X	は、
DISTRIBUTION ALONG TH	EPS-Y	
STRAIN DISTRI	у соокр	
IEL RS51: LEPEA	X COOND	00000000000000000000000000000000000000
PANE	NODE	5.4をアよりら替とうられ とてよりら替とうられをてよりら替とうられてしきようなのとられてよりのもないでしらなのれてよらもうられてしきとしましてになったとしましましましましましましましましましましま



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Figure 1.4 Panel RS51: Microstrain vs. Compressive Stress.

TABLE XXXVI

PANEL RR51: SELECTED STRAIN GAGE VALUES DURING LOAD.

Load (psi)	Micro	c-Strain I	ndicated b	; Gage:
(232)	#1	# 3	# 5	# .1
00000000000000000000000000000000000000	996317830477920506693 	586705019522125032503 418529753210987802982 	913555373 -2345714822 047 0 36040 066 -11245697 3 36040 066 -112111190223569 -11211111122222222	8013579810597107703819 -234567925792580370371 -111245803703371

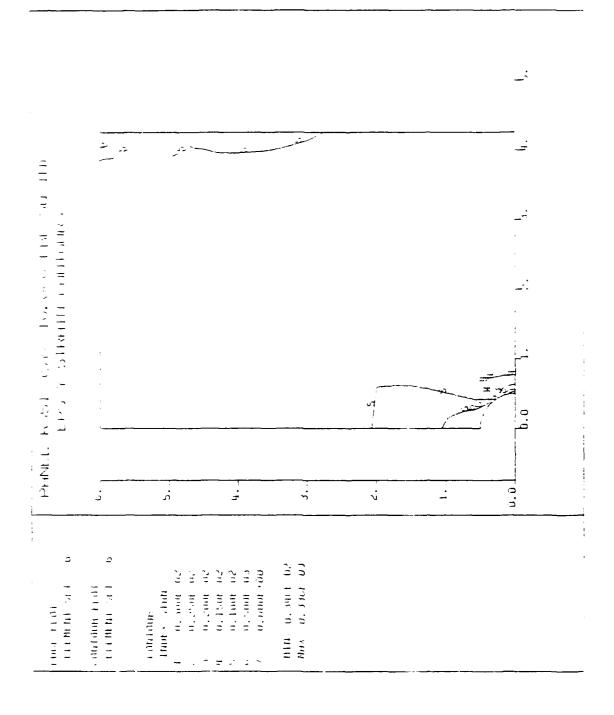


Figure I.5 Panel RS51: Eps-Y FEA Contours.

マング しき ソング・スク 重要的 ひょうひん 発量 アンプラング アンプランド マランド しろいのから 動物 しない いっかん としろう カスギ

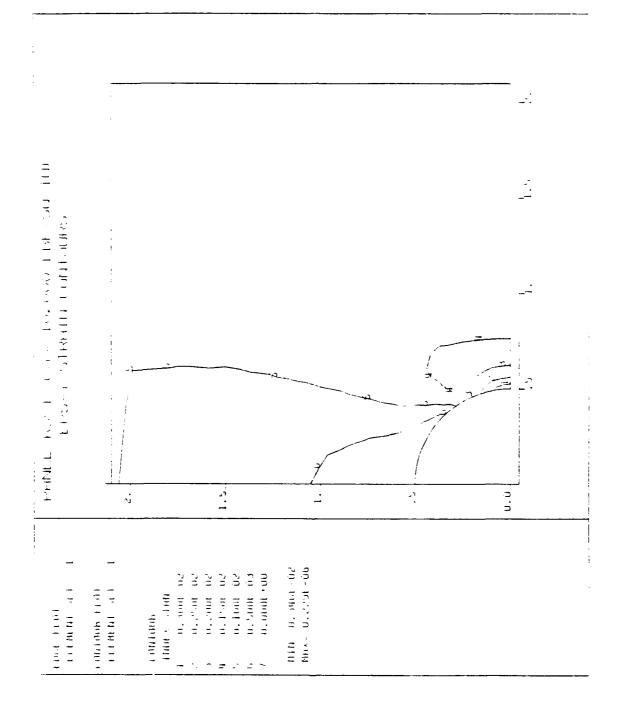


Figure I.6 Panel RS51: Eps-Y FEA Contours Near the Cutout.

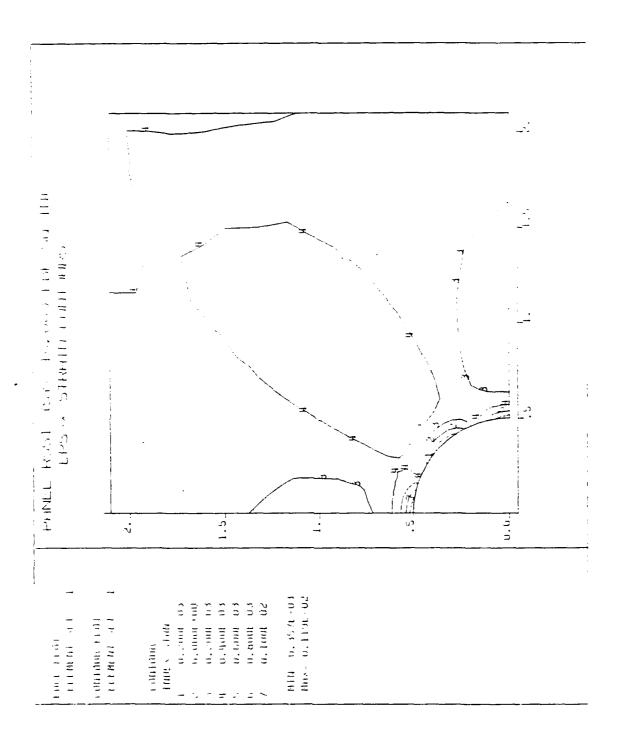


Figure I.7 Panel RS51: Eps-X FEA Contours Near the Cutout.

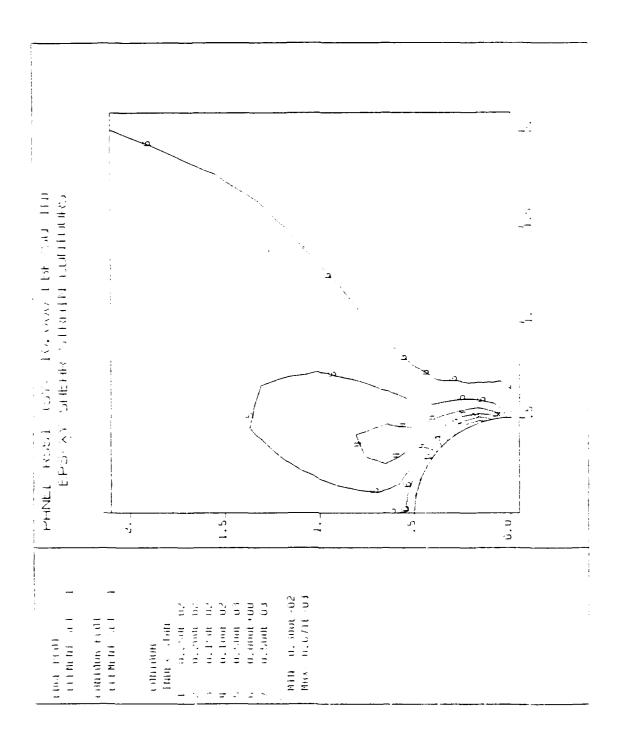


Figure I.8 Panel RS51: Eps-XY FEA Contours Near the Cutout.

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APPENDIX J

PANEL RH11: ANALYTICAL AND EXPERIMENTAL DATA

Panel RH11 was reinforced with one co-cured ply of G/Ep in the shape of two strips on either side of the cutout on the outside of each facesheet offset 0.50 inch from the edge of the cutout. The reinforcement had the following dimensions:

Strip

-	-			
Length:	1.57	in		
Width:	1.00	in		
Thickness (each):	0.014	in	(1	(Ylq
Area (each face):	3.14	in^2		
Total Volume:	0.088	in^3		

Net Cross Section: 0.056 in²

Shape:

The panel failed at the hole edge (Type-1) at an applied normal stress ($\overline{\sigma}_n$) of -29,960 psi. Based strictly on the failure of the unreinforced panel and the computed stress concentration factor of 3.02 (which was very slightly higher than the unreinforced panel), failure was predicted at $\overline{\sigma}_n$ = -30,200 psi. The panel failed within 0.6% of the predicted ultimate load.

The finite element model (mesh) is shown in Figure J.1. Inearea of the strip reinforcement is outlined by the heavy lines offset 0.50 inch to the right of the cutout edge.

Figure J.2 compares the three (finite element) computed strains around the cutout between the unreinforced panel ($PO\emptyset\emptyset$) and RH11. These computed strain values are listed in Table

XXXVII. There is no significant decrease in the strain due to the reinforcement. A very slight increase may be seen in Eps-Y near the O degree position (on the X axis). This increase in strain is due to the shifting of load paths to either side of the reinforcement. The slight load path shift toward the cutout acted to slightly increase the SCF.

Figure J.3 compares the computed and experimental strains in the X and Y (poisson) directions in the panel and shows almost perfect correlation between analytical and experimental strain at $\overline{\sigma}_n = -10,000$ psi. There was virtually no measured strain variation between the left and right side of the hole. The edge of the reinforcement can not be seen in the figure; the effects of reinforcement is a decrease around the reinforcement and a subtle increase near the hole and in the far field (where x = 2.50") compared to the unreinforced panel (POØØ). Taple XXXVIII gives the computed values of the strains along the X axis.

Figure J.4 shows the stress-strain state during the load sequence from 0 to -29 ksi. Experimentally measured strain values are given in Table XXXIX. Up to -23 ksi all gages indicated a normal stress-strain state. From -23 ksi there was a dramatic change; first gages #1 and #2 showed a load transfer from the area next to the right edge of the cutout to the left side. Then suddenly the roles were reversed and gage #2 (x = -0.583") indicated a load transfer to the right side of the cutout. Gage #1 (x = +0.568") shows a tremendous strain increase, off the scale on Figure J.4, as high as 12,800 microstrain (Table XXXIX). The effect of the load transfer is apparent on gage #6 (x = +0.681); it reflects the increased load away from the cutout edge on the right side of the hole. It appears that the fibers on the right

side of the cutout began to buckle on the micro-mechanical level very near the edge.

Figures J.5 through J.8 show the strain contours at $\overline{\mathbf{0}}_n = -10,000$ psi computed and plotted using DIAL. Figure J.5 is the full quarter panel with strain (Eps-Y) parallel to the applied load. Figures J.6 through J.8 (Eps-Y, Eps-X and Eps-XY) show the strains in detail close to the cutout.

PANEL RH11 STRIP REINFORCEMENT PANEL MESH LAYOUT

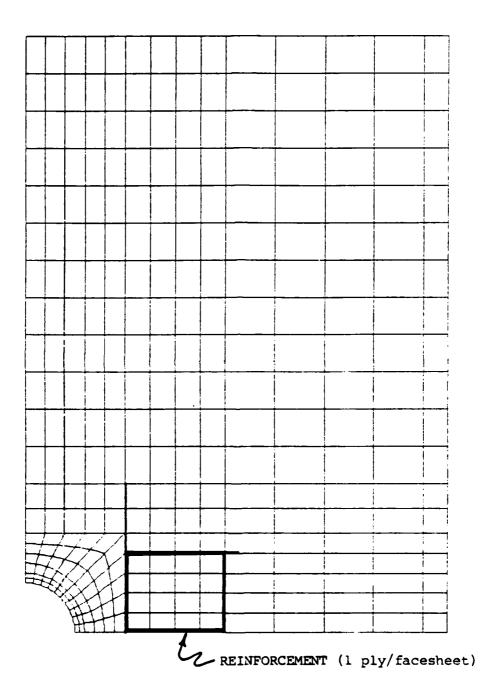
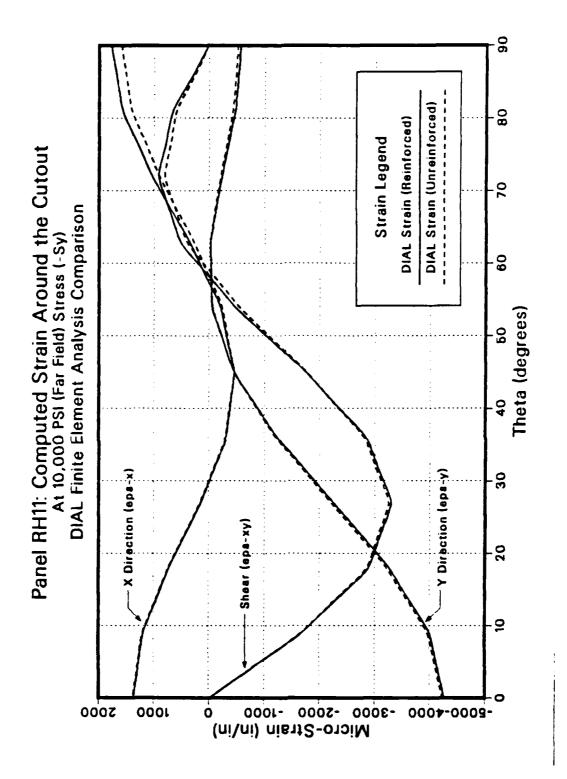


Figure J.1 Panel RH11: DIAL Finite Element Mesh.



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Figure J.2 Panel RHIL: Strain Comparison Around the Cutout.

TABLE XXXVII

PANEL RHII: LEFEA STRAIN DISTRIBUTION AROUND THE CUTOUT (-10,000 PSI).

NODE

EPS-XY	00000000000000000000000000000000000000
EPS-X	00000000000000000000000000000000000000
EPS-Y	20000000000000000000000000000000000000
Y COOKD	000000000000000000000000000000000000
X COORD	00000000000000000000000000000000000000

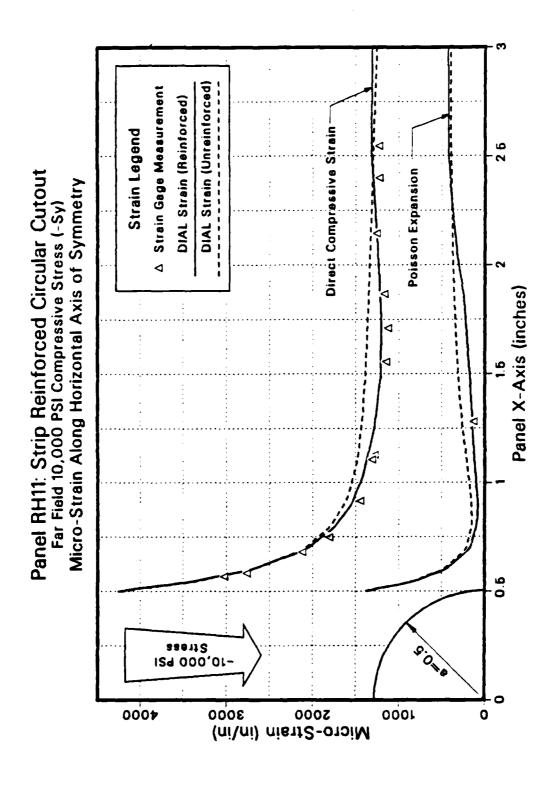


Figure J.3 Panel RH11: Strain Comparison Along the X Axis.

TITANTE XXXVIII

(-10,000 PSI).	EPS-XY	1111111 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
THE X AXIS (-10	X-S-I	00000000000000000000000000000000000000
DISTRIBUTION ALONG	EPS-Y	11 111 111 111 111 111 111 111 111 111
STRAIN	у соойр	
PANEL RHII, LEPEA	X COORD	00000000000000000000000000000000000000
PA	NODE	1068193mを1068193mを1068193mをとってってってってってってってってってってってってってってってってってってって

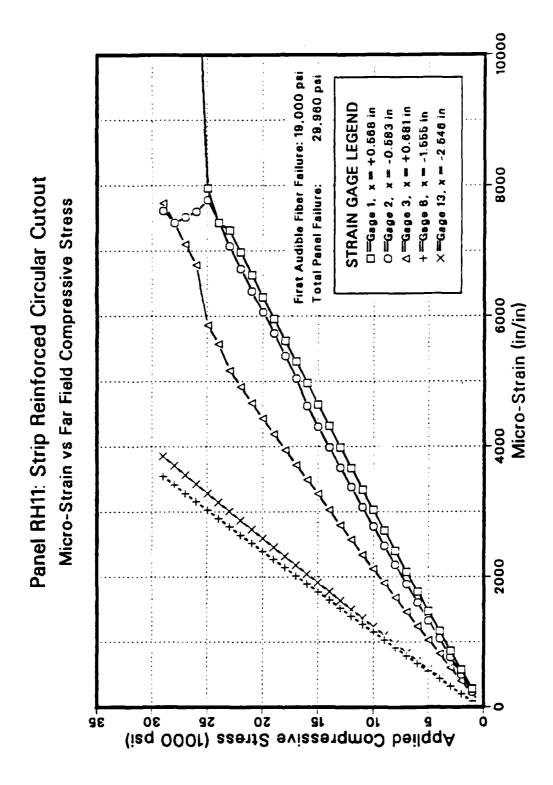


Figure J.4 Panel RHIL: Microstrain vs. Compressive Stress.

TABLE XXXIX

PANEL RH11: SELECTED STRAIN GAGE VALUES DURING LOAD.

Load (psi)	Mi	crc-Strain	Indicated	by Gage:	#12
00000000000000000000000000000000000000	* 766666779124781470259271764937 	# 296887695596678323910656381605 	#2801491211225590822006323632 14680246913570247914691587147 1	78421960100682725294730978513 * 89135681357914691469147925814 	84009961154940849830196805784 1 113457897036937047159360480605 1 113457891036937047159360480605 1 1111111111120000000000000000000000000

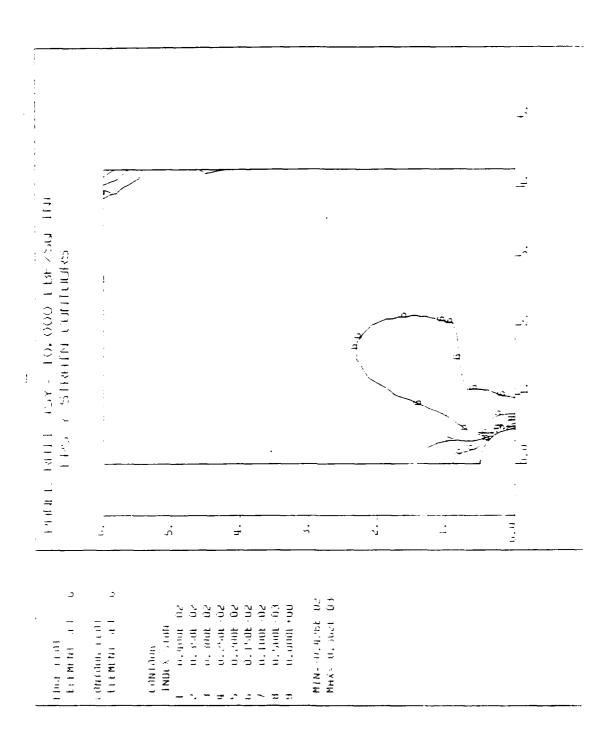


Figure J.5 Panel RHll: Eps-Y FEA Contours.

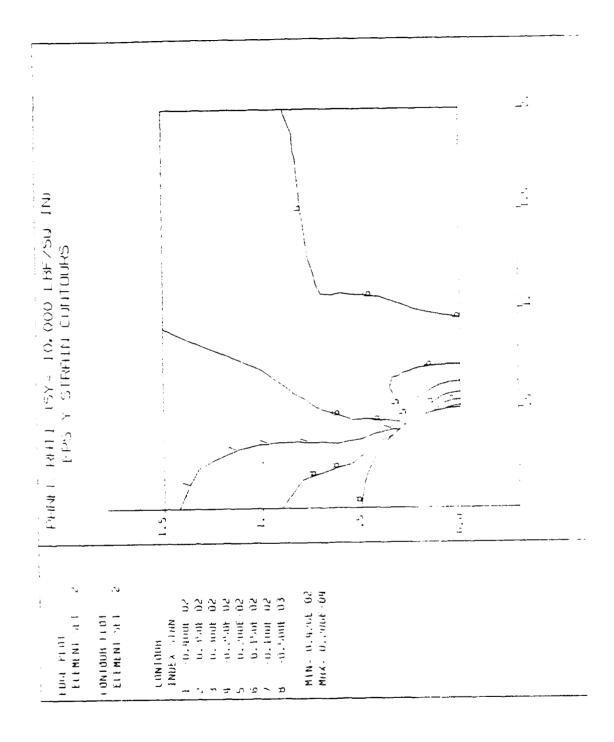


Figure J.6 Panel RH11: Eps-Y FEA Contours Near the Cutout.

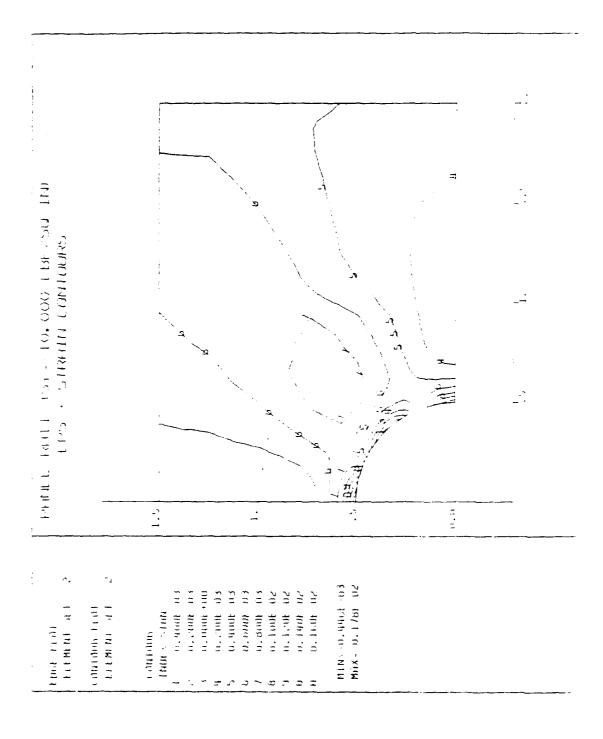


Figure J.7 Panel RH11: Eps-X FEA Contours Near the Cutout.

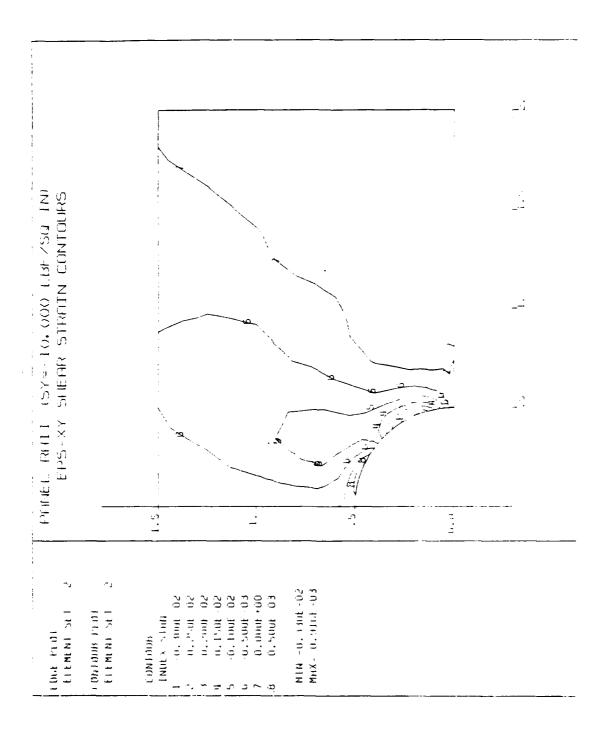


Figure J.8 Panel RHll: Eps-XY FEA Contours Near the Cutout.

APPENDIX K

PANEL RH22: ANALYTICAL AND EXPERIMENTAL DATA

Panel RH22 was reinforced with two co-cured plies of G/Ep in the shape of two strips on either side of the cutout on the outside of each facesheet offset 0.50 inch from the edge of the cutout. The reinforcement had the following dimensions:

Snape:	Strip		
Length:	1.57	in	
Width:	1.00	in	
Thickness (each):	0.028	in	(2 ply)
Area (each face):	3.14	in^2	
Total Volume:	0.176	in^3	
Net Cross Section:	0.112	in^2	

The panel failed at the hole edge (Type-1) at an applied normal stress of -31,460 psi. Based strictly on the failure of the unreinforced panel and the computed stress concentration factor of 2.91, the predicted failure was $\mathbf{\bar{G}}_n$ = -31,500 psi. The actual failure was within 0.4% of the predicted ultimate load.

The finite element model (mesh) is shown in Figure K.1. The area of the strip reinforcement is outlined by the heavy lines offset 0.50" to the right of the cutout's edge.

Figure K.2 compares the three (finite element) computed strains around the cutout between the unreinforced panel (PO \emptyset) and RH22. These computed strain values are listed in Table XXXX.

There is only a small decrease in the strain due to the reinforcement.

Figure K.3 compares the computed (solid and dashed lines) and experimentally measured (triangles) strains in the X and Y (poisson) directions in the panel and shows an excellent correlation between analytical and experimental strain at -10,000 psi applied stress. There was some very slight measured strain variation between the left and right side of the hole. The exact edge of the reinforcement can not be seen in the figure. The effects is a significant strain decrease (compared to the unreinforced panel, POOO) under the reinforcement, a small decrease near the hole and a slight increase in the far field (where x = 2.50"). Table XLI gives the computed values of the strains along the X axis.

Figure K.4 shows the stress-strain state during the load sequence from $\overline{\mathbf{G}}_n = 0$ to -30 ksi. Experimentally measured strain gage data are given in Table XLII. Up to about -9 ksi all gages indicated a normal stress-strain state. At -9 ksi gage #1 (x = ± 0.570 ") began showing decreasing reaction to the applied load. At -18 ksi, which coincided with the first audible ply failure (FAPF), the strain at gage #1 showed virtually no change up to -22 ksi. At -23 ksi, however, the strain suddenly doubles from 3100 to $6500\mu\epsilon$ and resumes its normal stress-strain ratio. At -9 ksi it appears that the load path is being diverted away from the right side of the cutout to the left. Gage #2 (x = ± 0.614 ") demonstrates an increased strain rate from -9 to -25 ksi when it increases significantly. Gage #1 failed above -27 ksi at about $\pm 10.000\mu\epsilon$ while Gage #2 continued to give reliable output up to almost $\pm 12.000\mu\epsilon$. It can be assumed from the response of gages in

the far-field that the stress-strain response of the panel as a whole remained constant with a slight decrease in stiffness with increased loads. The response of the facesheets close to the cutout show a very different response. It appears that there is a significant transfer of load from one side of the cutout to the other and to the opposing facesheet.

Figures K.5 through K.8 show the strain contours at $\overline{\mathbf{O}}_{n}$ = -10,000 psi computed and plotted using DIAL. Figure K.5 is the full quarter panel with strain (Eps-Y) parallel to the applied load. Figures K.6 through K.8 (Eps-Y, Eps-X and Eps-XY) show the strains in detail close to the cutout.

PANEL RH22 STRIP REINFORCEMENT PANEL MESH LAYOUT

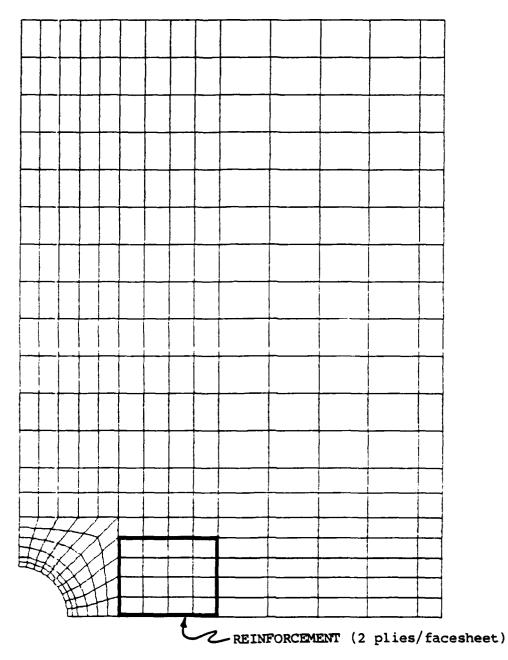


Figure K.1 Panel RH22: DIAL Finite Element Mesh.

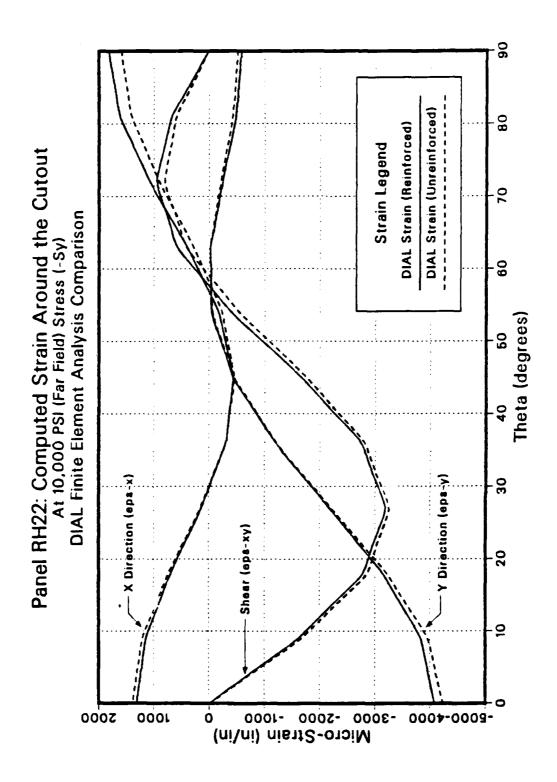


Figure K.2 Panel RH22: Strain Comparison Around the Cutout.

0,000 PSI).	EP S-XY	00000000000000000000000000000000000000
THE CUTOUT (-10,000	FPS-X	00000000000000000000000000000000000000
DISTRIBUTION AROUND	EPS-Y	100.2225
STRAIN DISTRI	Y COORD	0117:0000000000000000000000000000000000
el rh22: lepea	X COORE	00000000000000000000000000000000000000
PANEL	NCDE	トニュルシャン・サロースをはいまして、サロースのは、サロースをはなって、またって、サロースをはいました。よりでは、サロースをはいました。またられば、またっちょうない。またられば、いいいないのは、またっちょうない。またいまれば、またいいましょう。またいいましょうには、またいいいましょう。またいいましょうには、またいいいいいいいいいいいいいいいいいいいいいいいいいいいいいいいいいいいい

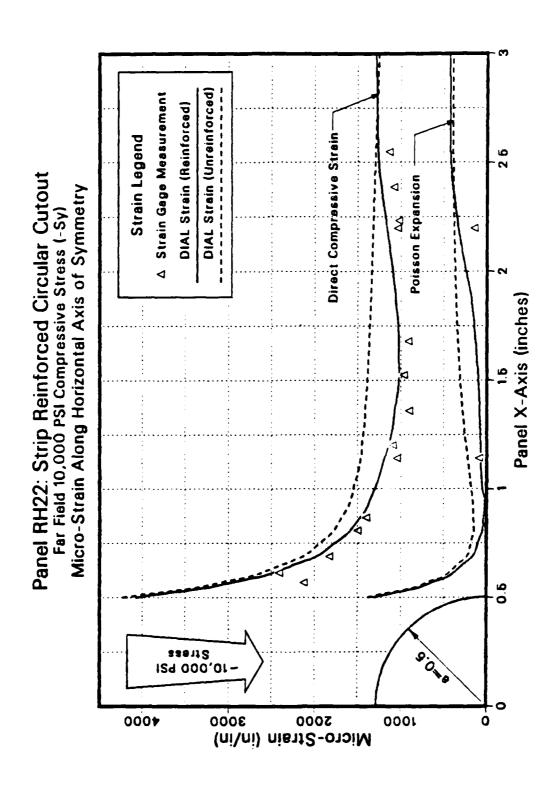


Figure K.3 Panel RH22: Strain Comparison Along the X Axis.

TABLE XLI

PANEL RH22, LEFEA STRAIN DISTRIBUTION ALONG THE X AXIS (-10,000 PSI).

EPS-XY		0.43988-0 0.83598-0 0.118598-0 0.17828-0 0.1918-0		. 76 43 E - 0 . 77 97 E - 0 . 17 96 E - 0 . 31 92 E - 0	. 881/E-0 . 2020E-0 . 1204E-0 . 5578E-0 . 7559E-0
EPS-X	00000000000000000000000000000000000000	220388 230888 270888 467888	7450 8460 12060 1450 1450 1450 1111 1111 1111 1111 111	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	140 140 140 140 140 140 140 140 140 140
EPS-Y	00000000000000000000000000000000000000	2000 2000 2000 2000 2000 2000 2000 200	00000000000000000000000000000000000000	2010 2010 2010 2010 2010 2010 2010 2010	1250E-0 1237E-0 1234E-0 1234E-0 1E-0
Y COORD					###### ###### 100000 100000 100000 100000 100000
X COORE	00000000000000000000000000000000000000	20000000000000000000000000000000000000	20000000000000000000000000000000000000	ンマスカので ひでもなるので ひでものので からのののので 本点面質問題	24444444444444444444444444444444444444
NODE	70000000 -2500000000000000000000000000000	3000cm	7000000 	30:0101010101010101010101010101010101010	MCMCMC -

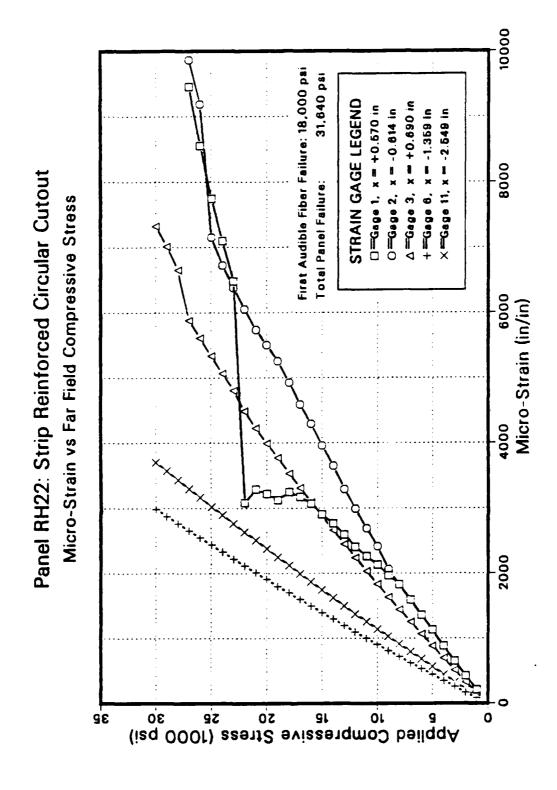


Figure K.4 Panel RH22: Microstrain vs. Compressive Stress.

	Panei	RH22: SE	tabli Lected Strai	XLII IN GAGE VALU	UES DURING I		
L	oad	M:	icrc-Strain	ı Indicatei	by Gage:		
(psi)	# 1	#2	#3	#ó	‡1	
2 3 4 5 6 7 8 9 10 11 11 13	00000000000000000000000000000000000000	8956812589998652737747438535aaa 246813589124557300074228889455// 246813589124557331212020889455// 	87255689013344 8360 b 933679 + 435258 246813580 4 692 63253679 52536 414	367447216364925313215287626347 1356802466024 98035792906318512 1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1	03481447068869990238363648695869 -123456789990123466789 -1	######################################	
				254		- 174326 - 1747926 - 17479	

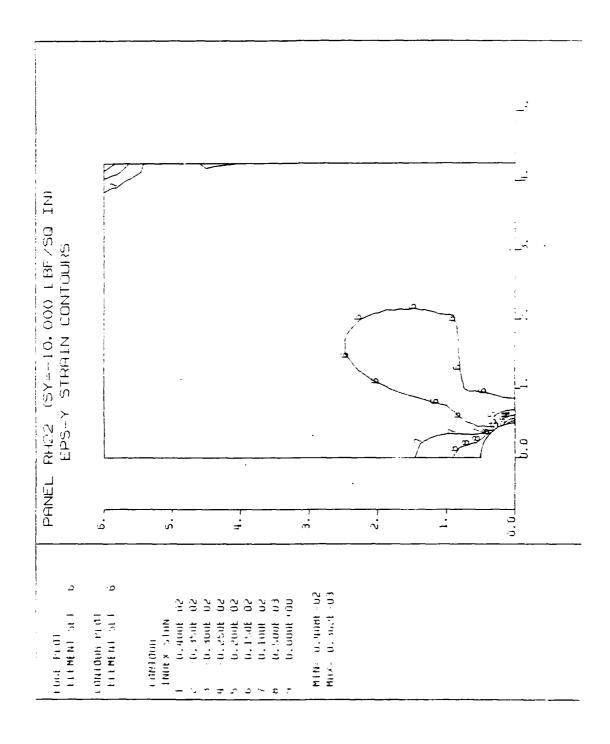


Figure K.5 Panel RH22: Eps-Y FEA Contours.

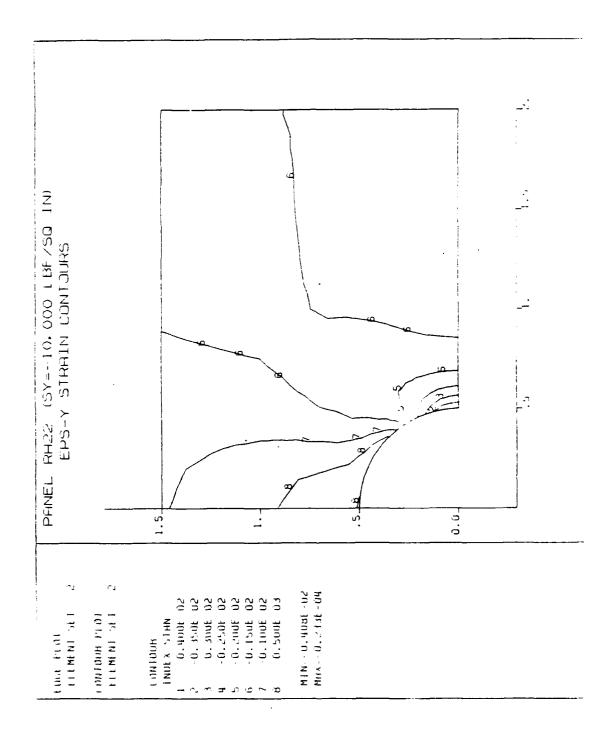
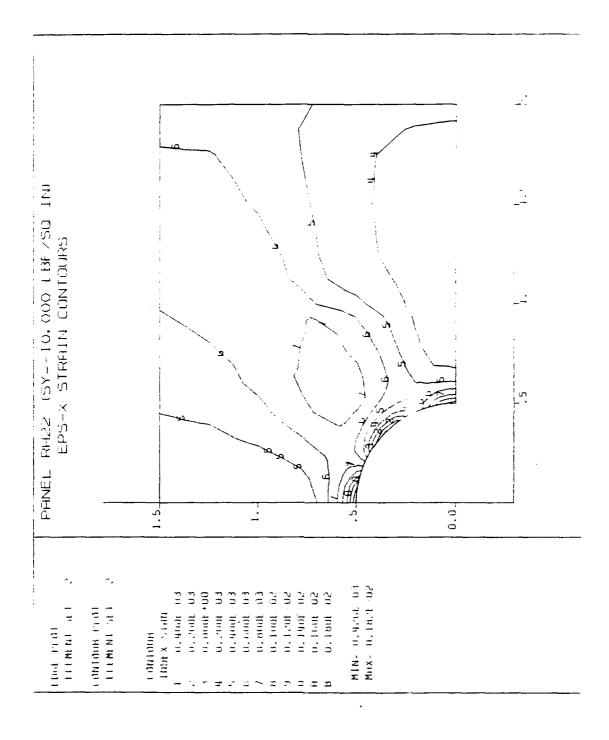


Figure K.6 Panel RH22: Eps-Y FEA Contours Near the Cutout.



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Figure K.7 Panel RH22: Eps-X FEA Contours Near the Cutout.

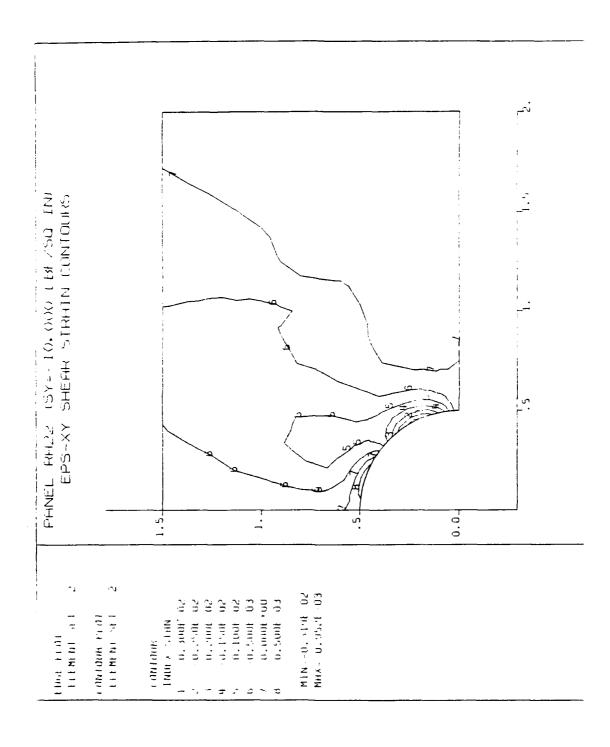


Figure K.8 Panel RH22: Eps-XY FEA Contours Near the Cutout.

APPENDIX L

PANEL RH31: ANALYTICAL AND EXPERIMENTAL DATA

Panel RH31 was reinforced with one co-cured ply of G/Ep in the shape of two strips on either side of the cutout on the outside of each facesheet offset 0.50 inch from the edge of the cutout. The reinforcement had the following dimensions:

Shape.	SCLIP
Length:	4.70 in
Width:	1.00 in
Tnickness (each):	0.014 in (1 ply)
Area (each face):	$9.40 ext{ in}^2$
Total Volume:	0.263 in ³

Net Cross Section: 0.056 in²

The panel failed by facesheet separation and buckling (Type-2) at an applied normal stress of -21,500 psi ($\overline{\mathbf{G}}_n$). Based strictly on the failure of the unreinforced panel and the computed stress concentration factor of 2.82, the predicted failure was at $\overline{\mathbf{G}}_n$ = -32,400 psi. The panel failed at 33.6% less than the predicted ultimate load.

The finite element model (mesh) is shown in Figure L.1. The area of the strip reinforcement is outlined by the heavy lines 0.50 inch to the right of the cutout's edge.

Figure L.2 compares the three (finite element) computed strains around the cutout between the unreinforced panel (PO $\emptyset\emptyset$) and RH31. These computed strain values are listed in Taple XLIII.

There was only a small decrease in the computed strain near the cutout due to the reinforcement.

Figure L.3 compares the computed (solid and dashed lines) and experimental (triangles) strains in the X and Y (poisson) directions in the panel and shows almost perfect correlation between analytical and experimentally measured strain at -10,000 psi applied normal stress. There was virtually no strain variation between the left and right side of the hole. The edge of the reinforcement can not be seen in the figure. The effect of reinforcement is a relatively small decrease in strain from the edge of the cutout out to about x = 3.0". Table XLIV gives the computed values of the strains along the X axis.

Figure L.4 shows graphically the stress-strain state during the load sequence from $\overline{\mathbf{O}}_n$ = 0 to -21 ksi. Strain gage values are given in Table XLV. Up to $\overline{\mathbf{O}}_n$ = -12 ksi all gages indicated a fairly normal stress-strain relation. At that point up to -18 ksi gage #2 demonstrated virtually no strain increase. At -18 ksi gage #1 (x = +0.572") suddenly indicated a strain decrease from 3900 to 6200 μ C and then an 1100 μ C increase at -19 ksi. From there it remained steady at about 7250 μ C to failure at $\overline{\mathbf{O}}_n$ = -21,500 ksi. Above -18 ksi gage #2 showed a steady decrease in strain which most probably indicated a separation of the facesheet from the core directly under the gage. As the load increased the facesheet buckled more and the indicated strain decreased. This panel shows how useful it would have been to instrument both facesheets of the panel to measure load transfer between them.

Figures L.5 through L.8 show the strain contours $\vec{\sigma}_n = -10,000$ psi computed and plotted using DIAL. Figure L.5 is the full quarter panel with strain (Eps-Y) parallel to the applied load.

Figures L.6 through L.8 (Eps-Y, Eps-X and Eps-XY) show the strains in detail close to the cutout.

PANEL RH31 STRIP REINFORCEMENT PANEL MESH LAYOUT

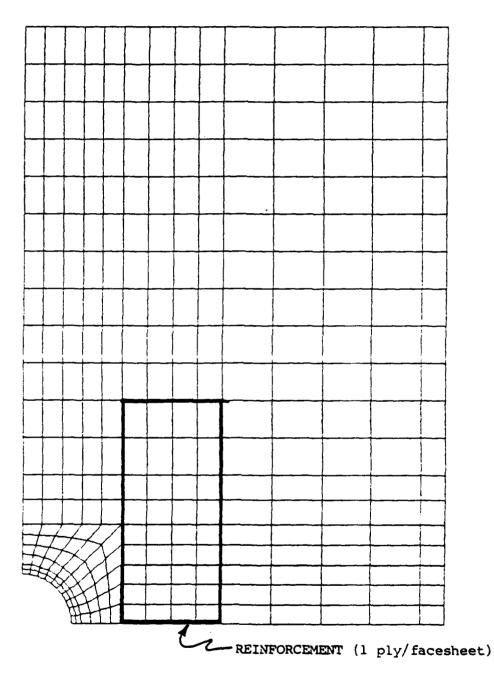


Figure L.1 Panel RH31: DIAL Finite Element Mesh.

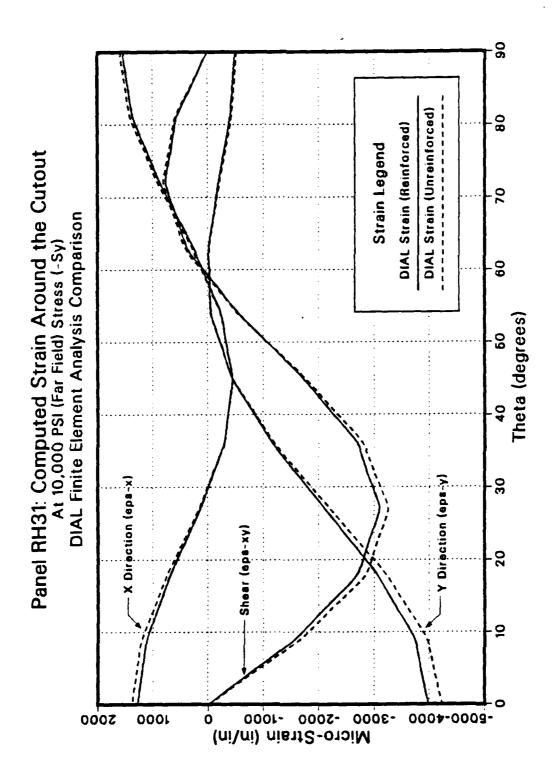


Figure L.2 Panel RH31: Strain Comparison Around the Cutout.

TABLE XLIII

PANEL RH31: LEFEA STRAIN DISTRIBUTION AROUND THE CUTOUT (-10,000 PSI).

EPS-XX	日本の 1 日本 1
EP S-X	00000000000000000000000000000000000000
EPS-	22222222222222222222222222222222222222
Y COOLD	00000000000000000000000000000000000000
X COORE	00000000000000000000000000000000000000
NCDE	1000とのられまで1008193mm~

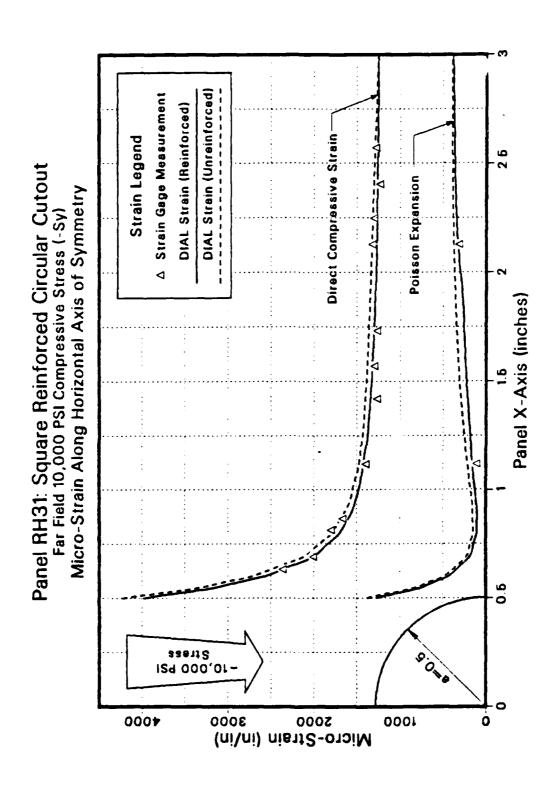


Figure L.3 Panel RH31: Strain Comparison Along the X Axis.

TABLE XLIV

PANEL RH31: LEPEA STRAIN DISTRIBUTION ALONG THE X AXIS (-10,000 PSI).

EP S-XY	
EP S-X	00000000000000000000000000000000000000
EPS-Y	00000000000000000000000000000000000000
у соокр	
х соовр	00000000000000000000000000000000000000
NODE	

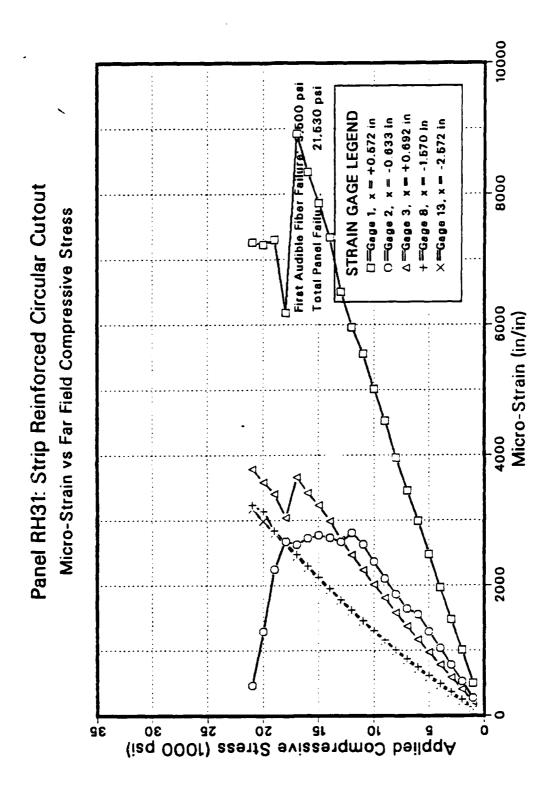


Figure L.4 Panel RH31: Microstrain vs. Compressive Stress.

TABLE XLV

PANEL RH31: SELECTED STRAIN GAGE VALUES DURING LOAD.

Load	M:	icro-Strain	Indicated	by Gage:	
(psi)	# 1	#2	#3	#8	#13
10000000000000000000000000000000000000	907678296512165756679 907678552156036327625 11122949552156036327025 1122334505555788913225 11223345055555788913225 112233450555555788913225	-267 -2627 -10295440 -11256460 -11816297 -11816297 -12368631 -1236863772288 -122277766229 -122221 -122221 -122221 -122221	779708176238592948098 	155273292278222735414 123469147060518529755414 1234678010518529755414 11134679122468123 1111111222222333	679395873511517895661 113681484840639631987 123457891246790246791 11111112223

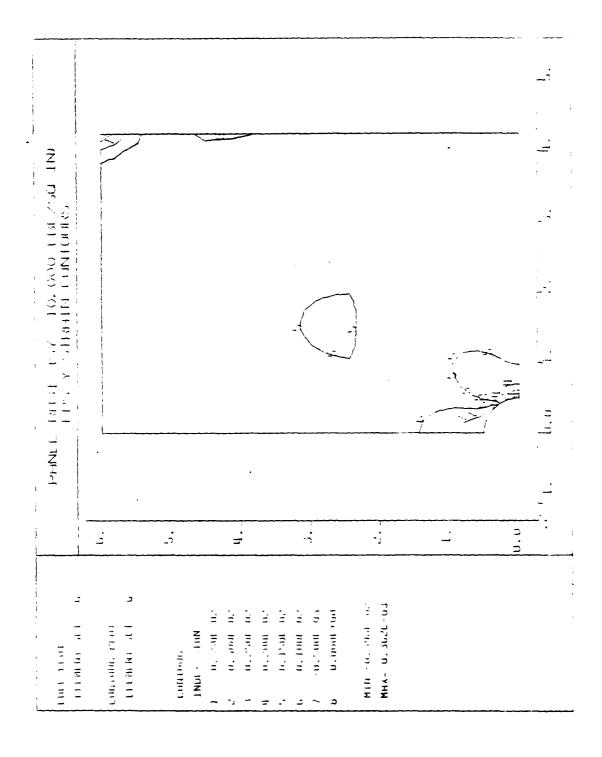
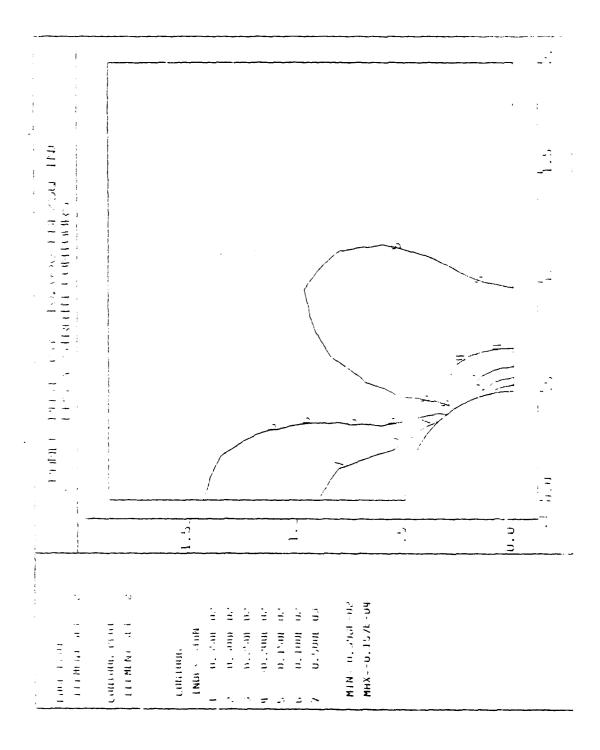


Figure L.5 Panel RH31: Eps-Y FEA Contours.

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Figure L.6 Panel RH31: Eps-Y FEA Contours Near the Cutout.

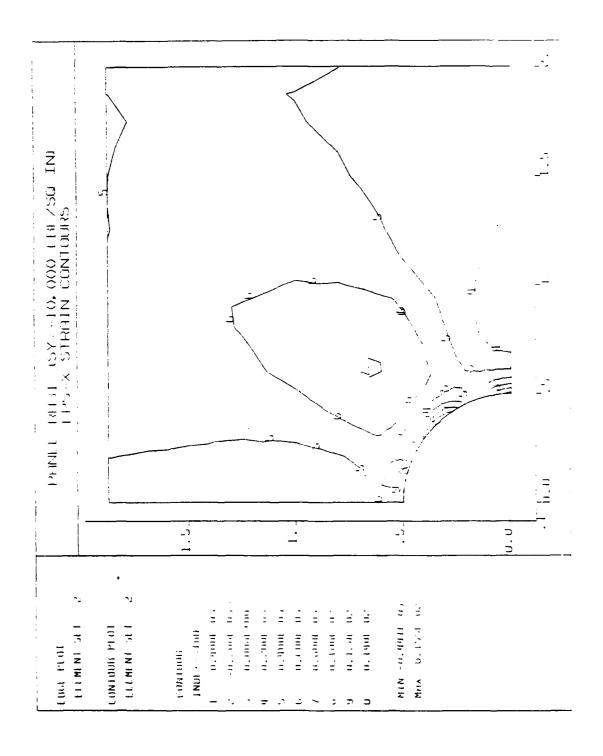


Figure L.7 Panel RH31: Eps-X FEA Contours Near the Cutout.

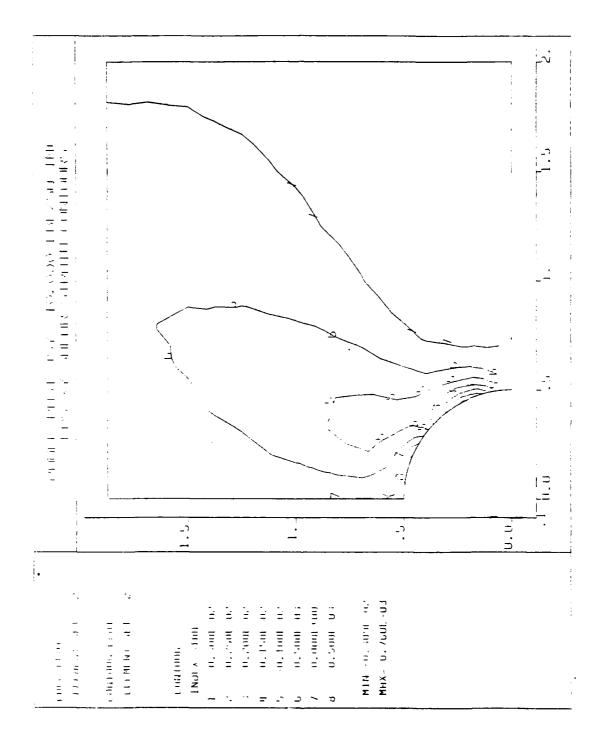


Figure L.8 Panel RH31: Eps-XY FEA Contours Near the Cutout.

APPENDIX M

PANEL RH42: ANALYTICAL AND EXPERIMENTAL DATA

Panel RH42 was reinforced with two co-cured plies of G/Ep in the shape of two strips on either side of the cutout on the outside of each facesheet offset 0.50 inch from the edge of the cutout. The reinforcement had the following dimensions:

Snape:	Strip		
Length:	3.14	in	
Width (each):	1.00	in	
Thickness (each):	0.028	in	(2 ply)
Area (each face):	6.280	in^2	
Total Volume:	0.352	in^3	
Net Cross Section:	0.112	in^2	

The panel failed at the hole edge (Type-1) at an applied normal stress of -36,990 psi $(\overline{\bf G}_n)$. Based strictly on the failure of the unreinforced panel and the computed stress concentration factor of 2.64 the predicted failure was $\overline{\bf G}_n = -34,650$ psi. The panel failed at 106.8% of the predicted ultimate stress. It sustained the highest load of any test specimen. The reinforcement increased the panel's weight little more than 3.6% and increased the failure strength by 21% over the unreinforced panel. It was one of the panels that led to the conclusion that several layers of reinforcement close to the cutout are more effective than spreading it out more thinly over a larger area.

The finite element model (mesh) is shown in Figure M.1. The area of the strip reinforcement is outlined by the heavy lines beginning 0.5" to the right of the cutout's edge.

Figure M.2 compares the three (finite element) computed strains around the cutout between the unreinforced panel ($PO\emptyset\emptyset$) and RH42. These computed strain values are listed in Table XLVI. There is a relatively small decrease in the strain due to the strip reinforcement compared with the equivalent amount of reinforcement concentrated next to the cutout.

Figure M.3 compares the computed (solid and dashed lines) and experimental (triangles) strains in the Y and X (poisson) directions in the panel and shows an excellent correlation between analytical and experimental strain at $\overline{\mathbf{O}}_n = -10,000$ psi. There was some strain variation between the left and right sides of the hole. The exact edge of the reinforcement can not be seen in the figure. The effects of reinforcement is a significant strain decrease (compared to the unreinforced panel, PODD) under the reinforcement, a small decrease near the hole and a slight increase in the far field (where x 2.50"). Table XLVII gives the computed values of the strains along the X axis.

Figure M.4 shows the stress-strain state during the load sequence from $\overline{\mathbf{O}}_{\mathrm{n}}$ = 0 to -36 ksi. Experimentally measured strain data are given in Table XLVIII. Up to about $\overline{\mathbf{O}}_{\mathrm{n}}$ = -24 ksi all gages indicated a normal stress-strain relation. At that load gage #2 (x = -0.571") demonstrated the "stair-step" phenomena. At -25 ksi gage #1 (x = +0.569") indicates what appears to be a softening or loss of stiffness--the strain rate drastically increased. Gage #2 seems to reflect the same behavior at -4 ksi higher stress. Gage #3 (x = +0.701") appears to pick up the load

when gage #1 shows what appears to be local buckling. Note that gages #8 and #13 (x = -1.512" and -2.460") reflect none of what is occurring next to the cutout.

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The reaction of this panel may help explain much of what occurs in the boundary region around the cutout on the other panels. At high levels of strain $(8,000 \text{ to } 10,000\,\mu\text{C})$ next to the cutout's edge, local delamination, buckling and fiber failure forces the transfer of the load path laterally away from the edge to the still intact and stiffer fibers and matrix farther from the cutout.

Figures M.5 through M.8 show the strain contours at σ_n = -10,000 psi computed and plotted using DIAL. Figure M.5 is the full quarter panel with strain (Eps-Y) parallel to the applied load. Figures M.6 through M.8 (Eps-Y, Eps-X and Eps-XY) show the strains in detail close to the cutout.

PANEL RH42 STRIP REINFORCEMENT PANEL MESH LAYOUT

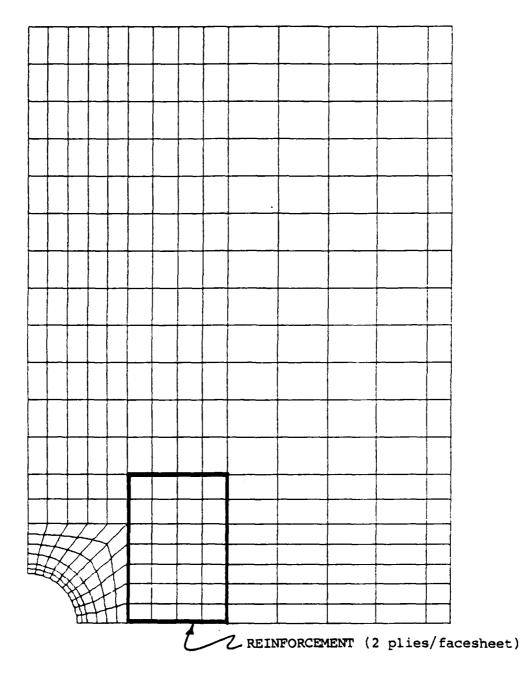
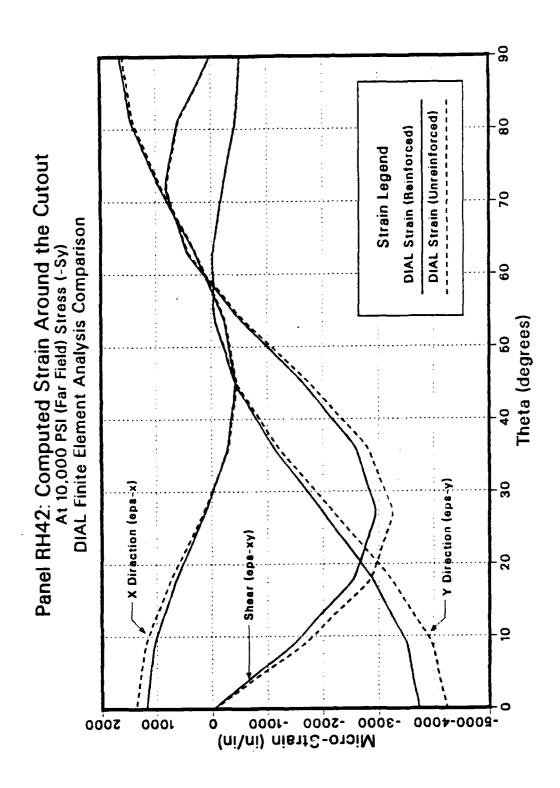


Figure M.1 Panel RH42: DIAL Finite Element Mesh.



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Figure M.2 Panel RH42: Strain Comparison Around the Cutout.

000 PSI).	EPS-XY	は、日本のでは、日本のは、日本のでは、日本のは、日本ので
THE CUTOUT (-10,000 PSI)	EPS-X	11111111111111111111111111111111111111
	EPS-Y	11111111111111111111111111111111111111
STRAIN DISTRIBUTION AROUND	Y COORD	00000000000000000000000000000000000000
RH42: LEFEA	X COORD	00000000000000000000000000000000000000
PANET,	NODE	

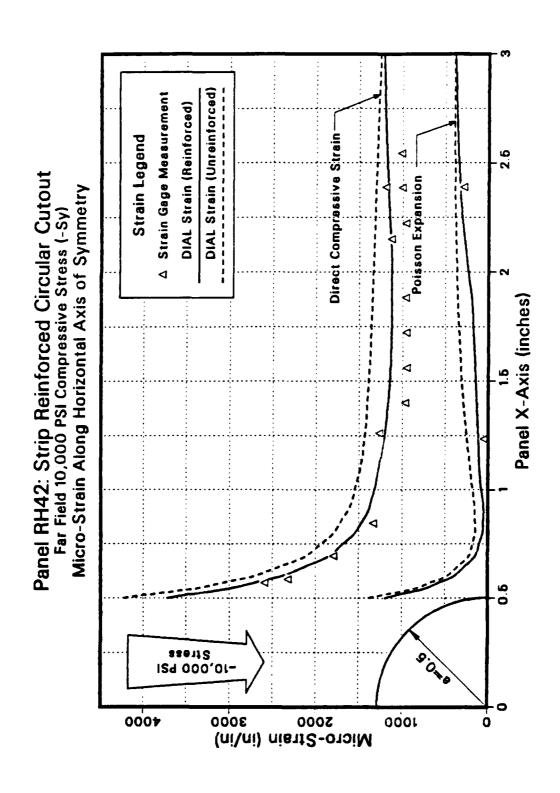


Figure M.3 Panel RH42: Strain Comparison Along the X Axis.

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PANET RH42: LEPEA STRAIN DISTRIBUTION ALONG THE X AXIS (-10,000 PSI).

EPS-XY	1652E- 1214E- 7504E- 6689E-	10.139899999999999999999999999999999999999	- 4469EE- - 2354EE- - 7561EE- 7360EE-	- 28 0 9 8 1 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	22 4 7 8 1 2 2 2 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	7887E-	4395E- 3135E- 2033E-	15568- 67678- 66498-	. 2/21E- 3485E- 3617E-
EPS-X	. 94 188 - 0 69 2 18 - 0 69 2 18 - 0 55 10 - 0	00.399999999999999999999999999999999999	- 55 - 55 - 55 - 55 - 56 - 56	76448-0 10358-0 11768-0	13.000 10.000 10.000 10.000 10.000	1912E-0 2348E-0 3053E-0	347881-0 37008-0 39058-0	- 000 - 000	. 39 2 1 1 1 0 1 39 1 5 E - 0 0 1 5 E - 0 0 1 5 E - 0
EPS-Y	0.3727E-0 0.3326E-0 0.2930E-0 0.2675E-0	-0.2406E-02 -0.2104E-02 -0.1682E-02	0.17 0.17 0.17 0.17 0.00 0.17 0.00 0.17 0.00 0.00	0.1323 0.12638 0.12048 0.12048	0000 0000 0000 0000 0000	0.112900 0.112900 112600 126000 1260	0.120 B-0 0.120 B-0 0.1219E-0	0.1221E-0	0. 1218E-0 0. 1218E-0 0. 1219E-0
Y COORD	0000 0000 0000 0000 0000	00000000000000000000000000000000000000		0000000000000000000000000000000000000	0000 0000 0000 0000 0000	0000 0000 0000		00000 00000 00000	0000 0000 0000
X COORD	50000 E + 0000 E + 00	0-6000 -65000 -65000 -7000 -75	2000 2000 2000 2000 2000 2000 2000 200	1125E+0	1500 1500 1600 1600 1600 1600 1600 1600	1875E+0 2000E+0 2750E+0	25 00 E+0 27 50 E+0 30 00 E+0	. 32 50 E+0 . 35 00 E+0 . 37 50 E+0	4125E+
DE									

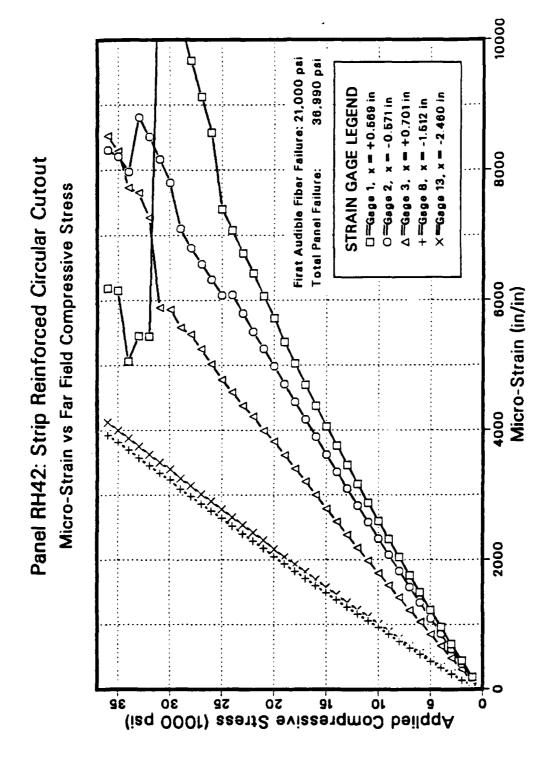


Figure M.4 Panel RH42: Microstrain vs. Compressive Stress.

TABLE XLVIII

PANEL RH42: SELECTED STRAIN GAGE VALUES DURING LOAD.

CON EXPERSOR EXPENSES BLOCK

Load (psi)	Mi	Micro-Strain Indicated by Gage:					
(501)	# 1	#2	#3	#8	#13		
00000000000000000000000000000000000000	539708945467067485762768905519393298 849529541976655792526127972763545648 146924703581470360370470351622944011 	752631613474451765948713882668889376 136803580358036814792580035818158923 	775690204695546969555184283155853901208644220988888900129178815886875292134680246791357924689235702458826725	315316515051087333599924995182643565 5433333455567787333599924995182643569 -1234567890123476801345688 -1-1-1-11111111222222222333333333333333	76601277441929503043631682725037461152456689022457013460245701450025702112345678012345767801124567801		

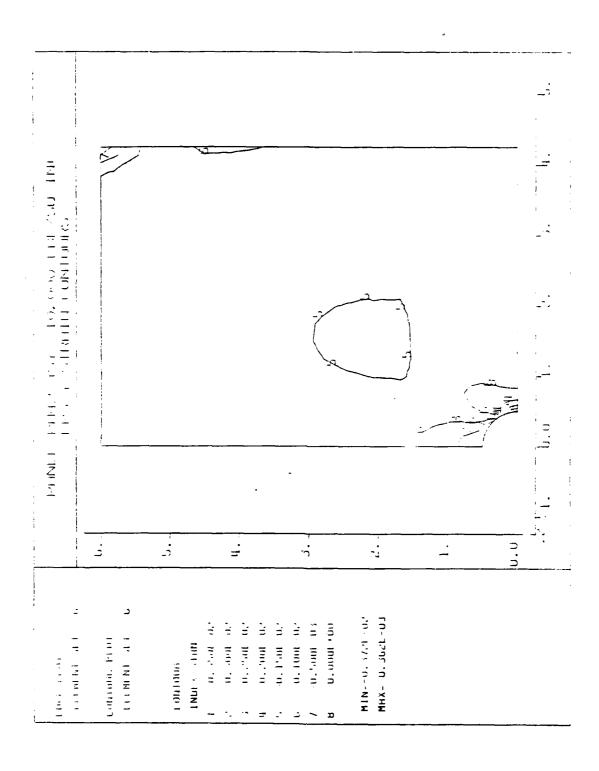


Figure M.5 Panel RH42: Eps-Y FEA Contours.

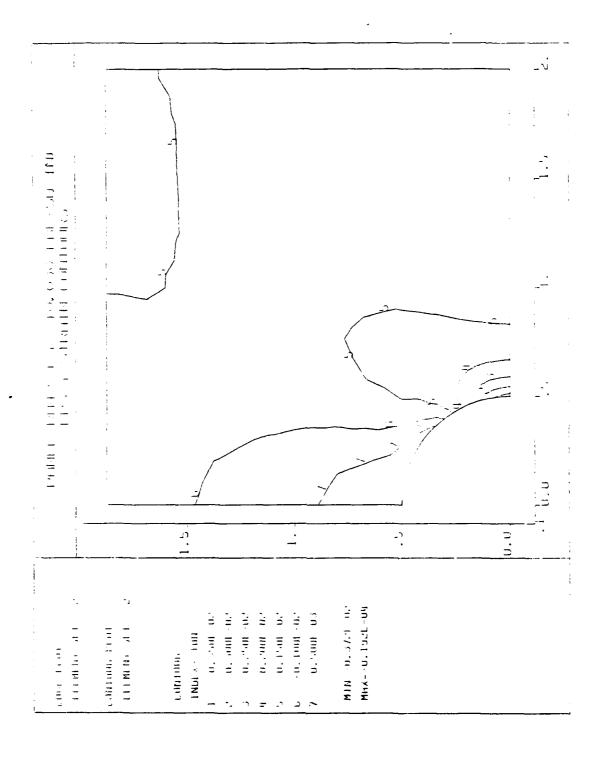
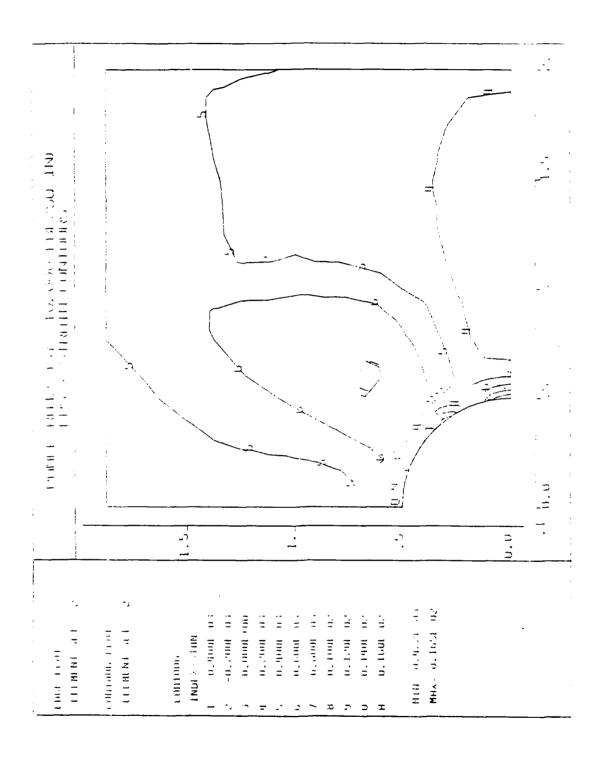
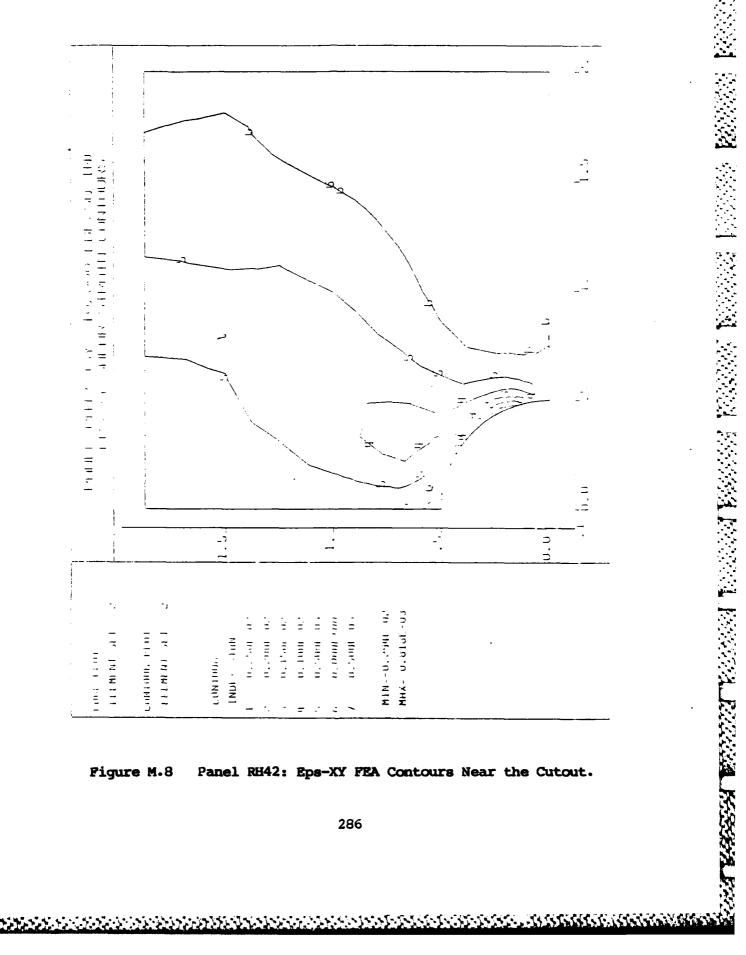


Figure M.6 Panel RH42: Eps-Y FEA Contours Near the Cutout.



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Figure M.7 Panel RH42: Eps-X FEA Contours Near the Cutout.



APPENDIX N

PANEL RH51: ANALYTICAL AND EXPERIMENTAL DATA

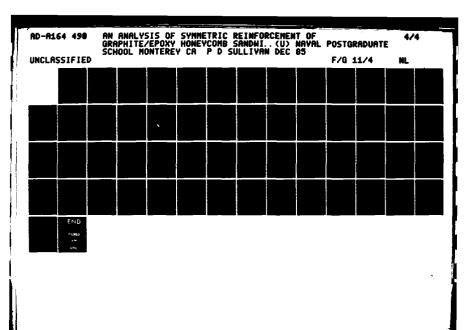
Panel RH51 was reinforced with one co-cured ply of G/Ep in the shape of two strips on either side of the cutout on the outside of each facesheet offset 0.50 inch from the edge of the cutout. The reinforcement had the following dimensions:

Shape:	Strip			
Length:	7.86	in		
Width (each):	1.00	in		
Thickness (each):	0.014	in	(1	ply)
Area (each face):	15.720	in^2		
Total Volume:	0.440	in^3		
Net Cross Section:	0.056	in^2		

The panel failed at the hole edge (Type-1) at an applied normal stress ($\overline{\sigma}_n$) of -31,630 psi. Based strictly on the failure of the unreinforced panel and the computed stress concentration factor of 2.83, the predicted failure was $\overline{\sigma}_n$ = -32,300 psi. The panel failed within 2.1% of the predicted ultimate load.

The finite element model (mesh) is shown in Figure N.1. The area of the strip reinforcement is outlined by the heavy lines beginning 0.50 inch to the right of the cutout's edge.

Figure N.2 compares the three (finite element) computed strains around the cutout between the unreinforced panel ($PO\emptyset\emptyset$) and RH51. These computed strain values are listed in Table XLIX.





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There is only a small apparent decrease in the strain around the cutout due to the reinforcement.

Figure N.3 compares the computed (solid and dashed lines) and experimental (triangles) strains in the Y and X (poisson) directions in the panel and shows a poorer than usual correlation between analytical and experimental strain at $\overline{\mathbf{O}}_n = -10,000$ psi. There was no apparent strain variation between the left and right side of the hole, but the finite element model predicted a higher level of strain at $\overline{\mathbf{O}}_n = -10$ ksi. From the appearance of the panel during the load sequence, this can not be explained. The finite element model was rerun to verify the results and the data is consistent with the other models. The effect of reinforcement is a very slight strain decrease (compared to the unreinforced panel, POO0) under the reinforcement and a small decrease near the cutout. Table L gives the LEFEA computed values of the strains along the X axis.

Figure N.4 shows the stress-strain relation during the load sequence from \vec{O}_n = 0 to -31 ksi. Experimentally measured strain values are given in Table LI. Both gages #1 and #2 (x = +0.569" and -0.571") show much higher strain rate than equivalent gages on other RH panels. Gage #3 at first parallels the strain rate of #1 and #2, then seems to indicate a load transfer away at -3 ksi and then again picks up the load at -9 ksi. Gages #1 and #2 show somewhat the same phenomena described in Appendix M: significant buckling and fiber failure close to the cutout and a transfer of the load path away from the cutout's edge. There may have also been a transfer of load from one side of the cutout to the other and to the opposing facesheet.

Figures N.5 through N.8 show the strain contours at $\overline{\boldsymbol{\sigma}}_n$ = -10,000 psi computed and plotted using DIAL. Figure N.5 is the full quarter panel with strain (Eps-Y) parallel to the applied load. Figures N.6 through N.8 (Eps-Y, Eps-X and Eps-XY) show the strains in detail close to the cutout.

PANEL RH51 STRIP REINFORCEMENT PANEL MESH LAYOUT

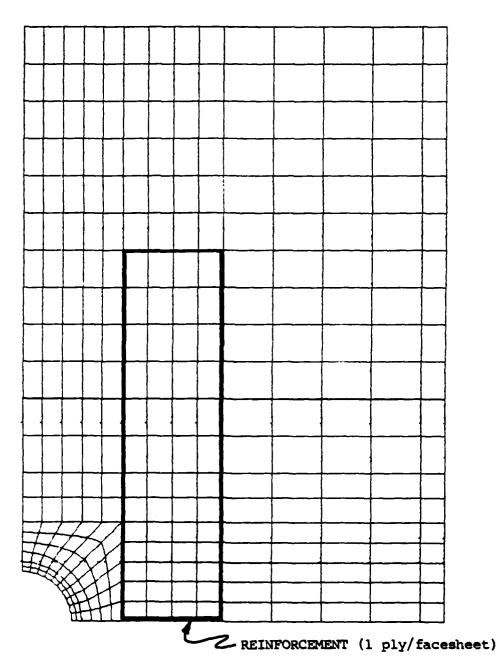


Figure N.1 Panel RH51: DIAL Finite Element Mesh.

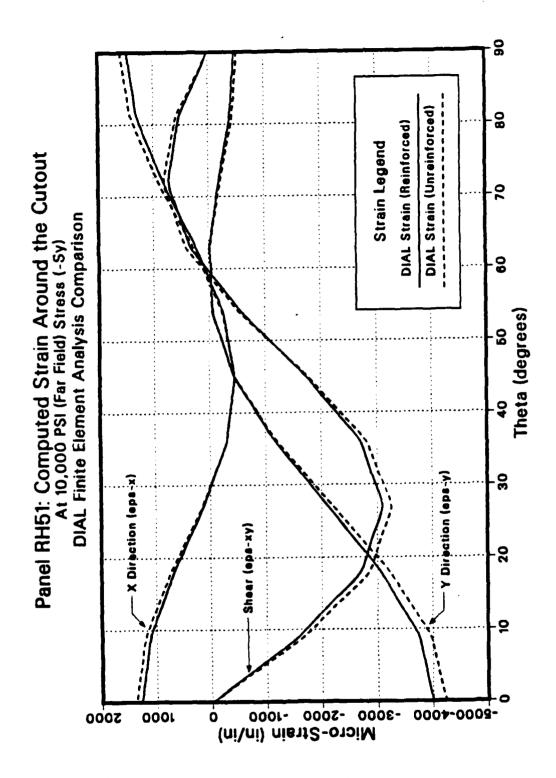


Figure N.2 Panel RH51: Strain Comparison Around the Cutout.

TABLE XILIX

COOK BUSINESS TO SERVICE STATE OF THE SERVICE STATE

(-10,000 PSI).	EPS-XY	00000000000000000000000000000000000000
THE CUTOUT (-10	EPS-X	00000000000000000000000000000000000000
DISTRIBUTION AROUND '	EPS-Y	11111111111111111111111111111111111111
Strain distrii	Y COORD	00000000000000000000000000000000000000
EL RH51: LEPEA	X COORD	00000000000000000000000000000000000000
PANEL	NODE	

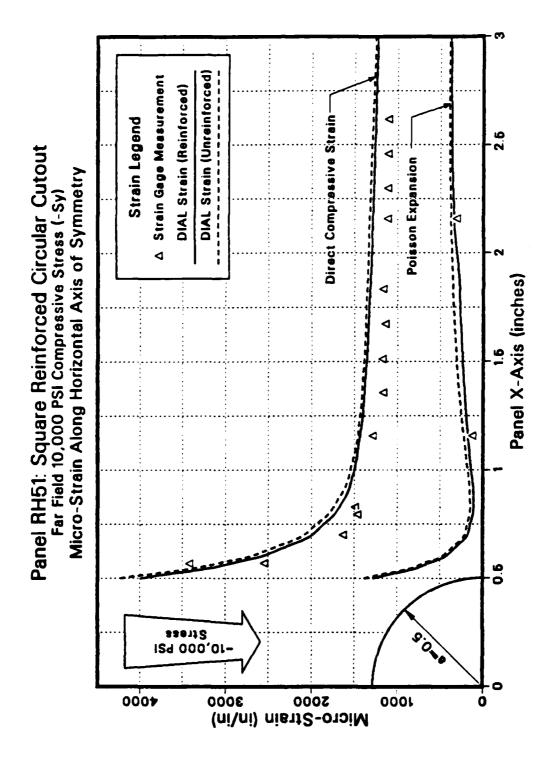


Figure N.3 Panel RH51: Strain Comparison Along the X Axis.

PART P

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PANEL RESI: LEPEA STRAIN DISTRIBUTION ALONG THE X AXIS (-10,000 PSI).

EPS-XY	
EPS-X	00000000000000000000000000000000000000
EPS-Y	00000000000000000000000000000000000000
Y COORD	
X COORD	00000000000000000000000000000000000000
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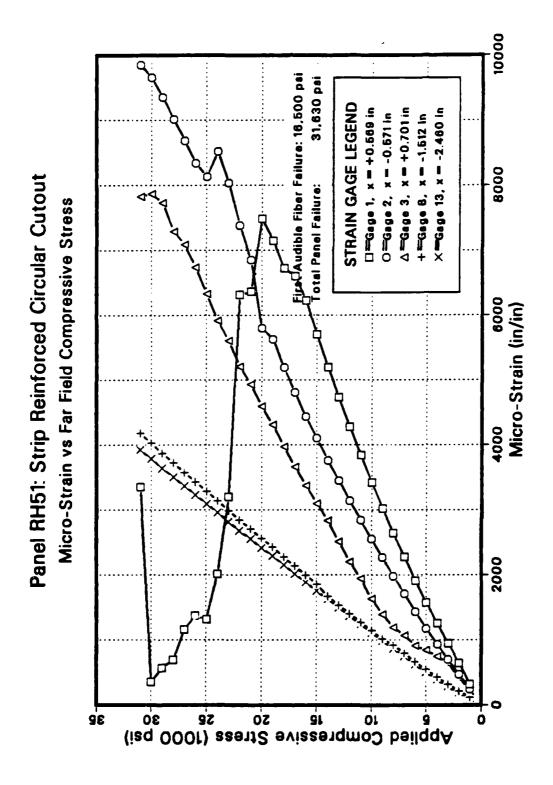
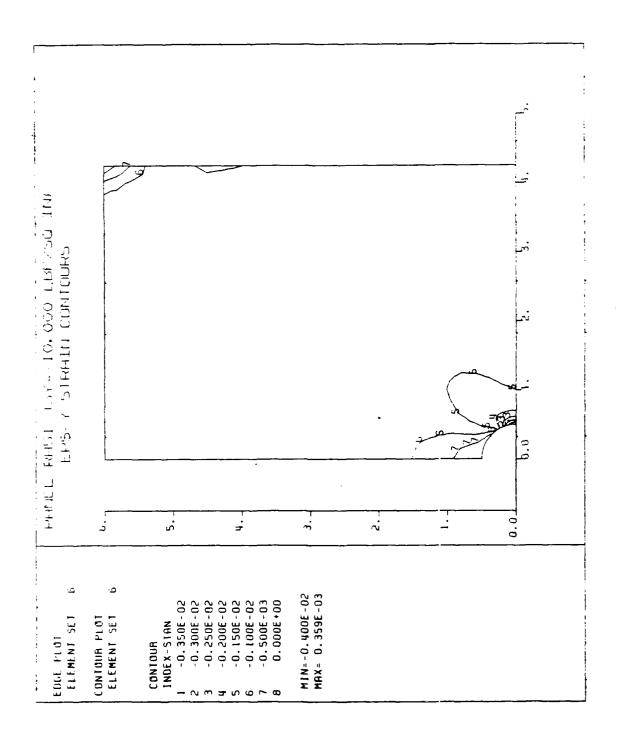


Figure N.4 Panel RH51: Microstrain vs. Compressive Stress.

TABLE LI
PANEL RH51: SELECTED STRAIN GAGE VALUES DURING LOAD.

Load (psi)	M.	icro-Strain	Indicate	d by Gage:	
12/	#1	#2	#3	#8	#13
12345678901111116789012345678901	7266236902163669138675764200699 	19613510801062138002725437654693731108010621380027254373186544460309304883133815546889368899998	491597014641178035813558112 2467897994641178035813558170 	658825397221+686687944875851250 	11231567891369258159157159260482 112315678912346780124568902355678 1112315678912346780124568902355679
30000 31000	-566 -349 -3349	-9354 -9656 -9848	-7289 -7730 -7866 -7831	-3872 -4025 -4180	-3641 -3785 -3927



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Pigure N.5 Panel RH51: Eps-Y FEA Contours.

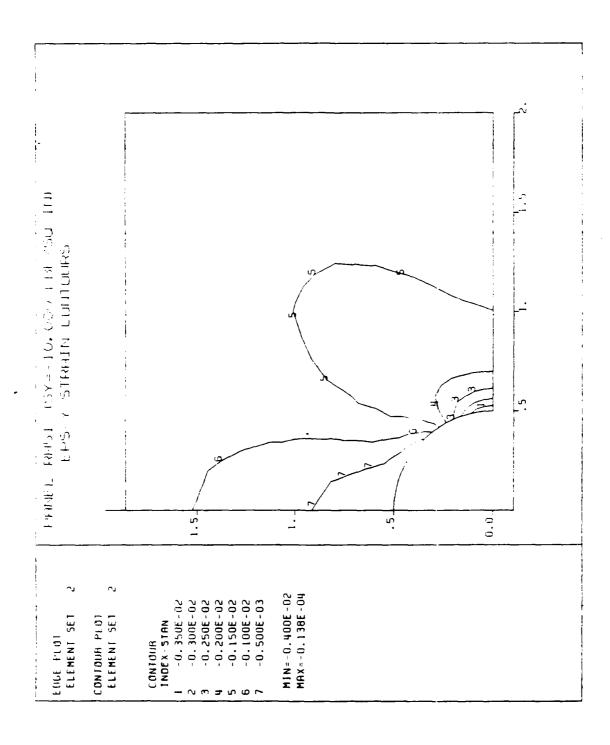
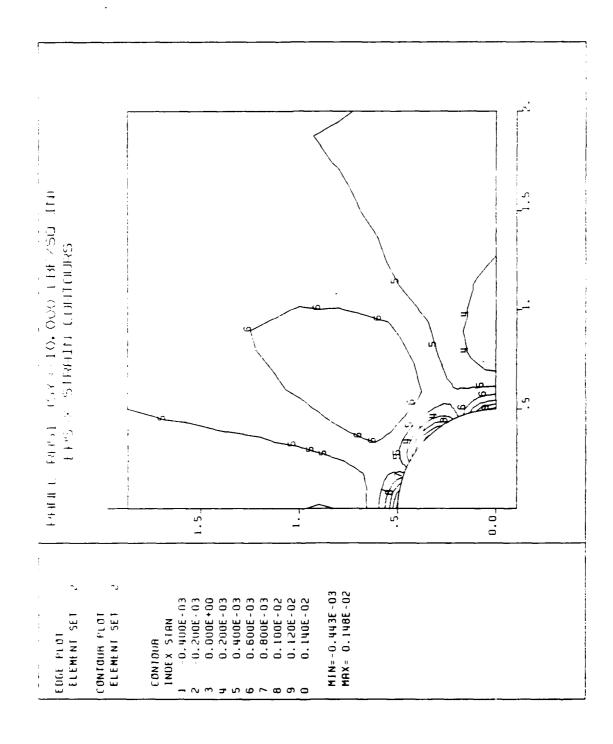
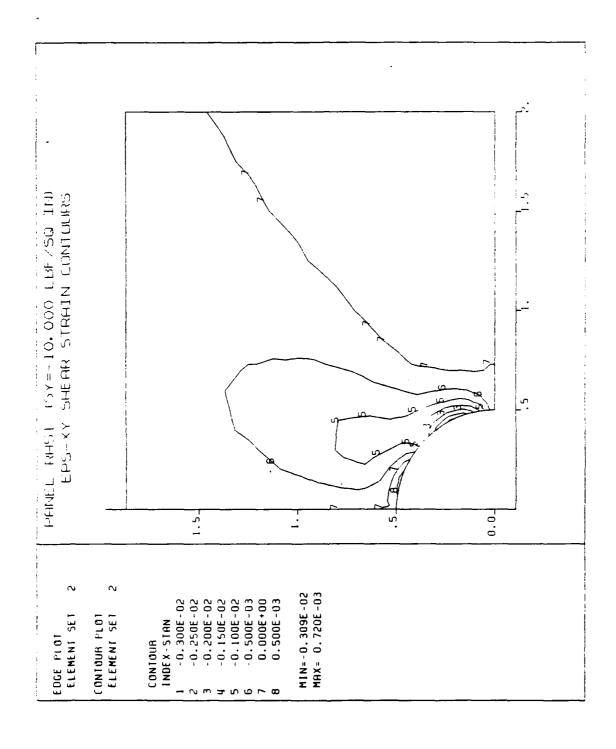


Figure N.6 Panel RH51: Eps-Y FEA Contours Near the Cutout.



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Figure N.7 Panel RH51: Eps-X FEA Contours Near the Cutout.



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Figure N.8 Panel RH51: Eps-XY FEA Contours Near the Cutout.

APPENDIX O

PANEL RR22: THREE-DIMENSIONAL LINEAR FINITE ELEMENT ANALYSIS

Panel RR22 was reinforced with two co-cured round plies of G/Ep around the cutout on the outside of each facesheet. The reinforcement configuration should have been among the most efficient, concentrating the maximum amount of reinforcement close to the cutout. Figure 5.3 and Table VI show that the round, 200% reinforcement produced about a 22.5% reduction in maximum strain (eps-y) parallel to the applied load. The round, 400% reinforcement with twice the volume of additional weight provided only 3.1% additional strain reduction. It was therefore more than a little disconcerting when the most promising panel failed at $\vec{O}_{\rm n}$ = 21,050 psi, only 55% of the predicted load. Table IX gives the predicted failure (based on the actual failure of the unreinforced panels and the LEFEA computed SCF) at 38,250 psi.

When trying to explain the failure, it was postulated that the facesheet layup $[0_3,\pm45,90]$ may have caused out-of-plane stresses $(+C_z)$ sufficient to cause the facesheet to separate from the core. This, of course, would have invalidated the entire thesis that local reinforcement around a cutout could be a significant design benefit. The two-dimensional LEFEA (see section III C.1) used in the computational analysis was not able to give stress or strain in the Z direction.

A three-dimensional analysis was undertaken. Figure O.1 shows the three-dimensional mesh. In order to conserve computer time and provide an accurate solution, the quarter panel was modeled only from the midplane (z=0.0). Modeling only half the core and and one facesheet did not affect the accuracy of the solution. In order to approximate the strain closer to the predicted failure, the model was subjected to an equivalent applied load of 30 ksi rather than the 10 ksi used on the 2-D models. The analysis was linear and did not take into account the very probable matrix cracking and non-linear behavior at high strain ($10,000 \, \mu \, \text{e}$). Table LII summarizes the results of the analysis.

TABLE LII

PANEL RR22: SUMMARY OF THREE-DIMENSIONAL LEFEA STRAIN

Direction:	Y	x	z	XY	YZ	ZX	
Maximum	1140	4690	92	2420	273	2100	~
Minimum	-10100	-2720	-11	- 9300	- 1060	-422 0	

Figure 0.2 gives the strain parallel to the applied load. The maximum predicted stain was $10,100\,\mu$ E at $\overline{\mathbf{O}}_{\mathrm{n}}=30\,\mathrm{ksi}$. This is exactly three times the maximum strain computed in the 2-D model described in Appendix C (see Figure C.5). The exact analytical correspondence of the 2- and 3-D FEA helps to validate it. Figure 0.3 shows the $\mathbf{E}_{\mathbf{y}}$ strain near the cutout. Figure 0.4 shows $\mathbf{E}_{\mathbf{x}}$ next to the cutout. This corresponds with Figure C.7.

The strain in the Z direction is shown in Figures 0.5 and 0.6. The maximum was $92\,\mu$ C, the minimum $-11\,\mu$ C. The stress at the interface of the facesheet and honeycomb core is shown in Figures 0.7 and 0.8. It is obvious that the out-of-plane stress at the interface is virtually nil (less than +5 psi) and that premature

failure was <u>not</u> due to the layup or the reinforcement configuration.

The shear strains $\boldsymbol{\epsilon}_{\mathbf{x}\mathbf{y}}$, $\boldsymbol{\epsilon}_{\mathbf{y}\mathbf{z}}$ and $\boldsymbol{\epsilon}_{\mathbf{z}\mathbf{x}}$ are shown in Figures 0.9, 0.10 and 0.11 respectively. The three-dimensional analysis reversed the sign on the shear strain from the two-dimensional. Comparing the results of the 2- and 3-D analyses, the maximum and minimum $\boldsymbol{\epsilon}_{\mathbf{x}\mathbf{y}}$: 2420 and -9300 $\boldsymbol{\mu}\boldsymbol{\epsilon}$ in the 3-D (Figure 0.9) are almost exactly 3 times the 2-D: 826 and -3110 $\boldsymbol{\mu}\boldsymbol{\epsilon}$ (Figure C.8).

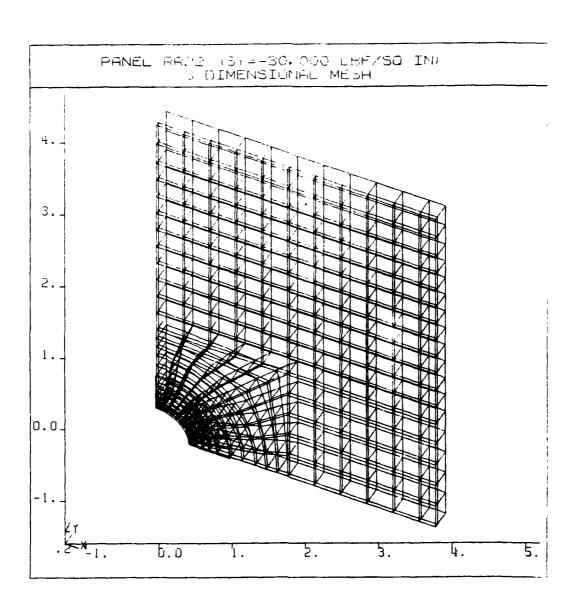


Figure 0.1 Panel RR22: 3-D DIAL Finite Element Mesh.

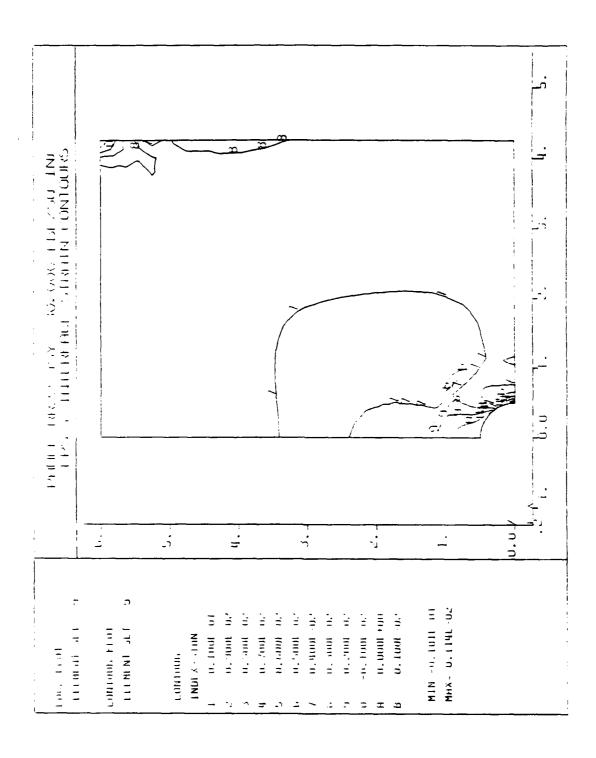
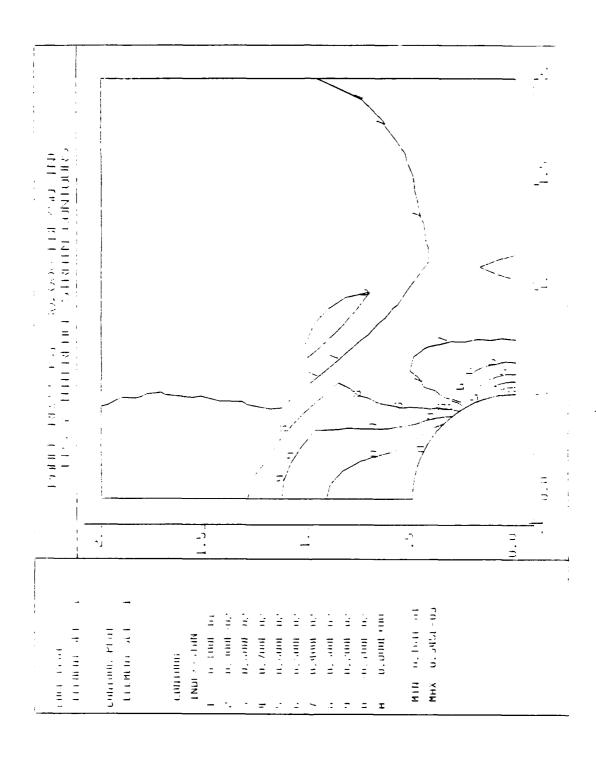


Figure 0.2 Panel RR22: 3-D Eps-Y FEA Contours.



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Figure 0.3 Panel RR22: 3-D Eps-Y FEA Contours Near the Cutout.

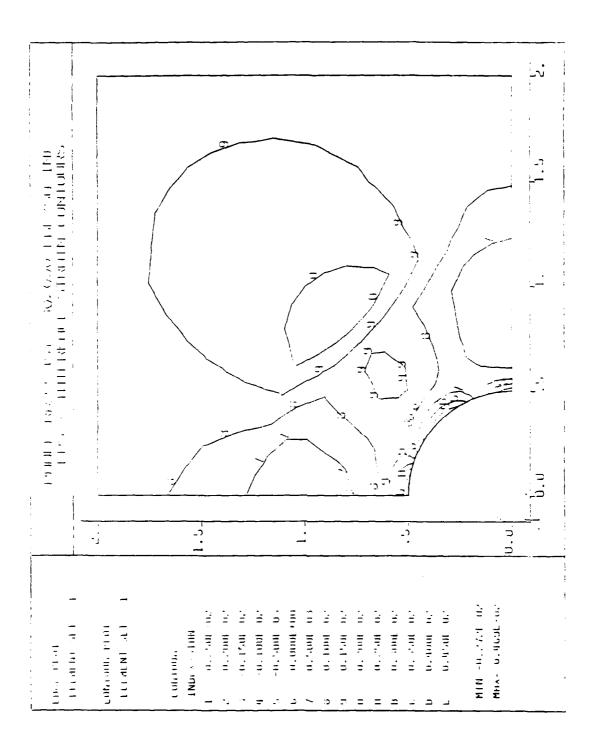


Figure 0.4 Panel RR22: 3-D Eps-X FEA Contours Near the Cutout.

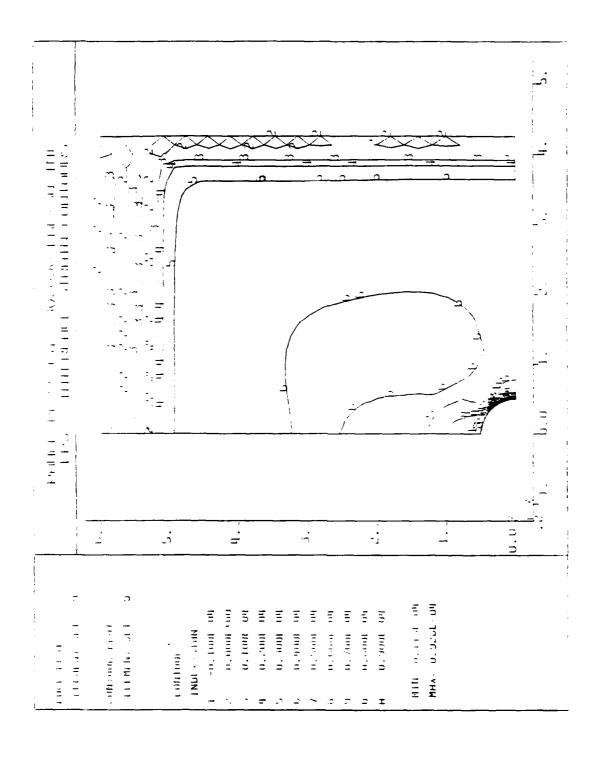


Figure 0.5 Panel RR22: 3-D Eps-Z FEA Contours.

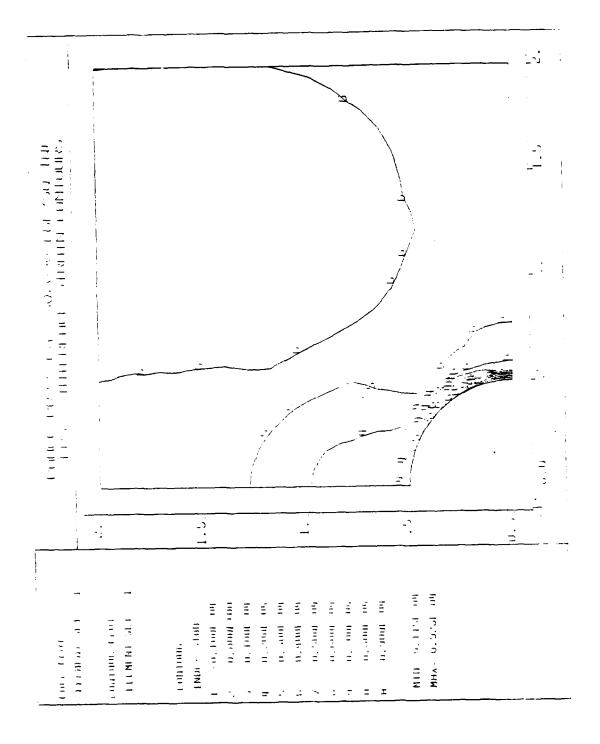


Figure 0.6 Panel RR22: 3-D Eps-Z FEA Contours Near the Cutout.

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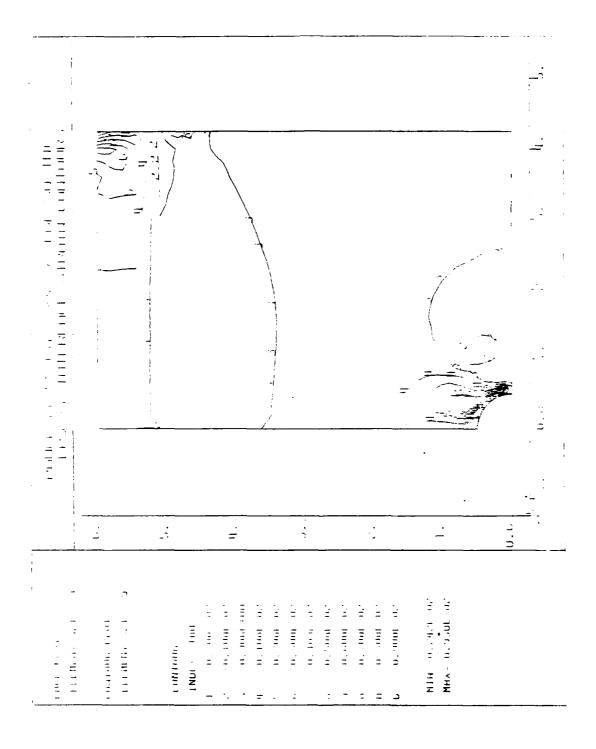


Figure 0.7 Panel RR22: 3-D Eps-XY FEA Contours.

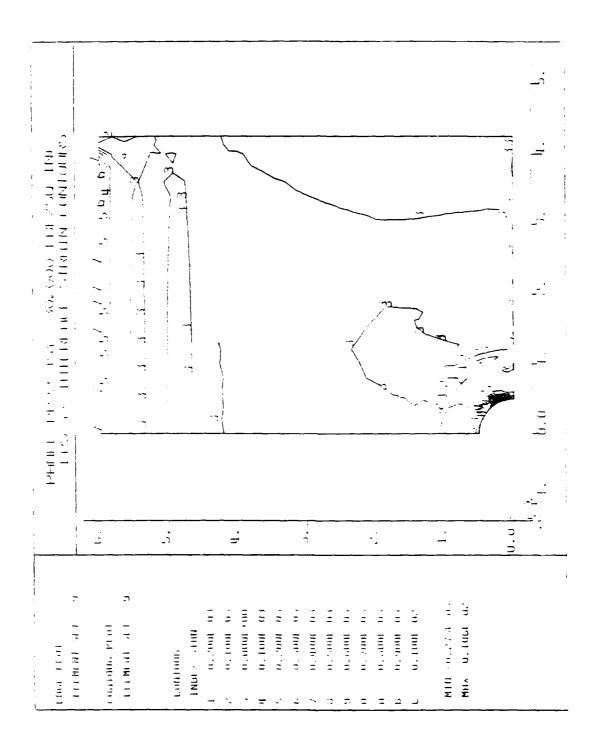


Figure 0.8 Panel RR22: 3-D Eps-YZ FEA Contours.

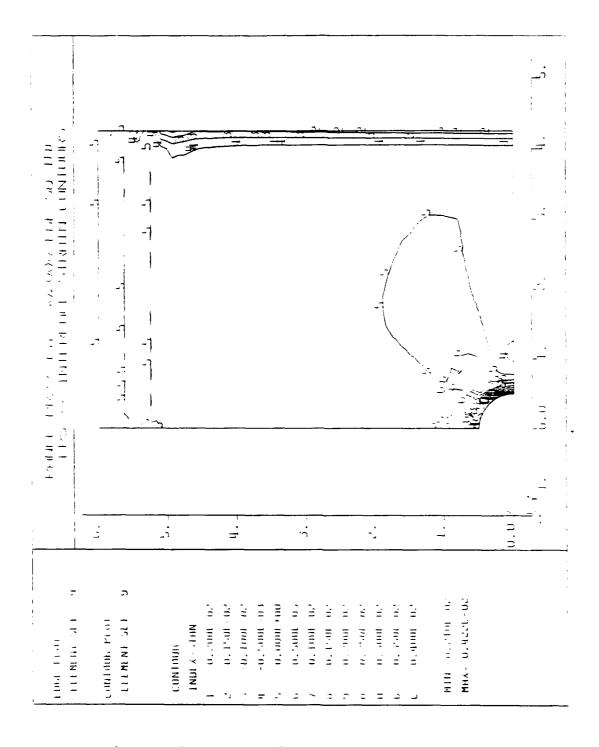
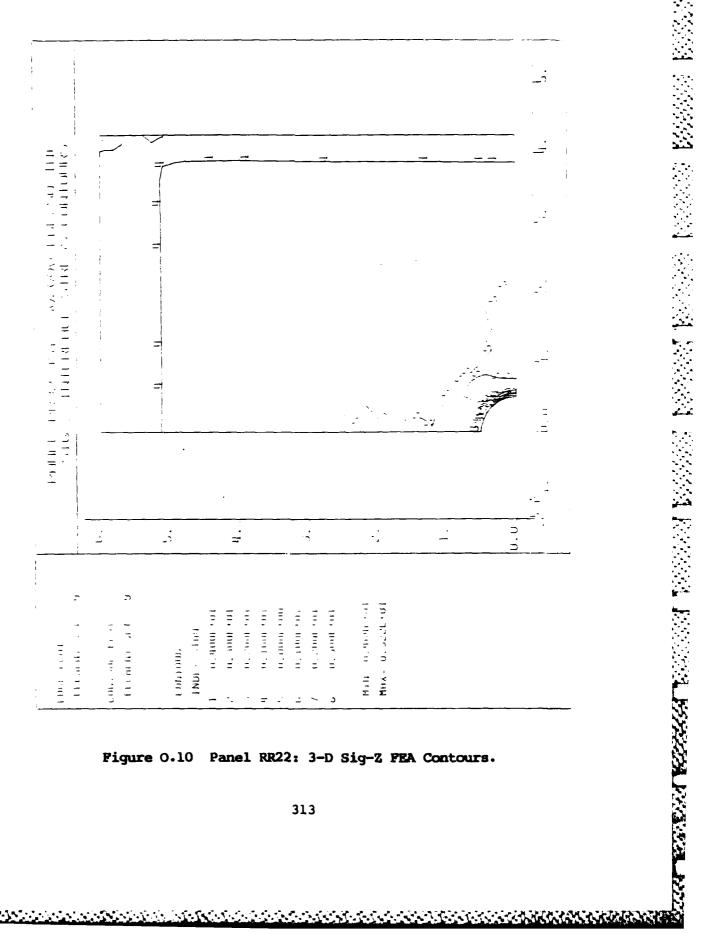
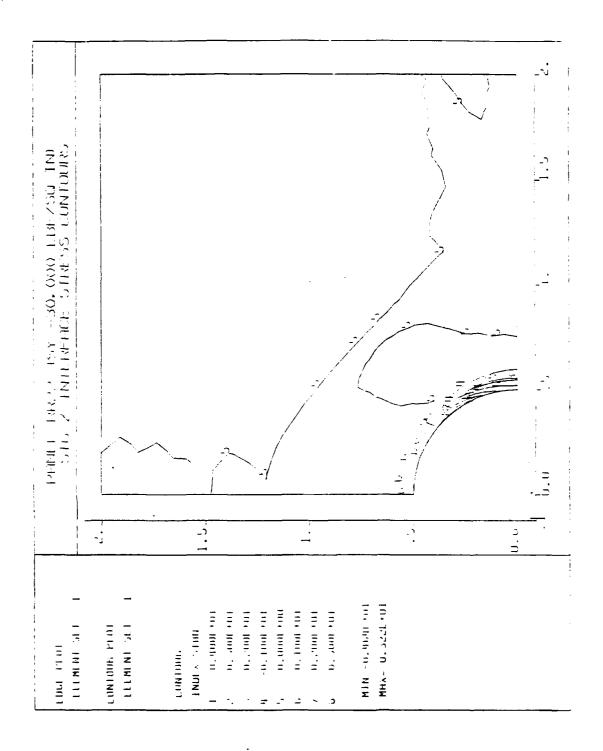


Figure 0.9 Panel RR22: 3-D Eps-ZX FEA Contours.



Panel RR22: 3-D Sig-Z FEA Contours. Figure 0.10



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Figure 0.11 Panel RR22: 3-D Sig-Z FEA Contours Near the Cutout.

APPENDIX P

FORTRAN PROGRAM "RBSFM"

This program written in FORTRAN was developed by S.P. Garbo and J.M. Ogonowski of McDonnell Aircraft Company, McDonnell-Douglas Aircraft Corporation, PO Box 516, St. Louis, MO 63166. It was published by the Air Force Flight Dynamics Laboratory, Wright Aeronautical Laboratories, Wright-Patterson Air Force Base, Ohio 45433 as report AFWAL-TR-81-3041, Volumes 1-3.

The program was modified by the author to run on the IBM 370. The code was renumbered, the input method and output format was altered for easier input.

```
RESFM VER 2. 2 11/09/83 PAT SULLIVAN I/O MODIFICATION TO RUN FROM INPUT FILZ.
                                      PAT SULLIVAN AERO ENGINEERI

LES: 01-READ DATA, 02-WRITE RESULTS, 03-SUMMARY OF INPUT

COMMON /ONE/ E1(3), 22(3), G12(3), V12(3),
COMMON /TWO/ ICUT(15), NUMPLY, NUMMAT, ANG(8), PLYTHK(8), MATID(8),
COMMON /TWO/ ICUT(15), NUMPLY, NUMMAT, ANG(8), PLYTHK(8), MATID(8),
COMMON /FOUR/ EX, EY, PXY, P, PW, ALPHA, BETA, DIA, CORREC,
COMMON /FIVE/ PIT(3), FXC(3), FYT(3), FIC(3), FXY(3), IFAIL

COMMON /SIX/ A1(3,3),
COMMON /SEVEN, S(3,3),
COMMON /SEVEN, S(3,3),
COMMON /SEVEN, S(3,3),
COMMON /SIZH / STR1(8,20,91), STR2(8,20,91), STR1(2(8,20,91), INTEGER ANS, ANSZ, YES, IANG, ILOW, IHIGH, BANGE

DIMENSION TITLE(16)

DATA RANGE/O/
                      READ INPUT FILE IN PREE FORMAT FOR ALL REQUIRED DATA.
                                            DO 10 L=1,15
ICUT(L)=0
10
                                            CONTINUE
                                           READ
READ
READ
READ
READ
                                                                                                                     TITLE
(IOUT(I), L=1,10)
NUMPLY, NUMBAT,
(E1(J), E2(J), G12(J), V12(J), J=1, NUMMAT)
(FX1(J), FXC(J), FYT(J), FYC(J), FYY(J), J=1, NUMMAT)
(ANG(J), PLTIEK, J), MATID(J), J=1, NUMPLY)
PX, FY, FX, SETA, P, ALPHA
W, DIA, IFAIL
ILOW, IHIGH, IANG, STPINK, NUMSTP
 C
                                          IF (NUMSTP.GT. 20) NUMSTP=20
IF (IANG. 50.0) GO TO 20
RANGE=IFIX(PLOAT(IHIGH-ILOW)/PLOAT(IANG))
CONTINUE
IF (RANGE.GT. 91) WRITE (2,180)
IF (RANGE.GT. 91) STOP
BL=P*DIA
PW=0.0
IF (P. NE. O. O. AND. W. NE. O. O) PW=PL/(2. O*W)
WD=W/DIA
  20
  C WRITE A SUMMARY OF THE INPUT DATA TO THE OUTPUT FILE
                                WRITE (2,90) (100T (L), L=1,10)
WRITE (2,10) (1,21 (J),22 (J),G12 (J),V12 (J),FXT (J),FXC (J),FYT (J),
   30
  40
                          ERANCH TO SUBROUTINES AS DIRECTED BY THE OFTION LIST
                                             IF (PUTOUT(IOUT,2).EQ.0.0) GO TO 60 ALFH=ALPHA CALL ABD (ALPH)
```

```
CORREC = 1.0
DUMMY = PUTOUT (ICUT, 98)
CONTINUE
50
C
                                       IF (PUTOUI(IOUI,3).EQ.0.0) GO TO 60 CALL LAMSTR
C
                                      IF (PUTOUT(IOUT,7).EQ.0.0) GO TO 60 CALL PLYSTR (IFAIL)
C
                                       IF (PUTOUI(IOUI,9).EQ.0.0) GO TO 60 CALL FAIL
c
                                       IF (20TOUT (100T, 10) . 20. 2. 0) DUMMY=PUTOUT (100T, 99) IF (CORREC.LT..999.08.CORREC.GT. 1.001) GO TO 50
 Ç0
                                       CONTINUE
DU MNY = PUTCUT (ICUT, 98)
If (PUTCUT(ICUT, 1). NE.2.0) GO TO 70
CCNTINUE
 70
C-
                               STOP
FORMART (16(A4))
FORMART (15(A4))
F
 80
  120
   130
   140
   160
   170
    180
     190
   DIMENSION TOUT (15)
                                           DATA=0.0
PUTOUT=0.0
PUTOUT=0.0
DO 10 J=1.15
IF (10 UT (1) .GE.IN) PUTOUT=1.0
CONTINUE
DO 20 J=1.15
IF (10 UT (1) .EQ.IN) PUTOUT=2.0
CONTINUE
CONTINUE
IF (DATA.EQ.1.0.AND.IN.LT.10) PUTOUT=0.5
      10
```

```
RETURN
ENC
SUBROUTINE ABD (ALPHA)

S/R ABD VER 1.1 4/25/83 PDS AERO ENGINEERING -
SUBROUTINE CALCULATES A,B,D MATRICIES AND INVERSION MATRICI
                COMMON /ONE/ E1(3), E2(3), G12(3), V12(3)

COMMON /TWO/ IOUT (15), NUMELI, NUMMAT, ANG (8), PLYTHK (8), MATID (8)

COMMON /SIX/ A1(3,3)

COMMON /SEVEN/ S(3,3)

DIMENSION V21(3), CIV(3), Q11(3), Q22(3), Q12(3), Q66(3), U1(3), U2(3), U3

1(3), U4(3), U5(3), CEAR (8,3,3), ZZ(20), Z(20), Q(3,3), AA(3,3), A(3,3)

DATA P1/3.14(15)26535/
     CALCULATE THE INVARIENTS (U) PROM THE Q MATRIX FOR EACH MATERIAL

DO 20 M=1 NUMMAT

U1(M) = (3.0*011 (M) +3.0*022 (M) +2.0*012 (M) +4.0*066 (M)) /8.0

U2(M) = (011 (M) -C22 (M) )/2.0

U3(M) = (011 (M) +C22 (M) -2.0*012 (M) -4.0*066 (M)) /8.0

U3(M) = (011 (M) +C22 (M) -2.0*012 (M) -4.0*066 (M)) /8.0

U5(M) = (011 (M) +C22 (M) -2.0*012 (M) +4.0*066 (M)) /8.0

CONTINUE
20
                   DO 30 I=1,3
DO 30 J=1,3
A (I,J) =0.0
AA (I,J) =0.0
CONTINUE
          TRANSFORMED REDUCED STIFFNESS MATFIX FOR EACH PLY
                   THICK=0.
DO 10 L=1.NUMPLY
DEG=ANG(L)*PI/180.0
H=NATID(L)
C
                    QBAR (L, 1, 1) = U1 (M) +U2 (M) *COS (2.0*DEG) +U3 (M) *COS (4.0*DEG) QBAR (L, 1, 2) = U4 (M) -U3 (M) *COS (4.0*DEG) +U3 (M) *COS (4.0*DEG) QEAR (L, 2, 2) = U1 (M) -U2 (M) *COS (2.0*DEG) +U3 (M) *COS (4.0*DEG) QBAR (L, 2, 3) = 0.5*U2 (M) *SIN (2.0*DEG) +U3 (M) *SIN (4.0*DEG) QBAR (L, 2, 3) = U5 (M) -U3 (M) *COS (4.0*DEG) +U3 (M) *SIN (4.0*DEG) QEAR (L, 3, 3) = U5 (M) -U3 (M) *COS (4.0*DEG) QEAR (L, 3, 1) = QBAR (L, 1, 1, 2) QEAR (L, 3, 2) = QEAR (L, 2, 3)
                    THICK= PLYTHK (L) +THICK ZZ (L+1) = THICK CONTINUE Z (1) =- 1.0 + THICK/2.0
40
          CALCULATE THE A MATRIX
                   DO 70 I=1,3

DO 60 J=1,3

DO 50 L=1,3UHPLY

Z(L+1) = Z(1) + ZZ(L+1)

ZI=Z(L+1) - Z(L)

A(IJ) = A(IJ) + QEAR(L,I,J) + ZA

COUTINUE
          MATRIX Q AND QQ ARE MATRICIES USED IN CALCULATIONS FOR THE MANIPU-
```

```
LATION OF OTHER MATRICIES
                    O(I,J) = A(I,J) / THICK
CONTINUE
CONTINUE
                     COMPUTE A/THICK INVERSE MATRIX
                    ISTEP=1
CALL INVERS (Q, AI)
                    THICK=0.0

ALPHA= ALPHA+PI/180.0

DO 80 L=1,NU3PIY

DIG=ANG(L)*PI/180.0

DEG=DEG-ALPHA

M=MATID(L)
                     QBAR (L, 1, 1) = U1 (M) +U2 (M) *COS (2.0*DEG) +U3 (M) *COS (4.0*DEG) QBAR (L, 1, 2) = U4 (M) -U3 (M) *COS (4.0*DEG) QBAR (L, 1, 2) = U1 (M) -U2 (M) *COS (4.0*DEG) +U3 (M) *COS (4.0*DEG) QBAR (L, 1, 3) = 0.5*U2 (M) *SIN (2.0*DEG) +U3 (M) *SIN (4.0*DEG) QBAR (L, 2, 3) = 0.5*U2 (M) *SIN (2.0*DEG) -U3 (M) *SIN (4.0*DEG) QEAR (L, 3, 3) = U5 (M) -U3 (M) *COS (4.0*DEG) -U3 (M) *SIN (4.0*DEG) QBAR (L, 2, 1) = U5 (M) -U3 (M) *COS (4.0*DEG) QBAR (L, 3, 1) = U5 (M) -U3 (M) *COS (4.0*DEG) QEAR (L, 3, 1) = QEAR (L, 1, 3) QEAR (L, 1, 3, 2) = QBAR (L, 2, 3)
THICK= PLYTHK (L) + TEICK
ZZ (L+1) = TRICK
CONTINUE
Z (1) = -1.0 + THICK/2.0
C CALCULATE AA HATRIX
                    DO 110 I=1,3

DC 100 J=1,3

DC 90 L=1,NUMPIY

Z(L+1)=Z(1)+ZZ(L+1)

ZA=Z(L+1)-Z(L)

AA[I,J]=AA(I,J)+QEAR(L,I,J)*ZA

CONTINUE

Q(I,J)=AA(I,J)/THICK

CONTINUE

CONTINUE
          COMPUTE AA/THICK INVERSE MATRIX
                     ISTEP=4
CALL INVERS (Q,S)
 C PRINT MATRIX AND LAMINATE DATA
                     IF (PUTOUT(IOUT, 2).NE.2.) GO TC 120
WEITE {2,130} {{AA(I,1), AA(I,2), AA(I,3), I=1,3}
WEITE {2,140} {{O(I,1), O(I,2), S(I,3), I=1,3}
CONTINUE
           CFF-AXIS LAMINATE PROPERTIES
```

```
GXY2=1.0/S(3,3)
                                            FURN (10X,9HA MATRIX: //.3(10X,3(1FE14.3)./)./)
FORMAT (10X,1HA/T HATRIX: //.3(10X,3(1FE14.3)./)./)
FORMAT (10X,15HA/T HATRIX: //.3(10X,3(1FE14.3)./)./)
FORMAT (10X,15HA/T HATRIX: //.3(10X,3(1FE14.3)./)./)
FORMAT (10X,15HA/T HATRIX: //.3(10X,3(1FE14.3)./)./)
FORMAT (10X,15HA/T HATRIX: //.3(10X,3(1FE14.3)./)./)
FORMAT (10X,15HEX = .611.3.5X.6HVXY = .0PF8.4.//.10X,30HS
LEND SUBROUTINE INVERS (X.XI)
                          S/R INVERS
CALCULATES THE INVERSE OF A 3X3 MATRIX

DIMENSION X(3,3), XI(3,3)

COMMON ISTEP

DET=(X(1,1)*X(2,2)*X(3,3))+(X(1,2)*X(2,3)*X(3,1))+(X(1,3)*X(2,1)*X(3,2))-(X(1,3)*X(2,2)*X(3,1))-(X(1,1)*X(2,3)*X(3,2))-(X(1,2)*X(2,1)*X(2,1)*X(3,3))

IF (DET-EQ.0.0) GC TO 10
C
               XI (3,2) = (I(2,1) = XII, ...,

GO TO 20
WBITE (2,30) ISTEF
CONTINUE

RETURN
FORMAT (49H SUEROUTINE INVERSE CALCULATES A SINGULAR HATRIX ,7HAT
1SITP, I3)
END
SUBROUTINE LAMSTR

S/R LAMSTR
CALCULATES THE LAMINATE STRESSES AND STRAINS DUE TO AN INPLANE LOAD =
AND A BOLT LOAD

COMMON / TWO/ ICUT (15), NUMELY, NUMBAT, ANG (8), 2LYTHK (8), MATID (8)
COMMON / TREZ/ IANG, ILOW, IHIGH, STPINK, NUMBIP
COMMON / FOURY PAYPY, P. PW, AIFHA, BETA, DIA, CORREC
COMMON / SIV/ AI (3,3)
COMMON / 
С
                                                         PX=CORREC+PX
PI=CORREC+PY
PXI=CORREC+PXY
P=CORREC+P
PW=CORREC+PW
  C
                                                         10
                              CALCULATE UNLOAD HOLE STRESSES
```

```
IF (PX.EC.0.0) GO TO 30

BETA 0=BETA
CALL UNLOAD (PX.CIA, AI, BETAO, STRESS, U, V)

CONTINUE
IF (PY.EC.0.0) GO TO 50

BETA 90 0 CALL UNLOAD (PY.DIA, AI, BETA 90, STR.UX, VY)

DO 40 J=1, NUMSIP
U(J, K) = U(J, K) + UX(J, K)
V(J, K) = V(J, K) + VY(J, K)

DO 40 I=1, 3

STRESS (I, J, K) = STRESS (I, J, K) + STR(I, J, K)

CONTINUE
30
40
50
                           CONTINUE

IF (PXY. EQ. 0.0) GO TO 80

BETT45=BETA+45.0

CALL UNLCAD (PXY. CIA, AI, BETA45, STR. UX, VY)

DO 60 J=1, NUMSIP

DO 60 K=1, NUMPT

V (J, K) = V (J, K) + ÜX (J, K)

V (J, K) = V (J, K) + VY (J, K)

DO 60 I=13

STRESS (I, J, K) + STR (I, J, K)

CONTINUE
                            BETA45=BETA-45.0

RYH=-DYY
CALL UNICAD (PYYN, DIA, AI, BETA45, STR, UX, 7Y)
DO 70 J=1, KUMSTP
DO 70 K=1, NUMSTP
U(J,K)=U(J,K)+UX(J,K)
V(J,K)=V(J,K)+VY(J,K)
DO 70 I= (3)
SIRESS(I,J,K)+STR(I,J,K)
CONTINUE
CONTINUE
               CALCULATE LOADED HOLE STRESSES
                            IF (P. 20.3.0) GO TO 110
ALPHAO = ALPHA
PB=P
CALL LOAR (PB,CIA,S,ALPHAO,STR,UX,VY)
DO 90 J=1,NUMSIP
U(J,K) = U(J,K) + UX(J,K)
V(J,K) = V(J,K) + VY(J,K)
DO 90 I=1,5K) + VY(J,K)
STRESS (I,J,K) = STRESS (I,J,K) + STR(I,J,K)
LONG OF LEFA
                              ALPHAO=ALPHA
CALL UNICAD (PW, DIA, AI, ALPHAO, STR, UX, VY)
DO 100 J=1,NUNSTP
DO 100 K=1,NUNSTP
U(J,K) = U(J,K) + UX(J,K)
V(J,K) = V(J,K) + VY(J,K)
DO 100 T=1,3
STRESS (I,J,K) = STRESS (I,J,K) + STR(I,J,K)
CONTINUE
CONTINUE
CONTINUE
LF (PUTOUT(IOUT,3), EQ.2.) WRITE (2,210)
                               IF (PUTOUT(IOUT, 3). EQ.2.) WRITE (2,210)
   C CALCULATE PRINCIPAL STRESSES
                           IF (?UTOUI(IOUT.3).ME.2.) GO TC 130
DC 120 JJ=1,NUESTP
DC 120 JM=1,NUESTP
DC 120 M=1,NUESTP
PRIMA=(STRESS(1,JJ,NN)-STRESS(2,JJ,NN))*(STRESS(1,JJ,NN)-STRESS(2,JJ,NN))*(STRESS(1,JJ,NN)-STRESS(2,JJ,NN))/0.0
PRIMA=(STRESS(1,JJ,NN)+STRESS(3,JJ,NN))/2.0+PRIMA
PRIM1=(STRESS(1,JJ,NN)+STRESS(2,JJ,NN))/2.0+PRIMA
PRIM2=(STRESS(1,JJ,NN)+STRESS(2,JJ,NN))/2.0-PRIMA
```

```
TSIS=SIRESS(1,JJ,NN)-STRESS(2,JJ,NN)
DIECT=0.0
IF (TSIS_NE.0.0) DIRCT=0.5*ATAN(2.0*STRESS(3,JJ,NN)/TSIS)
DIRCT=180.0*DIRCT/3.1415926535
c
                                                   IP (PUTOUT(IOUT, 3).NE.2.0) GO TO 130

ANGLE=(NN-1)*IANG+ILCW

DIST=(JJ-1)*STPINK
IP (DIST.LE.3.0005) DIST=0.001
WRITE (2,220) DIST, ANGLE, STRESS(1,JJ,NN), STRESS(2,JJ,NN), STRESS(3,JJ,NN), PRIN1, PRIN2, DIRCT
                                                  JJ, NN), PRINI, PRINI, DIRCT
CONTINUE
CONTINUE
IF (PUTOUI(IOUI, 4). EQ. 2.) WRITE (2, 230)
                      CALCULATE LAMINATE STRAINS
                                                  DO 140 JJ=1,NUESTF
DO 140 NN=1,NUMPT
DO 140 KK=1,3
DC 140 ME=1,3
STRAIN (KK,JJ,NN)=AI (KK,MM)*STRESS (MM,JJ,NN)*STRAIN (KK,JJ,NN)
CONTINUE
             CALCULATE PRINCIFAL STRAINS

IF (PUTOUT(IOUT, 4).NE.2.0) GO TO 160

DO 150 JJ=1,NUMSTF
DO 150 NN=1,NUMSTF
PRINA= (SIRAIN (1,JJ,NN)-STRAIN (2,JJ,NN)) * (STRAIN (1,JJ,NN)-STRAIN (2,JJ,NN)) / (2,N) / (
                             CALCULATE CIRCUMFERENTIAL AND RADIAL STRESSES & STRAINS
                                              LCULATE CIRCUMFERENTIAL AND RADIAL STRESSES & STRAINS

IF (PUTOUT(IOUT,5).EQ.2.) WRITE (2,250)

IP (PUTOUT(IOUT,5).NE.2.) GO TC (80

DO 170 J=1,NUMSTP
DO 170 N=1,NUMSTP
ENERGY=.5*(STRESS (1,J,N)*STRAIN(1,J,N)*STRESS(2,J,N)*STRAIN(2,J,N)

1*STRESS(3,J,N)*STRAIN(3,J,N)

ANGLE=(N-1)*IANG+ILOW
D=ANGLE=PI/180.0
DIST=(J-1)*STPINK
IP (DIST.LE.0.0005) DIST=0.001
RADSTS=STRESS(1,J,N)*SIN(D)*COS(D)*CCS(D)+STRESS(2,J,N)*SIN(D)*SIN(D)+2.*

1STRESS(3,J,N)*SIN(D)*COS(D)
CIRSTS=STRESS(1,J,N)*SIN(D)*SIN(D)*STRESS(2,J,N)*COS(D)*COS(D)-2.*

1STRESS(3,J,N)*SIN(D)*COS(D)
SHRSTS=-1.*STRESS(1,J,N)*SIN(D)*COS(D)+STRESS(2,J,N)*SIN(D)*COS(D)

1*STRESS(3,J,N)*(CCS(D)*COS(D)-SIN(D)*STR(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*COS(D)

SHRSTN=-1.*STRAIN(1,J,N)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*COS(D)

SHRSTN=-1.*STRAIN(1,J,N)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*SIN(D)*COS(D)

HEITE (2,260) CIST,ANGLE,CIRSIS,RADSTS,SHRSTS,CIRSTN,RADSTN,SHRSTN
CONTINUE
                            WHITE THE OUTPUT DISPLACEMENTS
```

```
D3=3.0*DIA
DISP=DIA/2.0+NUMSIP*STPINK
IF (PUTOUI(IOUI,6).2Q.2.0.AND.F.NE.0.0.AND.DISP.GT.D3) WRITE (2,27
                                    C
190
200
C--
                             RETURN
PORMAT (//.29 (1H-), 21H LAMINATE STRESSES ,29 (1H-) //.8HDISTANCE
PORMAT (//.29 (1H-), 21H LAMINATE STRESSES ,29 (1H-) //.8HDISTANCE
21NUM, 2X, 9HDIRECTICN, /.49 X, 5HSIG-Y, 5X, 6HSIG-Y, 5X, 7 HM XXIMUM, 4X, 7 HMIN
21NUM, 2X, 9HDIRECTICN, /.49 X, 20 HPRINCIPAL PRINCIPAL, /)
FORMAT (//.29 (1H-), 20H LAMINATE STRAINS ,30 (1H-), //.8HDISTANCE, 2
1X, 5HANGLE, 4X, 5 HEPS-X, 6X, 5 HEPS-Y, 5X, 6 HEPS-XY, 4X, 7 HMINI
1X, 5HANGLE, 4X, 5 HEPS-X, 6X, 5 HEPS-Y, 5X, 6 HEPS-XY, 4X, 7 HMINI
PORMAT (F7.3, F8.2, F10.6, 4F11.6, F7.1)
FORMAT (F7.3, F8.2, F10.6, 4F11.6, F7.1)
FORMAT (//.56 (1H-), 49H CIRCUMEREBNTIAL AND RADIAL STRESSES & STRAINS ,15 (1H-), //.8HDISTANCE, 2X, 5 HS HEAR, /.18X, 6 HS TRESS / 5X, 5 HT HETA, 5X, 6 HEADIAL, 5X, 5 HS HEAR, /.18X, 6 HS TRESS / 5X, 6 HS TRESS / 5X, 6 HS TRESS / 4X, 6 HS TRAIN, 4X, 6 HS TRAIN, ///
FORMAT (F7.3, F10.3, F10.1)
FORMAT (F7.3, F10.1)
FORMAT (//.13 (1H-), 16H DISPIACEMENT ,13 (1H-), //.8HDISTANCE, 4X, 5 HANGLE, 3X, 5 HS HEAR, /.18X, 6 HS TRAIN, ///
FORMAT (//.13 (1H-), 16H DISPIACEMENT ,13 (1H-), //.8HDISTANCE, 4X, 5 HANGLE, 3X, F10.2, F13.6, F12.6)
END
210
 220
230
  260
276
 280
 290
                                     END
SUBROUTINE UNLOAD (P,DIA, AI, BETA, STRESS,U, Y)
                  S/R UNLOAD

VER 1.1 4/25/83 PDS AERO ENGINEERING
CALCULATE STEESS DISTRIBUTION ARCUND AN UNLOADED HOLE

COMMON / THREE/ IANG, ILO4, IHIGH, STPINK, NUMSTP
INTEGER IANG, ILO4, IHIGH, STPINK, NUMSTP
DIMENSION STRESS (3, 20, 91), U (20, 91), AI (3, 3)
DIMENSION WORK (5), COEF(5), ETE (4), RTI (4)
COMPLEX R1, R2, COMPLIXIT, AI (2, CCM1, COM2, DEN1, DEN2, PHI1, PHI2
COMPLEX Z, Z, Z, Z, Z, P4, Z, Z, Z, Z, DATA NUMPI/1/, PI/3. 14 15 92 65 35/
                   CALCULATE COMPLEX PARAMETERS, INITIALIZE COMPLEX NUMBER: SQRT (-1.0)
                                   COMPLX = (0.0,1.0)
NUMCC=4
COEF (1) = AI (2.2) * 1000000.0
COEF (2) = -2.0 * AI (2.3) * 1000000.0
COEF (3) = (2.0 * AI (1.2) + AI (3.3)) * 1000000.0
COEF (3) = (2.0 * AI (1.3) * 1000000.0
COEF (5) = AI (1.1) * 10000000.0
COEF (5) = AI (1.1) * 100000000.0
COMPLX * ETI (3) * COMPLX * ETI (3)
IF (BTI (4).GT.0.0) R !=RTR (2) + CCMPLX * ETI (2)
IF (BTI (4).GT.0.0) R !=RTR (4) + CCMPLX * ETI (4)
P1 = AI (1.1) * RI * RI * AI (1.2) - AI (1.3) * RI
P2 = AI (1.1) * RI * RI * AI (1.2) - AI (1.3) * RI
CO = AI (1.2) * RI * AI (2.2) / RI - AI (2.3)
BETA = BETA * PET / 180.0
IF (1AMG.2C.3) GO TO 10
NUMPT = ((1BIGH - ILC.) / IAMG) * 1
                                      COMPLX = (0.0, 1.0)
 10
                                     DO 30 JJ=1, NUMSTP
DO 20 NM=1, NUMPT
U(JJ, NM) =0.0
V(JJ, NM) =0.0
```

```
NNM=NN-1

JJJ=JJ-1

THETA= (NNN*IANG+ILOW) *PI/180.0

RADIUS=JJJ=STFINK+DIA/2.0
CALCULATE X & Y CCORDINATES OF POINTS A BOUND UNLOADED HOLE
            X=RADIUS*COS (THETA)
Y=RADIUS*SIN (THETA)
  CALCULATE LOCATION PARAMETERS FOR UNLOADED HOLE EQUATIONS
            Z 1=X+R 1+Y
Z2=X+R 2+Y
Z=X+CO MPLX+Y
  COMPLEX MAPPING FUNCTION
            XI1=CSQRT(Z1*Z1-CIA*CIA/4.0-R1*R1*DIA*DIA/4.0)
XI2=CSQRT(Z2*Z2-DIA*CIA/4.0-R2*R2*DIA*DIA/4.0)
    CHOCSE THE BOOT WITH THE CORRECT SIGN
            XI1=Z1/XI1

XI2=Z2/XI2

IF (REAL(XI1) .LT.-0.00001) XI1=-1.0*XI1

IF (REAL(XI2) .IT.-0.00001) XI2=-1.0*XI2

XI1=1.0-XI1

XI2=1.0-XI2
   CALCULATE PHI PRIME
          COM1=R2*SIN(2.0*BETA)+2.0*COS(BETA)*COS(BETA)+COMPLX*(2.0*R2*SIN(B1ETA)*SIN(BETA)+SIN(2.0*BETA))
COM2=R1*SIN(2.0*BETA)+2.0*COS(BETA)*COS(BETA)+COMPLX*(2.0*R1*SIN(B1ETA)*SIN(BETA)+SIN(2.0*BETA))
            DEN1=2.0*DIA* (R1-32)*(1.0*COMFIX*R1)
DEN2=2.0*DIA* (R1-32)*(1.0*COMFIX*R2)
PHI1=-COMFLX*P*DIA*CCM1*X11/(2.0*DEN 1)
PHI2=COMFLX*P*DIA*COM2*X12/(2.0*DZN2)
        CALCULATE STRESSES AROUND HOLE
          STRESS (1, JJ, NN) =P*CCS (BETA) *CCS (BETA) +2.0*REAL (R1*R1*PHI1+R2*R2*PH 112)

STRESS (2, JJ, NN) =P*SIN (BETA) *SIN (BETA) +2.0*REAL (PHI1+PHI2)

STRESS (3, JJ, NN) =P*SIN (BETA) *CCS (BETA) -2.0*REAL (R1*PHI1+R2*PHI2)
    CALCULATE DISPLACEMENTS
            XI1=1.0-XI1

XI2=1.0-XI2

XI1=21.XI1

XI2=Z2/XI2

DEN1=16.0*(R1-R2)*(Z1*XI1)

DEN2=16.0*(R1-R2)*(Z1*XI1)

DEN2=16.0*(R1-R2)*(Z1*XI12)

PHI1=-P*DIA*DIA*(CCMPIX*R1)*CCM1/DEN1

PHI2=P*DIA*DIA*(CCMPIX*R2)*COM2/DEN2

0 (JJ,NN)=2.0*REAL(P1*PHI1+P2*PHI2)

CONTINUE

CONTINUE
             CONTÎN DE
    CONTINUE

RETURN

INC
SUBROUTINE LOAD (F,DIA,S,ALPHA,STRESS,U,V)

S/R LOAD

VER 1.1

4/25/83

PDS
AERO ENGINEERING =
CALCULATES STRESS CISTRIBUTION AFOUND A LOADED HOLE ASSURING A =
COSINE BOLT LOAD DISTRIBUTION

COMMON / INO/ ICUT (15), NUMPLY, NUMBAT, ANG (8), PLYTHK (8), NATID (8)
COMMON / THREE/ IANG, LOW, IHIGH, STPINK, NUMSTP
INTEGER IANG, ILOW, IHIGH
COMPLEX B1, R2, COMFLX, Z, Z1, Z2, CPOS (50), CNEG (50), CZERO, CM, AK1, AK2, XI
```

```
11,X12,PHI1,PHI2,CCM1,COM2,XXI1,XXI2

COMPLEX CHECK1,CHECK2,P1,P2,Q1,Q2

CCMPLEX A1(50),A2(50)

DIMENSION ANATEX(4,4),BMATRX(4),STRESS(3,20,91)

DIMENSION U(20,91),V(20,91),S(3,3)

DIMENSION WORK(5),COEP(5),RTR(4),RTI(4)

DATA NUMPT/1/,FI/5.1415926535/
                             INITIALIZE COMPLEX NUMBER: 5QRT (-1.0)
                                                            COMPLX = (0.0, 1.0)
                           CALCULATE COMPLEX PARAMETERS
                        CALCULATE COMPLEX PARAMETERS

NUMCO=4

COEF (1) = S(2, 2) *1000000.0

COEF (3) = -2.0*S(2, 3) *1000000.0

COEF (3) = -2.0*S(1, 2) *5 (1, 3) *1000000.0

COEF (3) = S(1, 1) *1000000.0

CALL ACOTS (COEF, WORK, WOMCO, RTE, RTI, IE)

R1=RTR(1) + COMPLEX RTI(1)

IF (RTI(2).GT.0.0) R1=RTR(2) + COMPLEX RTI(2)

R2=RTR(3) + COMPLEX RTI(3)

IF (RTI(4).GT.0.0) R2=RTR(4) + CCMPLEX RTI(4)

P1=S(1, 1) *R1*R1+S(1, 2) - S(1, 3) *R1

P2=S(1, 1) *R1*R1+S(1, 2) - S(1, 3) *R2

C1=S(1, 2) *R1+S(2, 2) / R1-S(2, 3)

C2=S(1, 2) *R2+S(2, 2) / R2-S(2, 3)

THICK = THICK+9LTHK(N)

CONTINUE

P=4.0*P/PI

A COSIYE SHAFED LOAD DISTRIBUTION OVER HALF CF HOLE AT AN ANGLE

ALPHA TO X AXIS. CALCULATE THE COMPLEX CONSTANTS
10
                                                         COSIVE SHAPED LOAD DISTRIBUTION OVER HALF CF HOLE AT PHA TO X AXIS. CALCULATE THE COMPLEX CONSTANTS

F12=P1/2.0

M=-1

CONTINUE

H=++1

IF (H. EQ.-1) GO TO 40

CONTINUE

C2=SIN (H-1) *P12) / (2*(H-1))

C3=SIN (H+1) * (-P12) / (2*(H-1))

C4=SIN ((H+1) * (-P12) / (2*(H+1))

C5=COS (H+1) *P12) / (2*(H+1))

C5=COS (H+1) *P12) / (2*(H+1))

C8=COS (H+1) *P12) / (2*(H+1))

C8=COS (H+1) * (-P12) / (2*(H+1))

C8=COS (H+1) * (-P12) / (2*(H+1))

CM=P* (C1+C2-C3-C4) - CONPLX*(-C5-C6+C7+C8)) / (2.0*P1)

IF (H. GT. 1) CPOS (H) = CM

IF (M. LT.-1) ENEG (MN) = CM

IF (M. LT.-1) GO TO 50

C5=SIN (-P12) *SIN (-P12) / 2.0

C5=SIN (-P12) *SIN (-P12) *SIN (-P12
20
30
50
                                                                    M=IABS(M)
IF (M. LT. 49) GO TO 20
```

```
SERIES TRUNCATED AFTPR 25 TERMS.
TEAMSFORM COMPLEX PARAMETERS INTO REAL AND IMAGINARY PARTS.

S1=REAL (R1)
S2=REAL (R2)
T1=AIM AG (R1)
T2=AIM AG (R2)
                                                                                              UATE COEFFICIENTS AND SOLVE FOR CONSTANTS

DO 80 M=1,45

MN=M-1

IF (MN.NE.O) GO TC 60

EMATRX (1) = REAL (-CZERO*DIA/2.0)

BMATRX (2) = AIMAG (-CZERO*DIA/2.0)

GO TO 70

CONTINUE

BMATRX (2) = AIMAG (-CPOS (MN) *DIA/ (2.0* (MN+1)))

EMATRX (2) = AIMAG (-CPOS (MN) *DIA/ (2.0* (MN+1)))

EMATRX (2) = AIMAG (-CNEG (MN) *DIA/ (2.0* (MNEG+1)))

BMATRX (3) = REAL (-CNEG (MN) *DIA/ (2.0* (MNEG+1)))

BMATRX (4) = AIMAG (-CNEG (MN) *DIA/ (2.0* (MNEG+1)))

BMATRX (1, 1) = T1+1.0

AMATRX (1, 2) = S1

AMATRX (1, 3) = T2+1.0

AMATRX (2, 3) = T2-1.0

AMATRX (2, 3) = T2-1.0

AMATRX (2, 4) = -T1-1.0

AMATRX (3, 4) = -S2

AMATRX (3, 4) = -S2

AMATRX (3, 4) = -S2

AMATRX (4, 4) = S1

AMATRX (4, 4) = S1

AMATRX (4, 4) = S2

AMATRX (4, 4) = S1

AMATRX (4, 4) = S1

AMATRX (4, 4) = S2

AMATRX (4, 4) = S2

AMATRX (4, 4) = S1

AMATRX (4, 4) = S1

AMATRX (4, 4) = S2

AMATRX (5, 4) = S2

AMATRX (6, 4) = S2

AMATRX (6, 4) = S2

AMATRX (7, 
E EQUATE COEFFICIENTS AND SOLVE FOR CONSTANTS
     60
     70
     80
C
                                                                                                                 PX=2.0*PI*AIMAG(CCMPIX*DIA*CNEG(1)/2.0)
PY=2.0*PI*RBAL(COMPLX*DIA*CNEG(1)/2.0)
                                                                                                            PY=2.0*PI*REAL (COMPLI*DIA*CNEG(1)/2.0)

AMATRX (1,1) = T1
AMATRX (1,2) = S1
AMATRX (1,3) = T2
AMATRX (1,4) = S2
AMATRX (2,1) = S0
AMATRX (2,1) = 1.0
AMATRX (2,2) = 1.0
AMATRX (2,1) = 1.0
AMATRX (3,1) = 2.0*S1*T1
AMATRX (4,1) = S1/S1*S1*T1*T1)
AMATRX (4,2) = S1/S1*S1*T1*T1)
AMATRX (4,2) = S1/S1*S1*T1*T1)
AMATRX (4,2) = S1/S1*S1*T1*T1)
AMATRX (4,2) = S1/S1*S1*T1*T1)
BMATRX (1,2) = S1/S1*S1*T1*T1)
BMATRX (1,3) = S1/S1*S1*T1*T1)
BMATRX (1,3) = S1/S1*S1*T1*T1
BMATRX (1,2) = S1/S1*S1*T1*T1
BMATRX (1,3) = S1/S1*S1*T1*T1*T1
BMATRX (1,3) = S1/S1*S1*T1*T1*T1*T1
BMATRX (1,3) = S1/S1*S1*T1*T1*T1
BMATRX (1,3) = S1/S1*S1*T
     С
```

```
CONTINUE
ALPHA=ALPHA+PI/180.0
ALPH=ALFHA
DO 160 JJ=1, YUMSTF
DO 150 Nn=1, NUMPT
U(JJ, NN) = 0.0
V(JJ, NN) = 0.0
V(JJ, NN) = 0.0
NNN=NN-1
JJJ=JJ-1
THETA=(NNN+IANG+ILOW)*PI/180.0
RADIUS=JJJ*STFINK+DIA/2.0

CALCULATE X AND Y COORDINATES OF FOINTS ARCUND LOADED HOLE
90
                    X=RADIUS*COS (THETA+ALPHA)
Y=RADIUS*SIN (THETA+ALPHA)
      CALCULATE PARAMETERS FOR LOADED HOLE EQUATIONS
                    Z 1=X+R 1*Y
Z 2=X+R 2*Y
Z=X+CO MPLX*Y
                    MAPPING FUNCTION
                    XXI1=CSQRT(Z1*Z1-EIA*DIA/4.0-R1*R1*D1
XXI2=CSQRI(Z2*Z2-DIA*DIA/4.0-B2*R2*DI
         CHOCSE THE CCRRECT SIGN OF CSQRT
                    CONTINUE
XI1=Z1+XXI1
XI2=Z2+XXI2
                    X12=Z2+XX12

X11=2.0*X11/(DIA*(1.0-COMPLX*E1))

X12=2.0*X12/(EIA*(1.0-COMPLX*E2))

COX1=REAL(XI1) *REAL(XI1) + AIMAG(XI1) * AIMAG(XI1)

COX2=REAL(XI2) *REAL(XI2) + AIMAG(XI2) * AIMAG(XI2)

If (COX1.GE.0.99999) GO TO 110

XXI1=-XXI1

GO TO 100

CONTINUE

IF (COX2.GE.0.99999) GO TO 120

XXI2=-XXI2

XXI2=XI2

XXI2=XI2

XXI2=XI2

XXI2=XI2
 120
 C CALCULATE PHI PRIME
                    COM1=(0.0,0.0)

COM2=(0.0,0.0)

DO 130 M=1,45

COM1=COM1+M*A1(H) *XI1**(-1*H)

COM2=COM2+H*A2(H) *XI2**(-1*H)

CONTINUE
                     CHECK SIGN OF CSORT
                     XI1=CS ORT (Z1*Z1-EIA*CIA/4.0-DIA*DIA*R1*R1/4.0)
XI2=CS ORT (Z2*Z2-DIA*DIA/4.0-DIA*DIA*R2*R2/4.0)
CHECK1=Z1/XI1
CHECK2=Z2/XI2
IF (RE AL (CHECK1).II.-0.00001) XI1=-1.0*XI1
IF (RE AL (CHECK2).IT.-0.00001) XI2=-1.0*XI2
PHI1=(AK1-COM1)/XI1
PHI2=(AK2-COM2)/XI2
 C CALCULATE SIRESS CCMPONENTS IN LAMINATE AT COORDINATES X,Y
                     STRX=2.0 *REAL (R1*F1*FHI 1+ B2*R2*PHI2)
STRY=2.0 *REAL (PHI 1+PHI2)
STRXY=-2.0 *REAL (R 1*PHI 1+ R2*PHI2)
STRXY=-2.0 *REAL (R 1*PHI 1+ R2*PHI2)
STRESS (1, JJ, NN) = STRX*COS (ALPH) *COS (ALPH) + STRY*SIN (ALPH) *SIN (ALPH) -
2.0 *STRXY*SIN (ALPH) *COS (ALPH) *SIN (ALPH) + STRY*COS (ALPH) *COS (ALPH) +
STRESS (2, JJ, NN) = STRX*SIN (ALPH) *SIN (ALPH) + STRY*COS (ALPH) *COS (ALPH) +
```

```
12.0*STR XY*SIN (ALPH) *COS (ALPH)
STRESS (3.JJ. NN) = STRX*SIN (ALPH) *COS (ALPH) - STRY*SIN (ALPH) *COS (ALPH) +
1STRXY* (CCS (ALPH) *COS (ALPH) - SIN (ALPH) *SIN (ALPH))
                            CALCULATE DISPLACEMENTS
                                                       XI = XX I 1
XI = XX I 1
XI = XX I 2
COM 1 = (0.0,0,0)
COM 2 = (0.0,0,0)
D0 140 M = 1,45
COM 1 = COM 1 + A 1 (M) * X I 1 * * (-1 * M)
COM 2 = COM 2 + A 2 (M) * X I 2 * * (-1 * M)
COM I = COM I + A 1 (M) * X I 2 * * (-1 * M)
COM I = COM I + A 1 (M) * X I 2 * * (-1 * M)
COM I = COM I + A 1 (M) * X I 2 * * (-1 * M)
COM I I U E
XXI 1 = CLOG (XI 1)
XXI 2 = CLOG (XI 2)
PH I = A K 2 * XXI 2 + COM 1
PH I 2 = A K 2 * XXI 2 + COM 1
PH I 2 = A K 2 * XXI 2 + COM 1
U (JJ, N) = 2 0 * R F A L (Q 1 * P H I 1 + Q 2 * F H I 2)
COM I N U E
CONTINUE
CONTINUE
   140
150
160
C--
                                                            RETURN
PORMAT (41H SIMULI CALCULATES A SINGULAR SET OF EQS.)
PCHAIT (41H SIMULT CALCULATES A SINGULAR SET OF EQS.)
                                                         SUBROUTINE PLYSTR (IFAIL)

TRANSFORMS LAMINATE STRAINS TO PLY STRESSES/STRAINS BY ASSU
CONSTANT STRAIN "EROUGH THE THICKNESS

COMMON / COME/ F1(3), F2(3), G12(3), V12(3),
COMMON / TRO/ IOUT (15), NUMELY, NUMBAY, ANG (8), PLYTHK (8), MATID (8),
COMMON / TREEL / IANG, ILOW, IHIGH, STPINK, NUMSTP,
COMMON / TERFEL / IANG, ILOW, IHIGH, STPINK, NUMSTP,
COMMON / TERFEL / IANG, ILOW, THIGH, STPINK, NUMSTP,
COMMON / NINE/ STRISS (3, 20, 91), STRAIN (3, 20, 91),
INTEGER IANG, ILOW, IHIGH,
DATA NUMFT/1/, PI/S. 1415926535/
                               CALCULATE THE STRAINS
                                                         LCULATE THE STRAINS

MOVE=0

IF (IANG.EO.O) GO TO 10

NUMPT= ((IHIGH-ILOW)/IANG)+1

CONTINUE

IF (PUTOUT(IOUT,7).EQ.2.) WRITE (2,60)

CONTINUE

DO 30 UN=1,NUMSTP

DO 30 UN=1,NUMSTP

DO 30 UN=1,NUMPTT

D=ANG(L)*PI/180.0,NN)

STRANY=STRAIN(1,JJ,NN)

STRANY=STRAIN(1,JJ,NN)

STRANY=STRAIN(3,JJ,NN)

STRANY=STRAIN(3,JJ,NN)

STRANY=STRAIN(3,JJ,NN)

STRANY=STRAIN(3,JJ,NN)

STRANY=STRAIN(3,JJ,NN)

STRANY=STRAIN(3,JJ,NN)

STRANY=STRANY*SIN(D)*SIN(D)

STRAIN(1,JJ,NN)=STRAIN+STRAN2+GAMA12

STRAIN(2,STRANY*SIN(D)*SIN(D)

GAMA12=-1.0*GAMA*SIN(D)*COS(D)

STRAIN(2,STRAINY*SIN(D)*COS(D)

STRAIN(2,JJ,NN)=STRAIN*SIN(D)*COS(D)

STRAIN(2,JJ,NN)=STRAIN*S
   10
   20
   C
   30
```

```
IF (PUTOUT(TOUT, 8). EQ. 2.0) FRITE (2, 80)

DO 40 JJ=1, NUMSTP

DO 40 NN=1, NUMPT

DO 40 L=1, NUMPT

DO 40 L=1, NUMPT

DO 40 L=1, NUMPT

DO 40 L=1, NUMPT

DE N=1.0-V12(H)*V21(H)

DEN=1.0-V12(H)*V21

ABC=STR2(L,JJ,NN)/DEN

BCA=STR1(L,JJ,NN) / DEN

BCA=STR1(L,JJ,NN) = 12(H)*STR1(L,JJ,NN)/DEN+V12(H)*E2(H)*ABC

STR1(L,JJ,NN) = 12(H)*E2(H)*BCA/DEN+E2(H)*ABC

STR1(L,JJ,NN) = STR12(L,JJ,NN) *G12(H)

DIST=(JJ-1)*STP1NK

DIST=(JJ-1)*STP1NK

IF (DIST.L2.0.0005) DIST=0.001

IF (PUTOUT(IOUT, 8). EQ. 2.0) WRITE (2, 90) DIST, ANGLE, ANG(L), STR1(L,J)

JJ,NN), STR2(L,JJ,NN), STR12(L,JJ,NN)

CONTINUE

MOVE=1

IF (IFAIL.EQ.1) GO TO 20

CONTINUE

RETURN
                                  CALCULATE THE STRESS IN EACH PLY
C
40
                           RETURN

POEMAT (///, 20(1H-), 19H PLY-BY-PLY STRAIN, 20(1H-), //, 8HDISTANCE, 2

1x, 5HANGLE, 4x, 3HPLY, 7x, 5HEPS-1, 7x, 5HEPS-2, 6x, 6HEPS-12, //)

PCEMAT (F. 3, F8. 2, F8. 1, 3F12-6;

PCEMAT (//, 20(1H-), 19H PLY-BY-PLY STRESS, 20(1H-), //, 2x, 4HDIST, 4x

1, 5HANGLE, 4x, 3HFLY, 7x, 5HSIG-1, 7x, 5HSIG-2, 6x, 6HSIG-12, //)

FORMAT (FT. 3, F8. 2, F8. 1, 3F12-1)

END

SUBGOUTINE FAIL

FCINT STRESS/STRAIN ANALYSIS POR FAILURE USING UNIDIRECTION =

dATERIAL ALLOWABLES

COMMON /TWO/ LOUT(15), NUMELY, SUMMAT, ANG (8), PLYTHK (8), MATID (8)

COMMON /TWO/ LOUT(15), NUMELY, SUMMAT, ANG (8), PLYTHK (8), MATID (8)

COMMON /TWO/ LOUT(15), NUMELY, SUMMAT, ANG (8), PLYTHK (8), MATID (8)

COMMON /TWO/ PXPI, PXPI
 50
60
70
80
 90
   10
                                                                      P3=0.0
NUMPT=1
IF (IANG.EQ.0) GO TO 30
NUMPT=((IHIGH-ILOW)/IANG)+1
CONTINUE
DO 140 JJ=1,NUMSTP
DO 140 KK=1,NUMPT
SIG=10
DO 130 II=1,NUMPLY
X=STR1 (II,JJ,KK)
XI=STR1 (II,JJ,KK)
HATII=MATID(II)
GO TO (40,40,50,60,70), IPAIL
   30
                                       MAXINUM STRESS/STRAIN CRITERIA
                                                                                                                                                                                                                                 FR=FRC (MATII)
```

```
IF (Y.LT.O.O) FY=FYC (MATIC)
F1=1/PX
F2=Y/PY
F3=XY/FXY (MATII)
GO TO 80
                                               TSAI-HILL CRITERIA
                                              CONTINUE

FX=FXT (MATII)

IF (X.LT.0.0)

FX=FXC (MATII)

FY=FYT (MATII)

IF (Y.LT.0.0)

FY=FYT (MATII)

F1=X*X/(FX*FX)+Y*Y/(FY*FY)-X*Y/(FX*FX)+XY*XY/(FXY (MATII)*FXY (MATII)
                                              | Total (X/FI) /SORT(F1) | RTOY=(Y/FI) /SORT(F1) | RTOY=(Y/FI) /SORT(F1) | RTOY=(XI/FI) (MATII) ) /SORT(F1) | GO TO 80 | CETTERIA
                        MODIFIED TSAI-WU CRITERIA
                                            CONTINUE

P1=1.0/FXT(MATII) -1.0/PXC(MATII)

F2=1.0/FXT(MATII) -1.0/PYC(MATII)

F11=1.0/FXT(MATII) +1.0/FYC(MATII)

F11=1.0/FYT(MATII) *FXC(MATII)

F66=1.0/FYT(MATII) *FXY(MATII)

F66=1.0/FYT(MATII) *FXY(MATII)

F1=P**X+F2*Y+F11*X*X+F22*Y*Y+F66*XY*XY

FX=FXT(MATII)

IF (X.LT.O.G) FX=FXC(MATII)

FY=FYT(MATII)

IF (Y.LT.O.G) FX=FXC(MATII)

FY=FYT(MATII)

IF (Y.LT.O.G) FX=FXC(MATII)

FY=FYT(MATII)

IF (Y.LT.O.G) FX=FXC(MATII)

F1=ABS(F1)

RTCX=(X/FX)/SCRT(F1)

RTCX=(X/FX)/SCRT(F1)

RTCX=(X/FX)/SCRT(F1)

RTCX=(X/FX)/SCRT(F1)

RTCX=(X/FX)/SCRT(F1)

RTCX=(X/FX)/SCRT(F1)

RTCX=(X/FX)/SCRT(F1)

RTCX=(X/FX)/SCRT(F1)

RTCX=(X/FX)/SCRT(F1)
                                                 HOFPMAN FAILURE CRITERIA
                                    HOFPMAN FAILURE CRITERIA

CONTINUE

71=1.J/FXT(MATII) -1.0/FXC(MATII)

F2=1.0/FYT(MATII) *FXC(MATII)

F11=1.0/FXT(MATII) *FXC(MATII)

F2=1.0/FYT(MATII) *FXC(MATII)

F10=1.0/FXT(MATII) *FXC(MATII)

F10=1.0/FXT(MATII) *FXC(MATII)

F10=1.0/FXT(MATII) *FXC(MATII)

F10=1.0/FXT(MATII)

F10=1
80
C
                                        GO TO 100 CONTINUE (2,230) DIST, ANGLE, ANG (II), F1,F2,F GO TO 100 CONTINUE IF (2,240) DIST, ANGLE, ANG (II), F1,RTOX 1, RTOY, RTCXY CONTINUE
90
100
C--
                        AUTOMATIC STARCH FOR FAILURE
```

```
IF (SIG.EQ.2.) RTC(1,II) = RTOY
IF (SIG.EQ.2.) RTC(2,II) = RTOY
IF (SIG.EQ.2.) RTC(3,II) = RTOY
IF (JJ.NE.1) = RTOY
IF (JJ.NE.1) = RTOY
IF (JJ.NE.2) = RTOY
IF (ABS.(CHECK) .LT.ABS.(F1) CHECK=F1
IF (ABS.(CHECK) .LT.ABS.(F1) CHECK=F2
IF (ABS.(CHECK) .LT.ABS.(F3) CHECK=F3
IF (CHECK.EQ.CHK) GO TO 120
KKK=KK
III=II
DO 110 N=1,31
DO 110 N=1,31
DO 110 N=1,31
PAILS.(N,N)=PLYFAL(N,N)
RTC(N.M)=PLYRTC(N,M)
CONTINUE
CONTINUE
CONTINUE
CONTINUE
IF (CHECK.EQ.O.O) GO TO 190
                                                                                                           CONTINUE

IF (CHECK.20.0.0) GO TO 190

IF (IPAIL.E0.1) CCRREC=1.0/ABS(CHECK)

IF (IPAIL.E0.2) CORREC=1.0/SORT(CHECK)

IF (IPAIL.E0.3) CCRREC=1.0/SORT(CHECK)

IF (IPAIL.E0.4) CCRREC=1.0/SORT(CHECK)

IF (IPAIL.E0.4) CCRREC=1.0/SORT(CHECK)

WRITZ (2.200) CORREC

IF (PUTOUT(IOUT, 10).NE.2.) GO TO 180

IF (CORREC.IT..999.0F.CORREC.GT.1.001) GO TO 180

ANGLE=(KKK-1)*IANG+ILOW

IF (IFAIL.G1.2) GO TO 160

WRITZ (2.250) FX,FY,ZXY,P

DO 150 I=1,NUMPLY

WRITZ (2.250) STPINK,ANGLE,ANG(I),FAILS(1,I),FAILS(2,I),FAILS(3,I)

CONTINUE

GO TO 190

CONTINUE

170
180
190
   230
240
250
      280
```

```
SUPROUTINE SIMULT (A,B,N,KS)

TEST POR ALGORITHMIC SINGULARITY ADDED 01/10/79
MACHINE EPSILON PCR CYBER SINGIE PRECISION

DIMENSION A (1), P(1)
DATA 2PS/7.11E-15/

TOL=3.18*EPS*(N-1)
BETA=0.0
XS=0
JJ=N
DO 80 J=1,N
JY=J+1
JJ=J+N+1
BIGA=0.0
IT=JJ-J
DO 20 I=J,N
IJ=IT+I
PO 20 I=J,N
IJ=IT+I
PO 20 I=J,N
IJ=IT+I
PO 20 I=J,N
IJ=IT+I
PO 20 I=J,N
IJ=IT+I
CONTINUE
                                                                                                                                IJ=IT+I
IF (ABS(BIGA) - ABS(A(IJ))) 10,20,20

BIGA=A(IJ)
IMAX=I
CONTINUE
IF (ABS(BIGA) -GI.BETA) BETA=AES(BIGA)
IF (ABS(EIGA) -TOL*BETA)
IF (ABS(EIGA) -TOL*BETA)
IF (ABS(BIGA) -TOL*BETA)
IF (ABS(BIGA)
IF (ABS(BIGA) -TOL*BETA)
IF (ABS(BIGA)
IF (ABS(BIGA)
IF (ABS(BIGA) -TOL*BETA)
IF (ABS(BIGA)
IF (ABS(BIGA) -TOL*BETA)
IF (ABS(BIGA)
IF (ABS(BIGA)
IF (ABS(BIGA) -TOL*BETA)
IF (ABS(BIGA)
IF (ABS(BICA)
IF (ABS(BIGA)
IF (ABS(BICA)
IF (AB
10
   20
   30
      40
   50
   60
      100
```

Providence proposed from the season from the seasons seasons. Seasons in

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DIHEMSION XCOF (M), COF (M), POOTE (M), ROOTI (M)
REAL+8 XC, YO, Y, YFR, YFR, UX, UY, Y, TXT, U
RELATIVE MACHINE FRECISION (TIST FOR *ALMOST ZERO*)
DATA R MPREC/1.0D-14/, TOL/1.0D-4/
IFIT=0
N=M
IES=0
IF (XCOF (N+1)) 10,30,10
IER=1
GO TO 290
IER=2
GO TO 290
IER=2
GO TO 290
IF (N-36) 60,60,40
NX=N
NX=N+1
С
  10
20
    30
    40
                                                                                               GO TO 290
IF (N-36) 60,60,40
NX=N+1
NX=N+1
N2=1
KJ1=N+1
DO 79 L=1,KJ1
M1=KJ1-L+1
COF(XT)=XCOF(L)
XO=0.00500101D0
YO=0.01000101D0
IN=0
X=X0
X=X0
X=-10.0F0*Y0
YO=-10.0F0*Y0
Y=Y0
IN=IN+1
GO TO 110
IFIT=1
XFR=X
YPR=Y
ICT=0
UX=0.0D0
UY=0.0D0
UY=0.0D0
VT=0.0D0
VT=1.0D0
XT=1.0D0

    70
E0
    90
         100
       110
120
                                                                                                           V=V+TEMP+YTZ
PI=IIX+PI+X***TEMP
UX=UX-PI+X***TEMP
UX=UX-PI+X***TEMP
UX=UX-PI+X***TEMP
UX=UX-PI+X**TEMP
UX=Y**UX+UX+UY+UY
IF (SUMSQ.LE.RMPREC) GO TO 190
DX=(V**UY-U**UX)/SUMSQ
L=X+DX
UX-(U**UY+V**UX)/SUMSQ
U=X+DX
UX-(U**UY+V**UX)/SUMSQ
U=X+DY
UX-(U**UY+V**UX)/SUMSQ
U=X+DY
UX-(U**UY+V**UX)/SUMSQ
U=X+DY
UX-(U**UY+V**UX)/SUMSQ
UX-Y+DY
UX-(U**UY+V**UX)/SUMSQ
UX-Y+DY
                                                                                                           T=Y+DIBS (EY) +DAES (DX) .LE. TOL) GO TO 170 ICT=ICT+1 IT (ICT-500) 120.140.140 IF (ICT-500) 150.170 IT (ICT-500) 160.160 IT (ICT-500) 160.160 IER=3 GO TO 290 DO 180 L=1,NXX NT=KJ1-L+1
              170
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